

# Networks, instruments and data centres: what does your seismic (meta-) data really mean?





## Why an issue?

- many different data formats are existing, but uniform standard exists to send the data to DCs
- meta data of special importance!
- possibility to form “virtual networks” - especially important for regional events or earthquakes located close to a border region
- increasing the value of the network owners (more use gives more credits)
- simulating instruments is sometimes easier than correcting real data to true ground motion (relevant for synthetics)

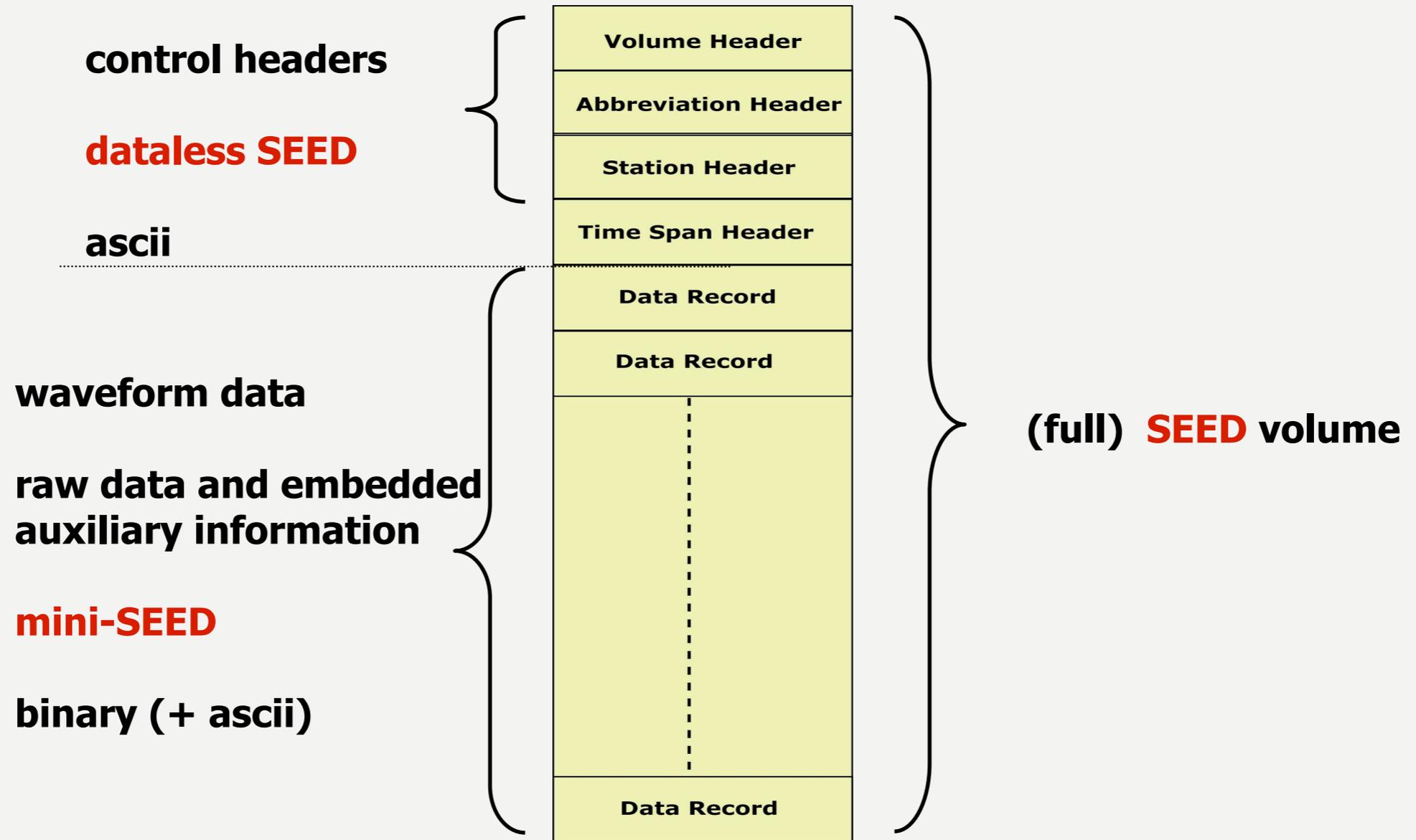


## What is SEED ?

- SEED is an international standard for the exchange of digital seismological data
- SEED was designed for use by the earthquake research community, primarily for the exchange between institutions of unprocessed earth motion data
- SEED is a format for digital data measured at one point in space and at equal intervals of time.



- recordings of digital time-series data (seismic waveforms)
- exchange of waveform data (real-time, archive)
- archiving of digital waveform data (IRIS-DMC, ODC, EIDA...)
- storage of meta-data (information about the data, e.g. station information, sensor)
- end user (analysis software)
- **not for non-time series data**
- **not for unequal time-interval sampled data (except logs)**
- **not designed for processed or synthetic data, but possible (IRIS already use it!)**
- parametric data possible (e.g. phase readings) but never used; IASPEI Seismic Format (ISF)





- **All site characteristics:**
  - Latitude, longitude, elevation
- **All instrument characteristics:**
  - Detailed responses - calibration, transfer functions
    - Sensor
    - External Preamp and Filter
    - Datalogger
  - Orientation angles and depth of emplacement
  - Serial numbers
  - Instrument type
- **Effective date/time**

# System Response or: Filters and Their Description

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F. Scherbaum (Univ. Potsdam)

# From source to receiver...

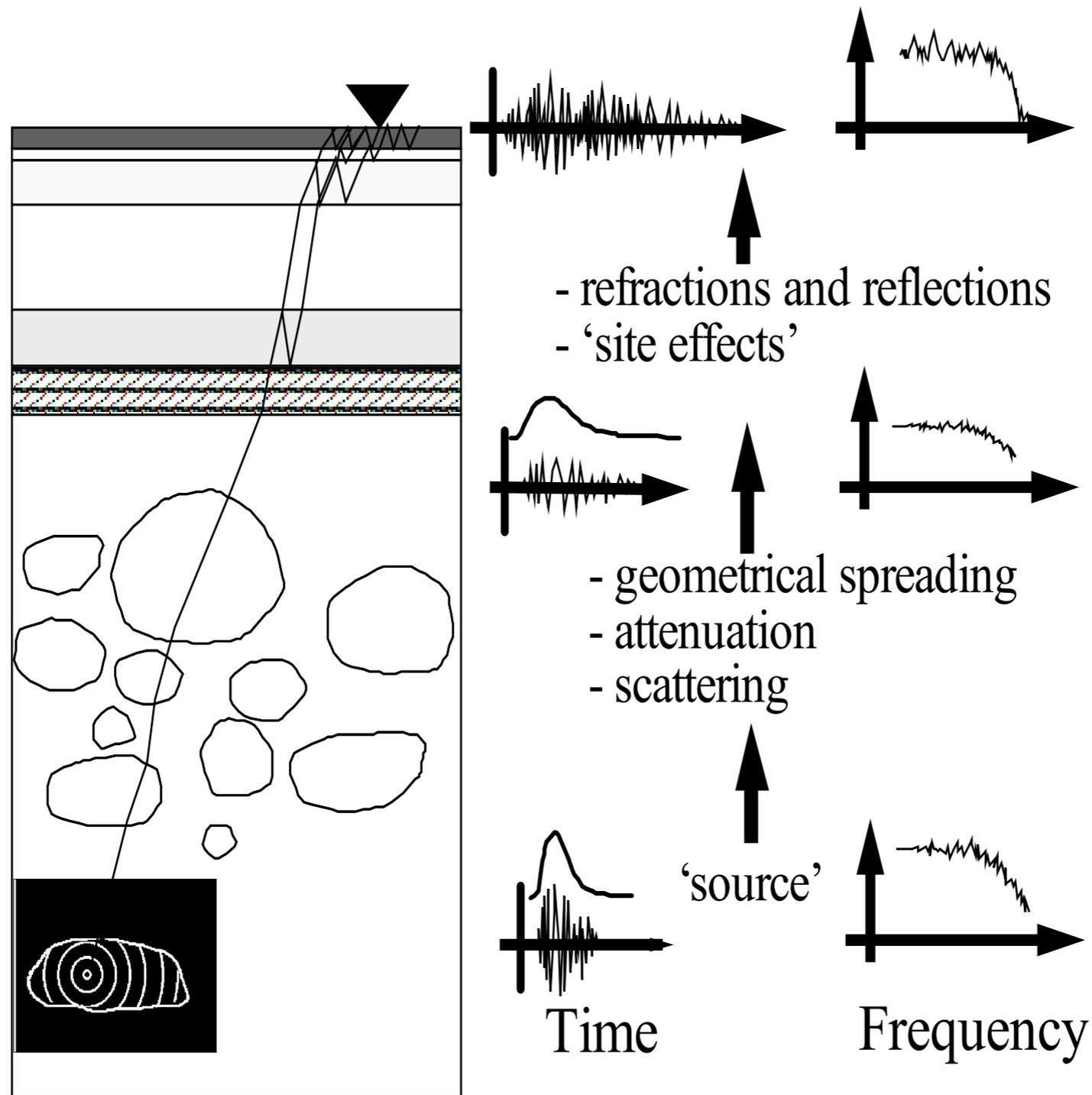
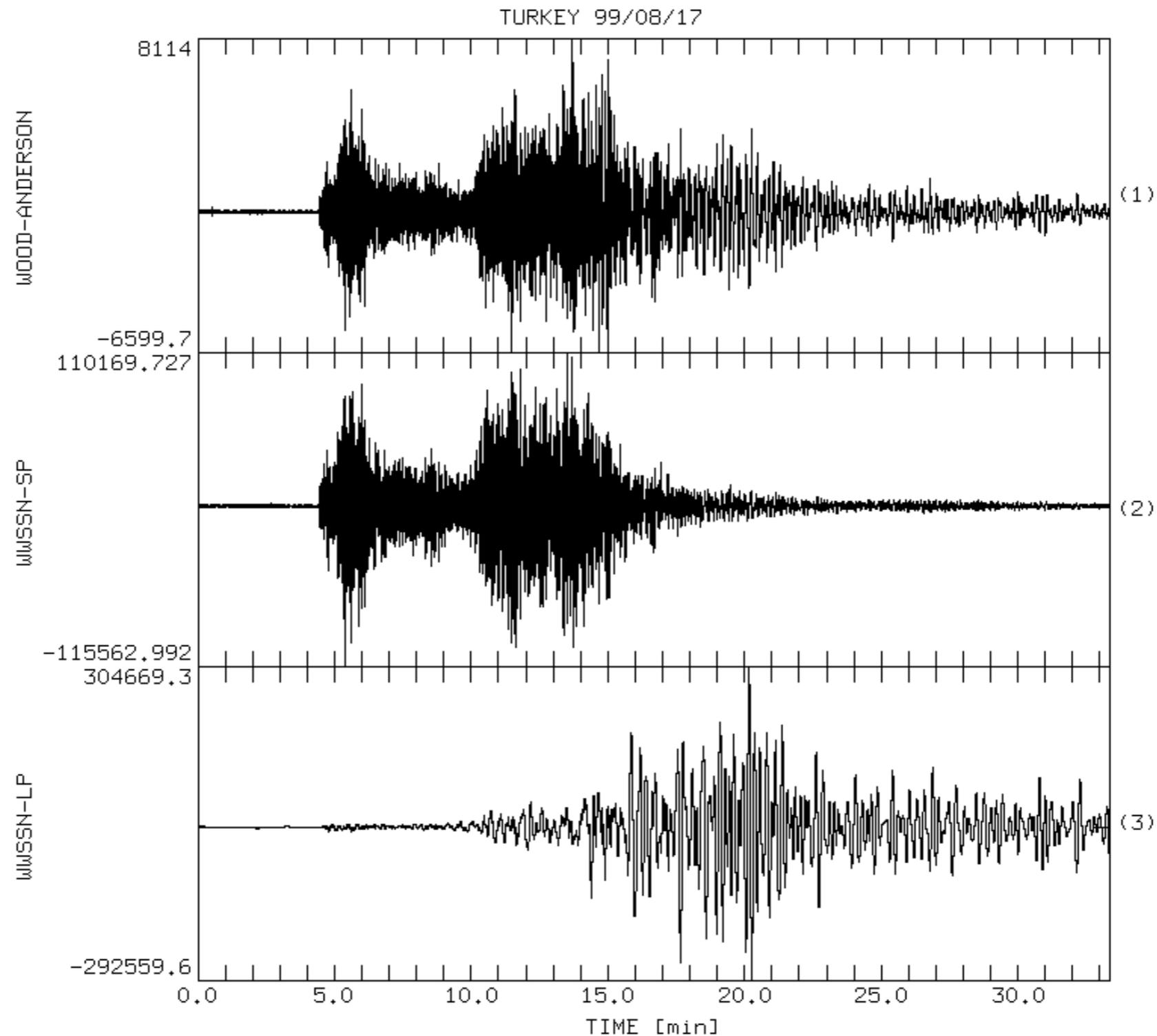


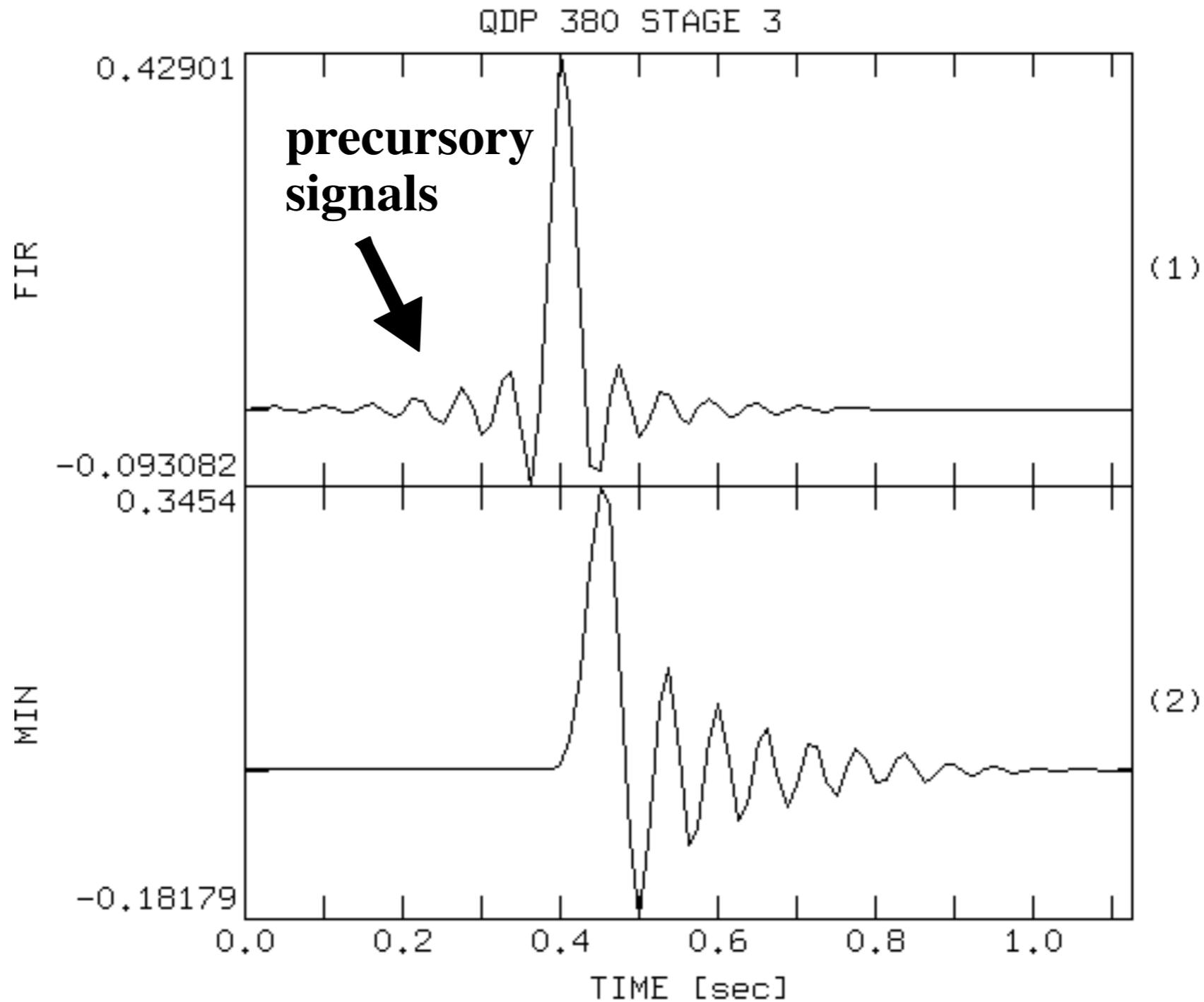
Fig. 1.1 Signal distortion during wave propagation from the earthquake source to the surface.

# Influence of recording system



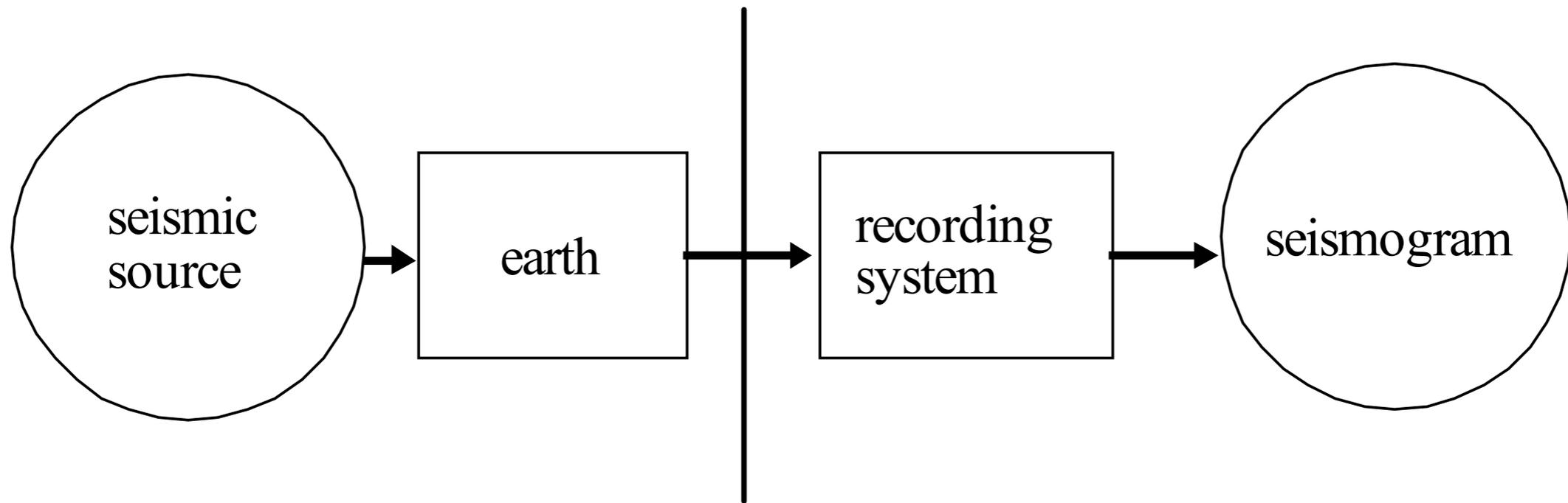
**Fig. 1.2** Vertical component record of the Izmit earthquake in Turkey (1999/08/17) recorded at station MA13 of the University of Potsdam during a field experiment in Northern Norway. Shown from top to bottom are the vertical component records for a: Wood-Anderson, a WWSSN SP, and a WWSSN LP instrument simulation.

# Sampling process



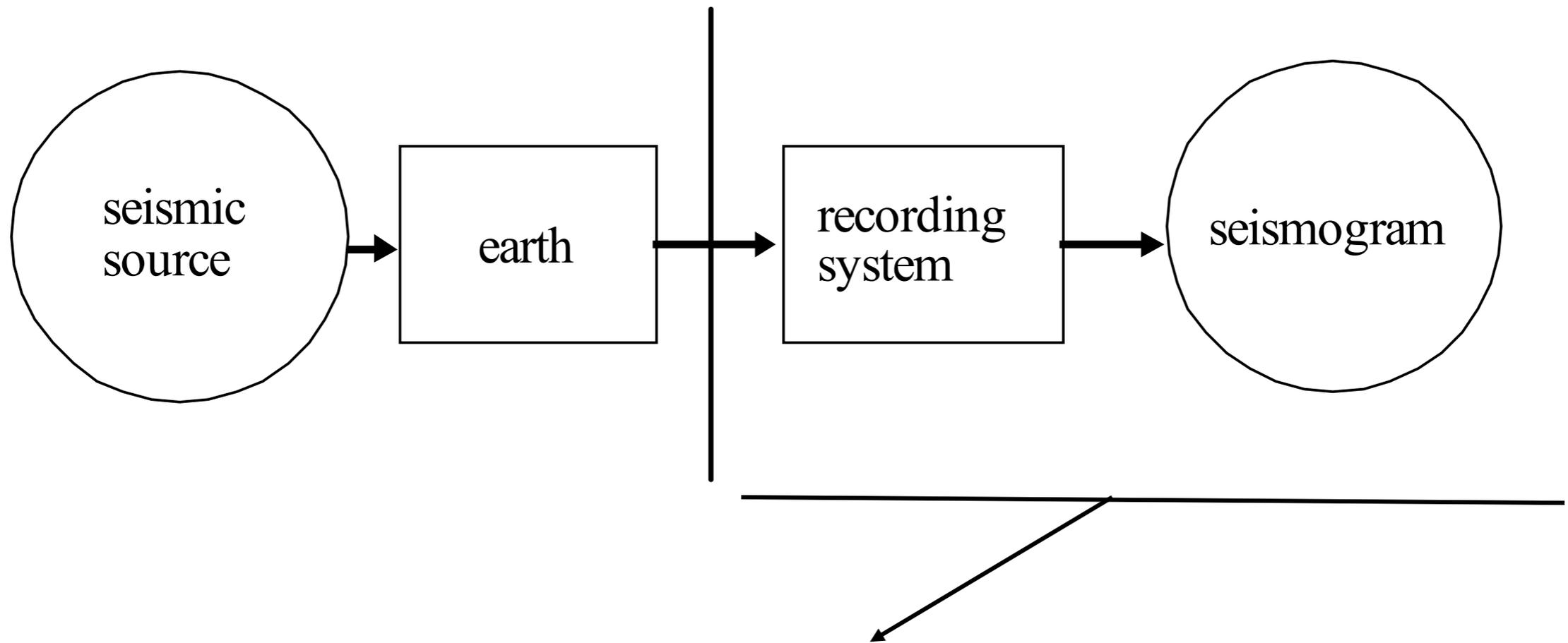
**Fig. 1.3** Impulse response of stage 3 of the two-sided decimation filter incorporated in the Quanterra QDP 380 system (top trace). The bottom trace shows a filter response with an identical amplitude but different phase response.

# Seismogram



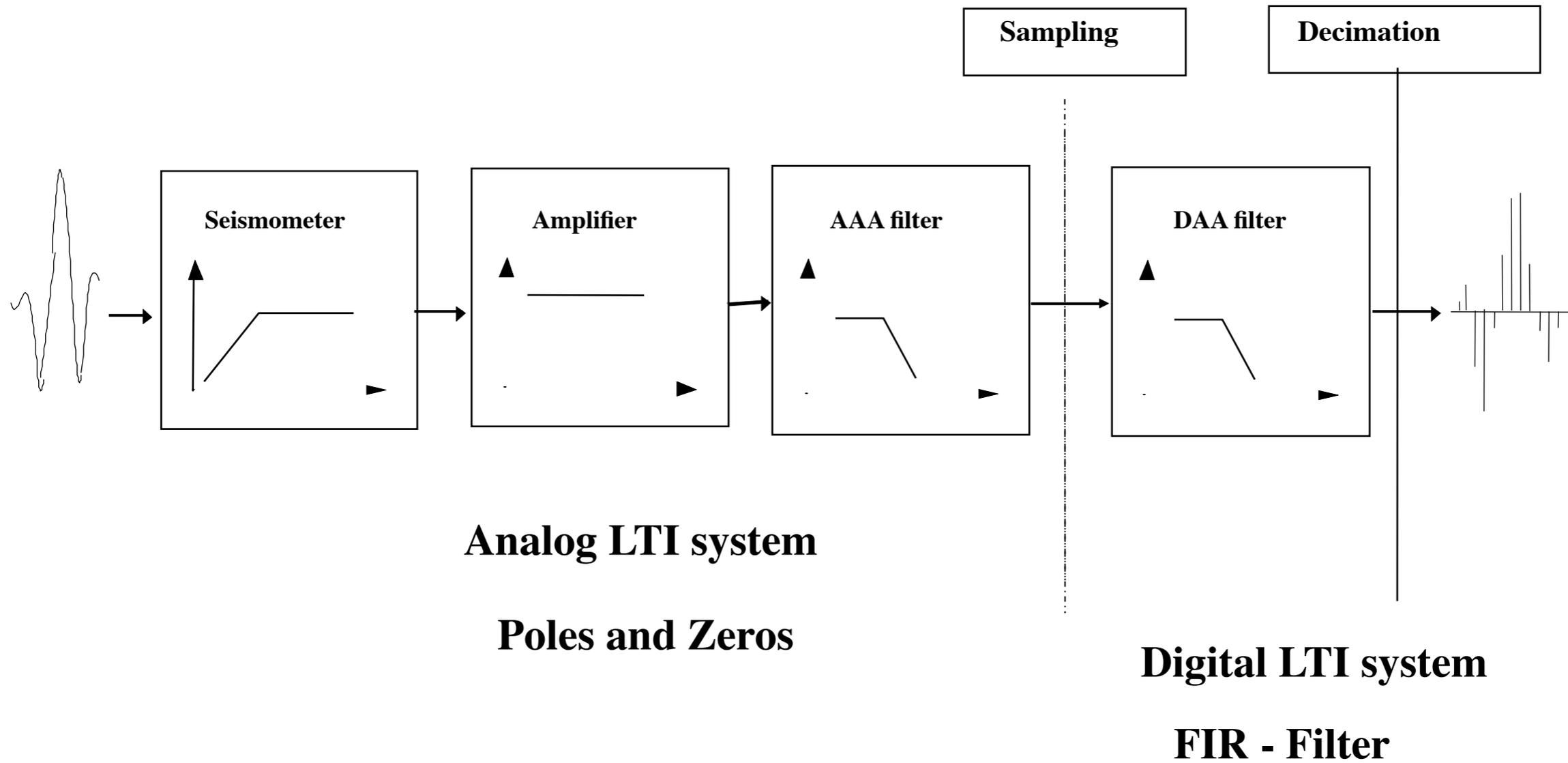
**Fig. 1.11** System diagram of a seismogram

# Seismogram



This part is covered by SEED

# SEED response information



# << IRIS SEED Reader, Release 4.4 >>

#

# ===== CHANNEL RESPONSE DATA =====

B050F03 Station: RJOB  
B050F16 Network: BW  
B052F03 Location: ??  
B052F04 Channel: EHZ  
B052F22 Start date: 2007,199  
B052F23 End date: No Ending Time

#

```
# +-----+
# + | Response (Poles & Zeros), RJOB ch EHZ | +
# +-----+
#
```

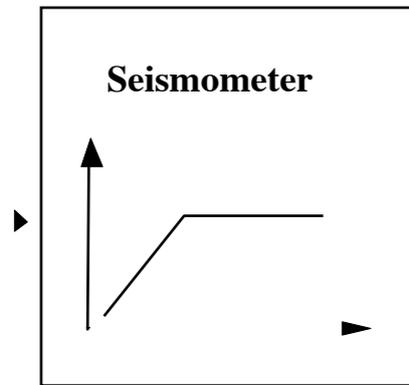
B053F03 Transfer function type: A [Laplace Transform (Rad/sec)]  
B053F04 Stage sequence number: 1  
B053F05 Response in units lookup: M/S - Velocity in Meters per Second  
B053F06 Response out units lookup: V - Volts  
B053F07 A0 normalization factor: 6.0077E+07  
B053F08 Normalization frequency: 1  
B053F09 Number of zeroes: 2  
B053F14 Number of poles: 5

# Complex zeroes:

```
# i real imag real_error imag_error
B053F10-13 0 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00
B053F10-13 1 0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00
```

# Complex poles:

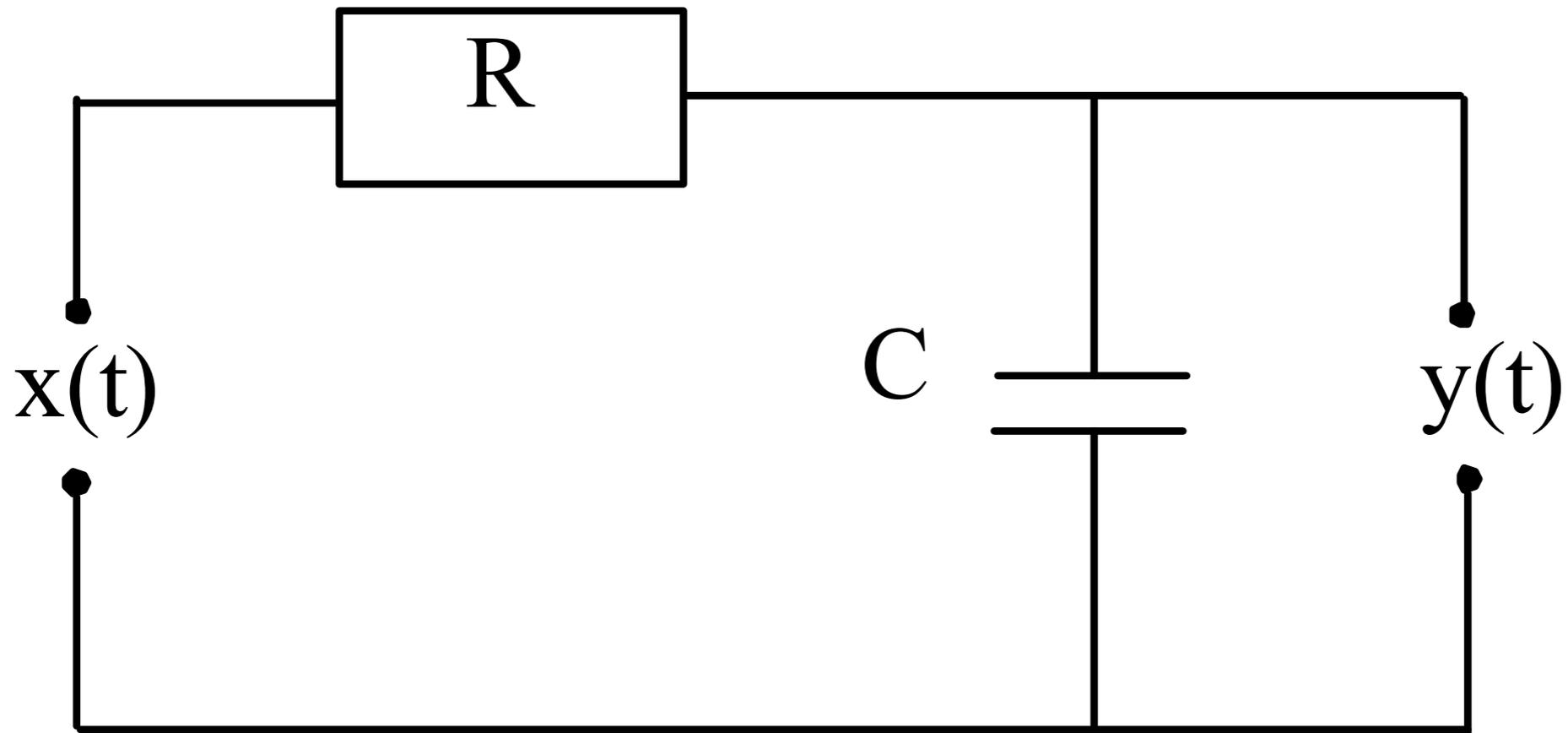
```
# i real imag real_error imag_error
B053F15-18 0 -3.700400E-02 3.701600E-02 0.000000E+00 0.000000E+00
B053F15-18 1 -3.700400E-02 -3.701600E-02 0.000000E+00 0.000000E+00
B053F15-18 2 -2.513300E+02 0.000000E+00 0.000000E+00 0.000000E+00
B053F15-18 3 -1.310400E+02 -4.672900E+02 0.000000E+00 0.000000E+00
B053F15-18 4 -1.310400E+02 4.672900E+02 0.000000E+00 0.000000E+00
```



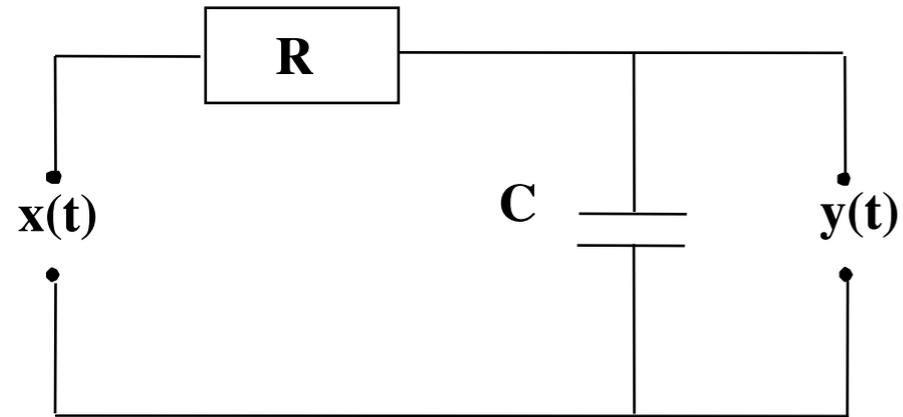
# Definition

- **Filters** or **systems** are, in the most general sense, devices (in the physical world) or algorithms (in the mathematical world) which act on some **input signal** to produce a - possibly different - **output signal**.

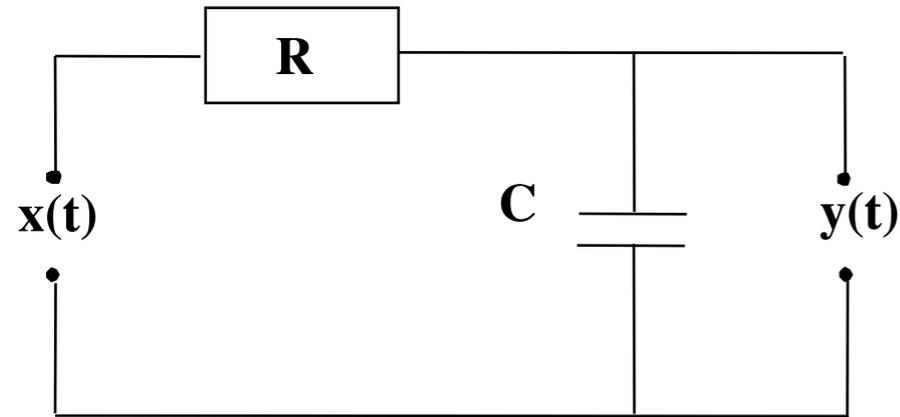
# RC filter



# Differential equation

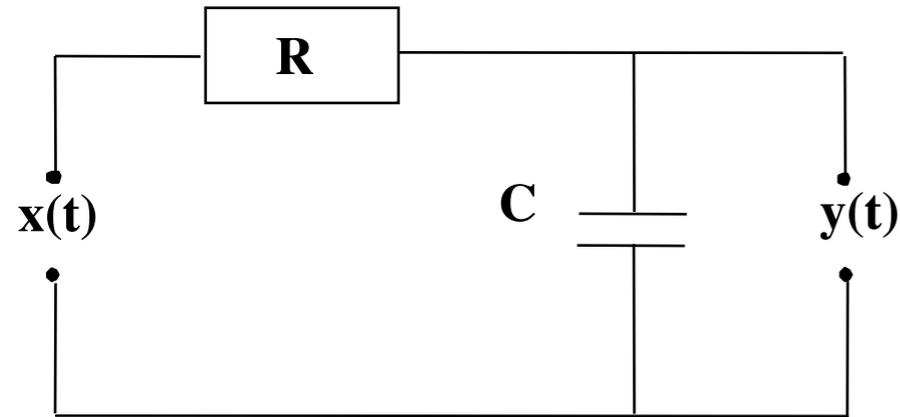


# Differential equation



Voltage balance?

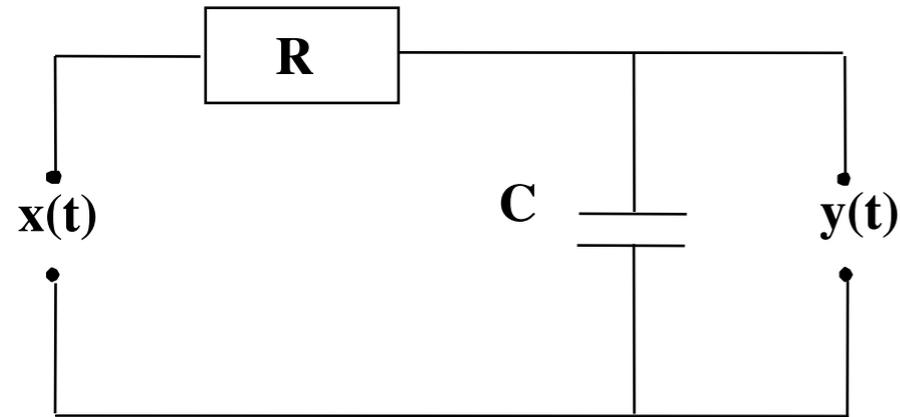
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$$RI(t) + y(t) = x(t)$$

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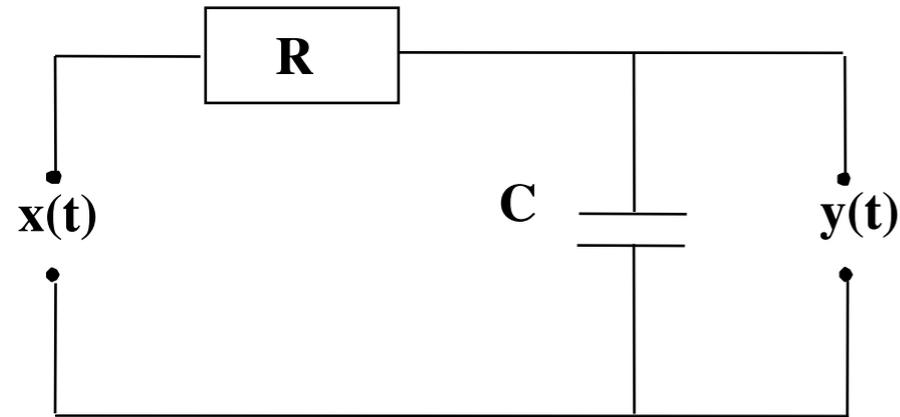
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Current through resistor  $R$  and capacitance  $C$ :

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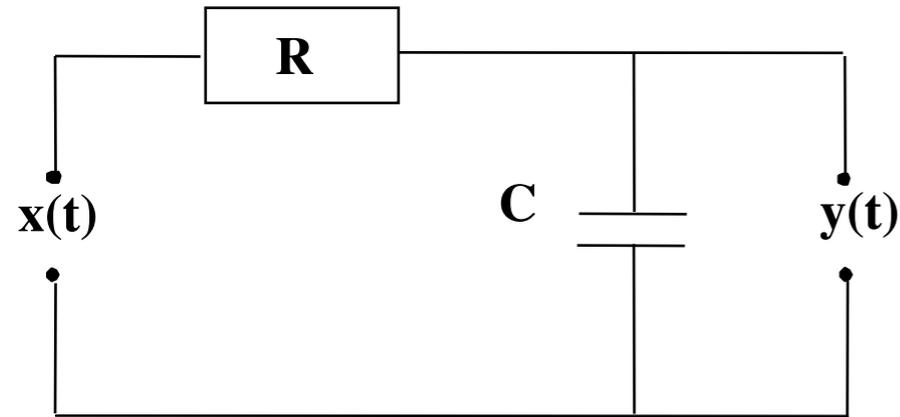
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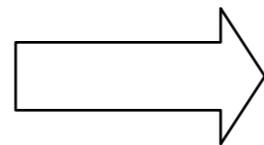


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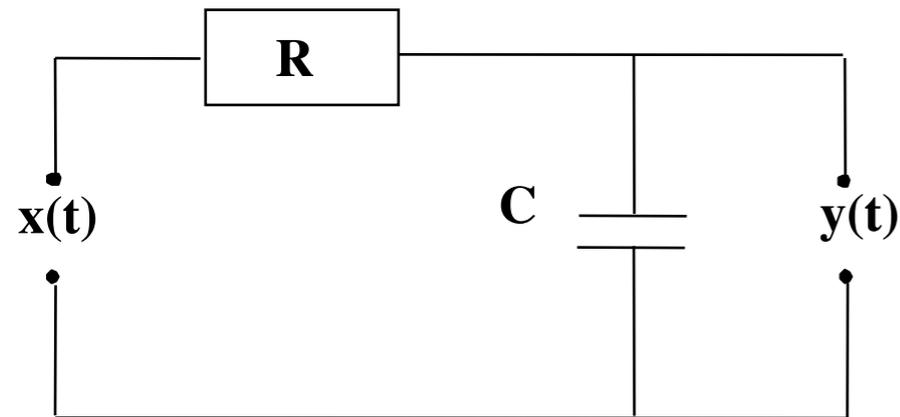
Current through resistor R and capacitance C:

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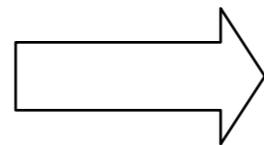


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**First order linear differential equation**

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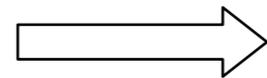
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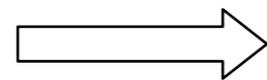
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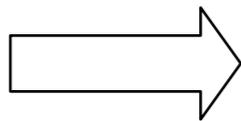
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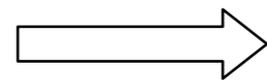
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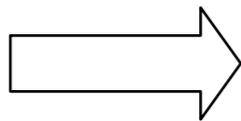
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**Frequency response function**

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The frequency response function can be measured by comparing output and input signals to the system **without further knowledge of the physics going on inside the filter!**

# Transfer function and Laplace transform

Bilateral Laplace transform of  $f(t)$ : 
$$\mathbf{L} [f(t)] = \int_{-\infty}^{\infty} f(t)e^{-st} dt$$

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**Property:** 
$$\mathbf{L} [\dot{f}(t)] = s \cdot F(s)$$

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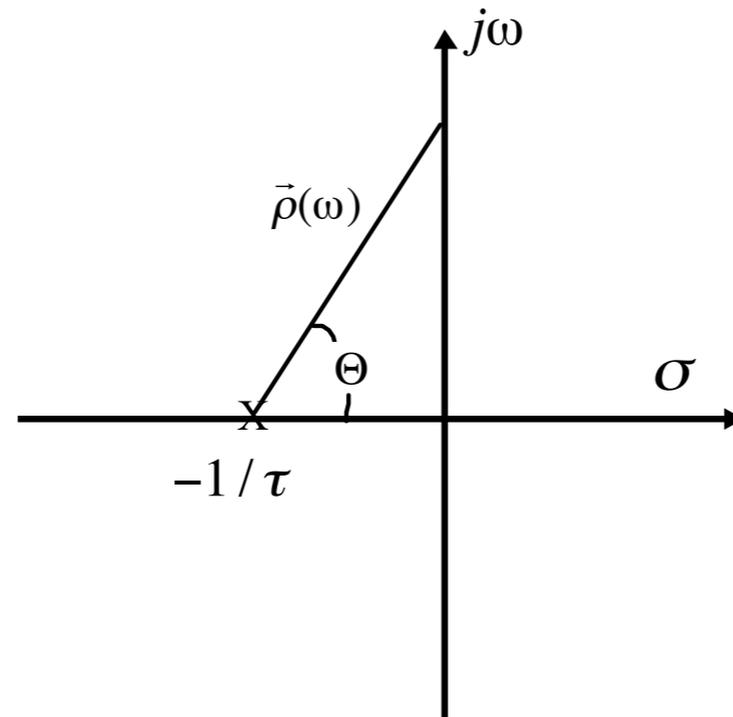
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$s = -1/\tau$  “pole” of the transfer function

# The frequency response function and the pole position



**Fig. 2.10** Representation of the RC filter in the  $s$  plane. The pole location at  $-1/\tau$  is marked by an X.

Transfer function RC filter:

$$T(s) = \frac{1}{1 + s\tau} = \frac{1}{\tau} \left[ \frac{1}{(1/\tau) + s} \right]$$

For  $s = j\omega$ ,  $\omega$  moves along the imaginary axis  $\Rightarrow T(j\omega) = \frac{1}{\tau} \left[ \frac{1}{(1/\tau) + j\omega} \right]$

$1/\tau + j\omega$  represents the vector  $\rho(j\omega)$

which is pointing from the pole position towards the actual frequency on the imaginary axis.

# General linear time invariant systems

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**Generalization of concepts**

# General linear time invariant systems

## Generalization of concepts

Rewrite the differential equation for the RC filter:

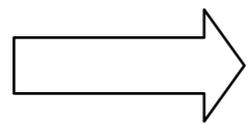
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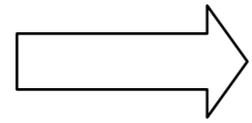
RC filter special case of  
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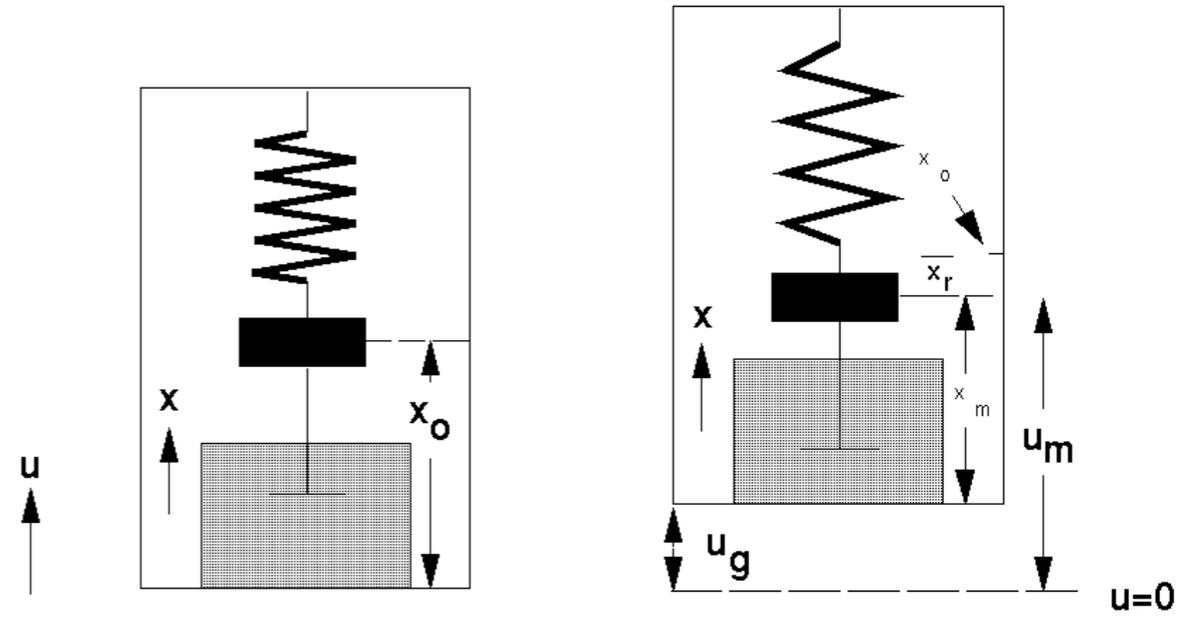
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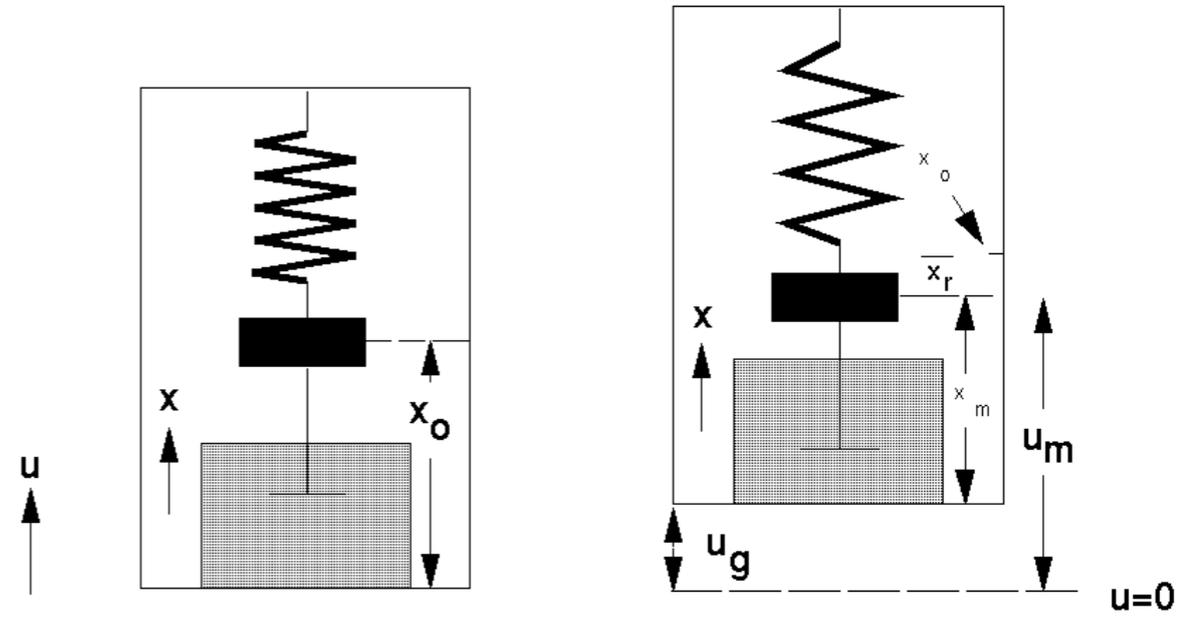
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# Seismometer

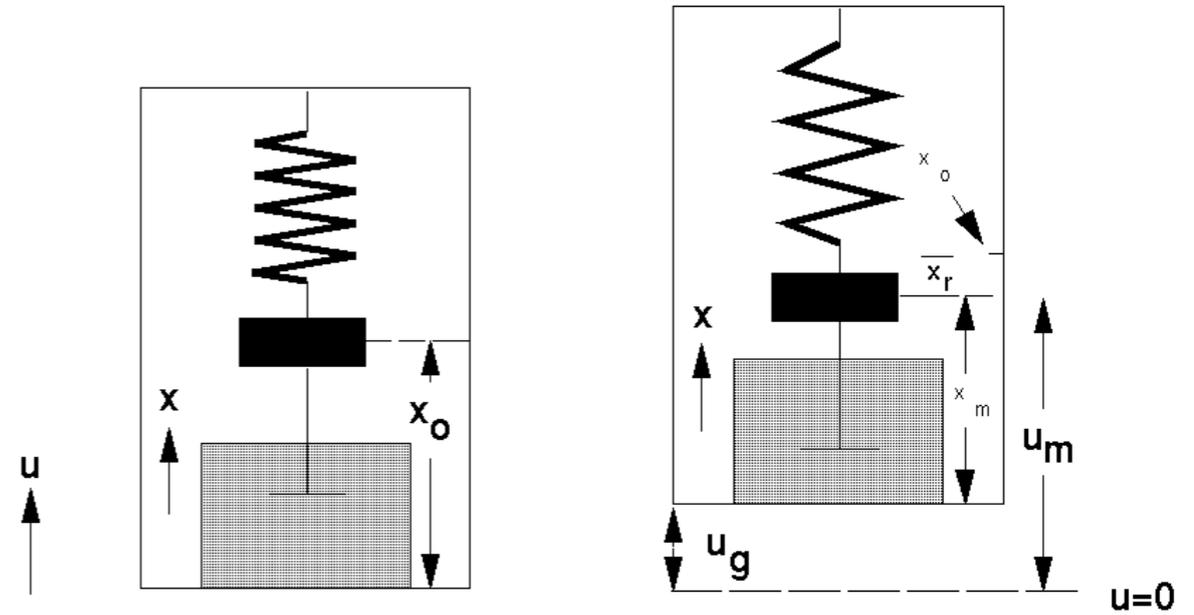


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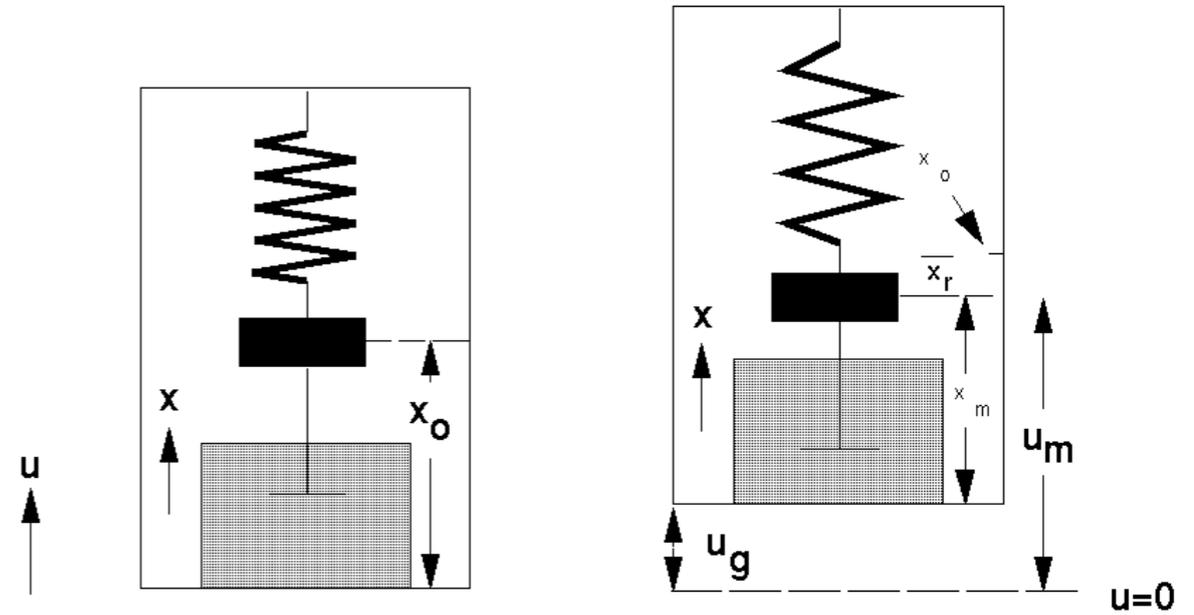


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• *The spring* —  $f_{sp} = -kx_r(t)$

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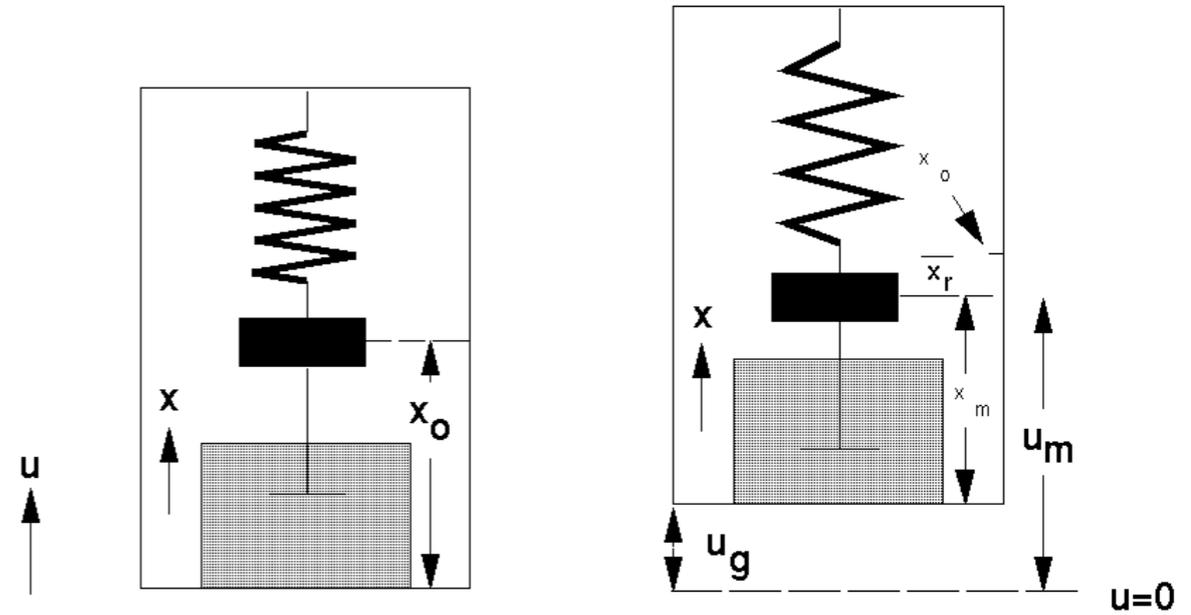
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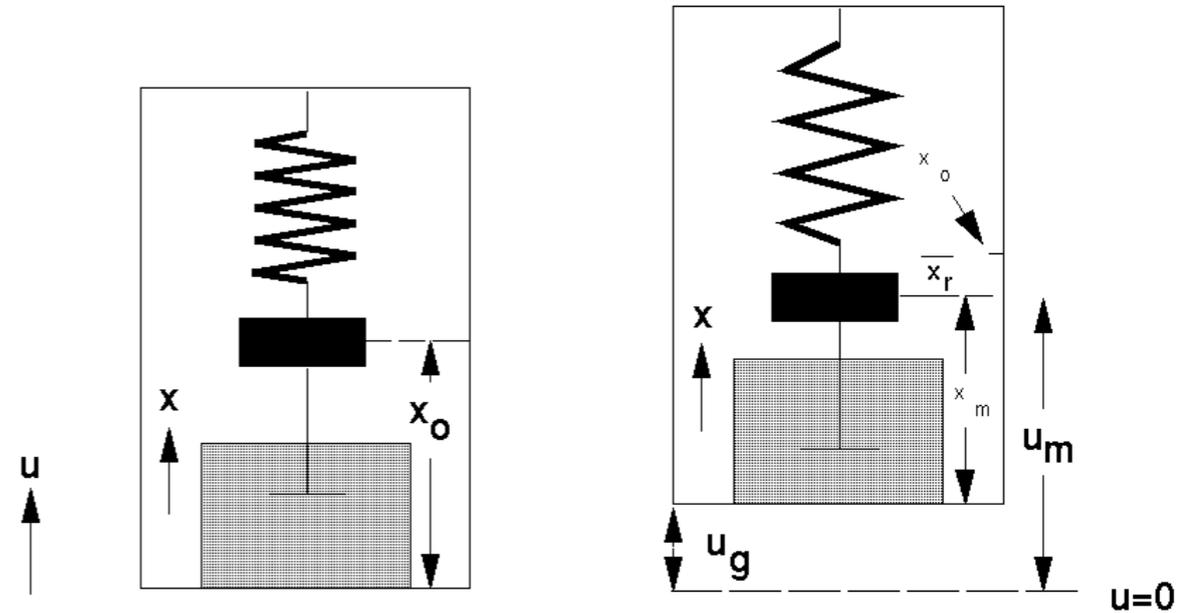
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$$-m\ddot{u}_m(t) - D\dot{x}_m(t) - kx_r(t) = 0 \quad \text{2nd order LTI !!}$$

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**Transfer function:**  $T(s) = \frac{X_r(s)}{U_g(s)} = \frac{-s^2}{s^2 + 2\varepsilon s + \omega_0^2}$

# Seismometer Transfer function

Laplace transform of  $\ddot{x}_r(t) + 2\varepsilon\dot{x}_r(t) + \omega_0^2x_r(t) = -\ddot{u}_g(t)$

$$\Rightarrow s^2X_r(s) + 2\varepsilon sX_r(s) + \omega_0^2X_r(s) = -s^2U_g(s)$$

**Transfer function:**  $T(s) = \frac{X_r(s)}{U_g(s)} = \frac{-s^2}{s^2 + 2\varepsilon s + \omega_0^2}$

Since a quadratic equation  $x^2 + bx + c = 0$  has the roots

$$x_{1,2} = -\frac{b}{2} \pm \sqrt{\frac{b^2}{4} - c}$$

pole positions  $p_{1,2}$ :

$$\begin{aligned} p_{1,2} &= -\varepsilon \pm \sqrt{\varepsilon^2 - \omega_0^2} \\ &= -h\omega_0 \pm \omega_0 \sqrt{h^2 - 1} \\ &= -\left(h \pm \sqrt{h^2 - 1}\right)\omega_0 \end{aligned}$$

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For the underdamped case ( $h < 1$ ) the pole position becomes

$$p_{1,2} = -\left(h \pm j\sqrt{1 - h^2}\right)\omega_0$$

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For the underdamped case ( $h < 1$ ) the pole position becomes

$$p_{1,2} = -\left(h \pm j\sqrt{1 - h^2}\right)\omega_0$$

with the pole distance from the origin

$$|p_{1,2}| = \left| \left( h \pm j\sqrt{1 - h^2} \right) \right| \cdot |\omega_0| = \sqrt{h^2 + (1 - h^2)} \cdot |\omega_0| = |\omega_0|$$

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 p_{1,2} &= -\varepsilon \pm \sqrt{\varepsilon^2 - \omega_0^2} \\
 &= -h\omega_0 \pm \omega_0 \sqrt{h^2 - 1} \\
 &= -\left(h \pm \sqrt{h^2 - 1}\right)\omega_0
 \end{aligned}$$

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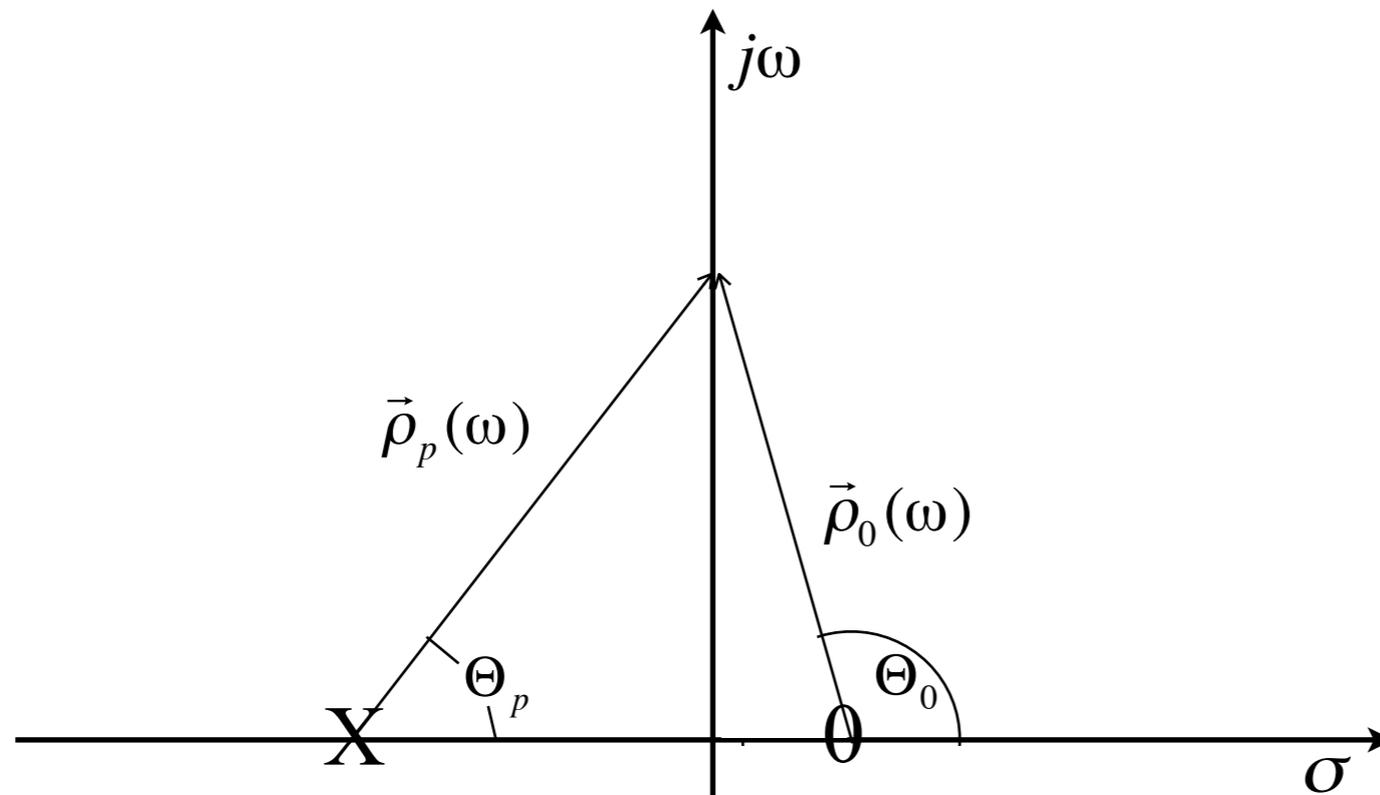
$$|p_{1,2}| = \left| \left( h \pm j\sqrt{1 - h^2} \right) \right| \cdot |\omega_0| = \sqrt{h^2 + (1 - h^2)} \cdot |\omega_0| = |\omega_0|$$

Therefore, the poles of an underdamped seismometer are located in the left half of the s plane in a distance of  $|\omega_0|$  from the the origin. The quantity  $h |\omega_0|$  gives the distance from the imaginary axis.

# Consequences of transition from single pole to general N-th order system

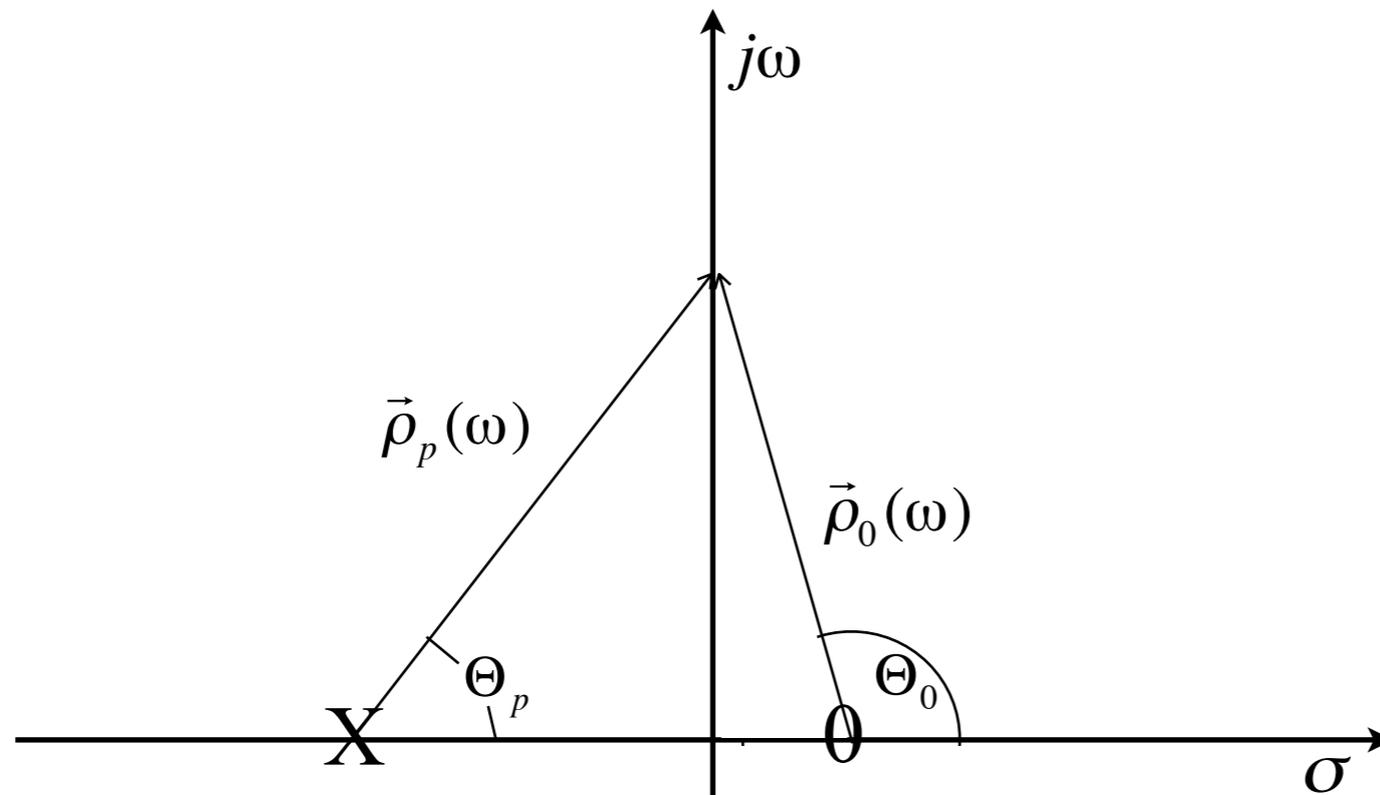
- No major change in concept
- Zeros in addition to poles
- Can be treated in very similar way

# Graphical estimation of the frequency response function



**Fig. 3.2** Complex s plane representation of a system with a single pole and zero. The pole and zero locations are marked by an X, and a 0, respectively.

# Graphical estimation of the frequency response function



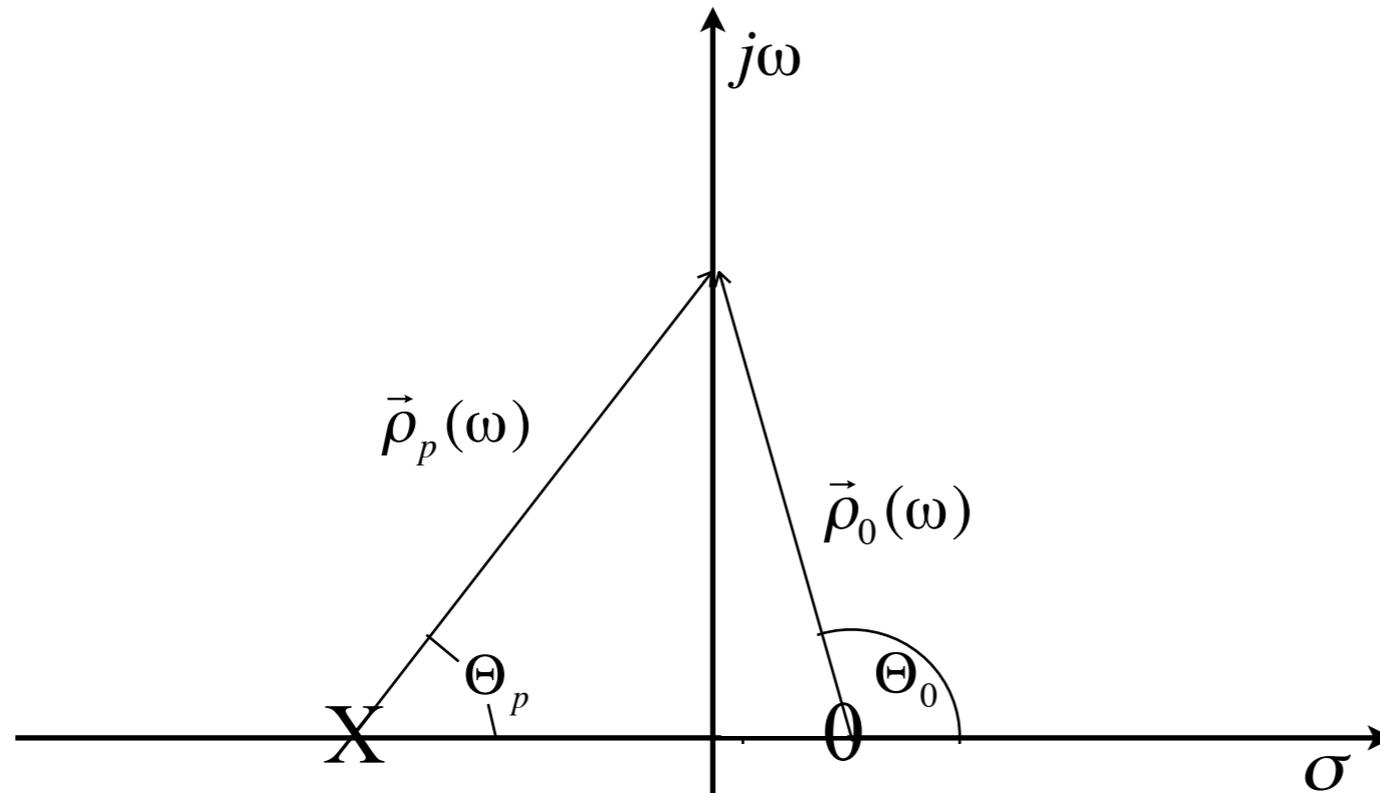
**Fig. 3.2** Complex s plane representation of a system with a single pole and zero. The pole and zero locations are marked by an X, and a 0, respectively.

**Transfer function:**

$$T(s) = \frac{s - s_0}{s - s_p}$$

$s_0$  and  $s_p$ : position of the zero and the pole, respectively.

# Graphical estimation of the frequency response function

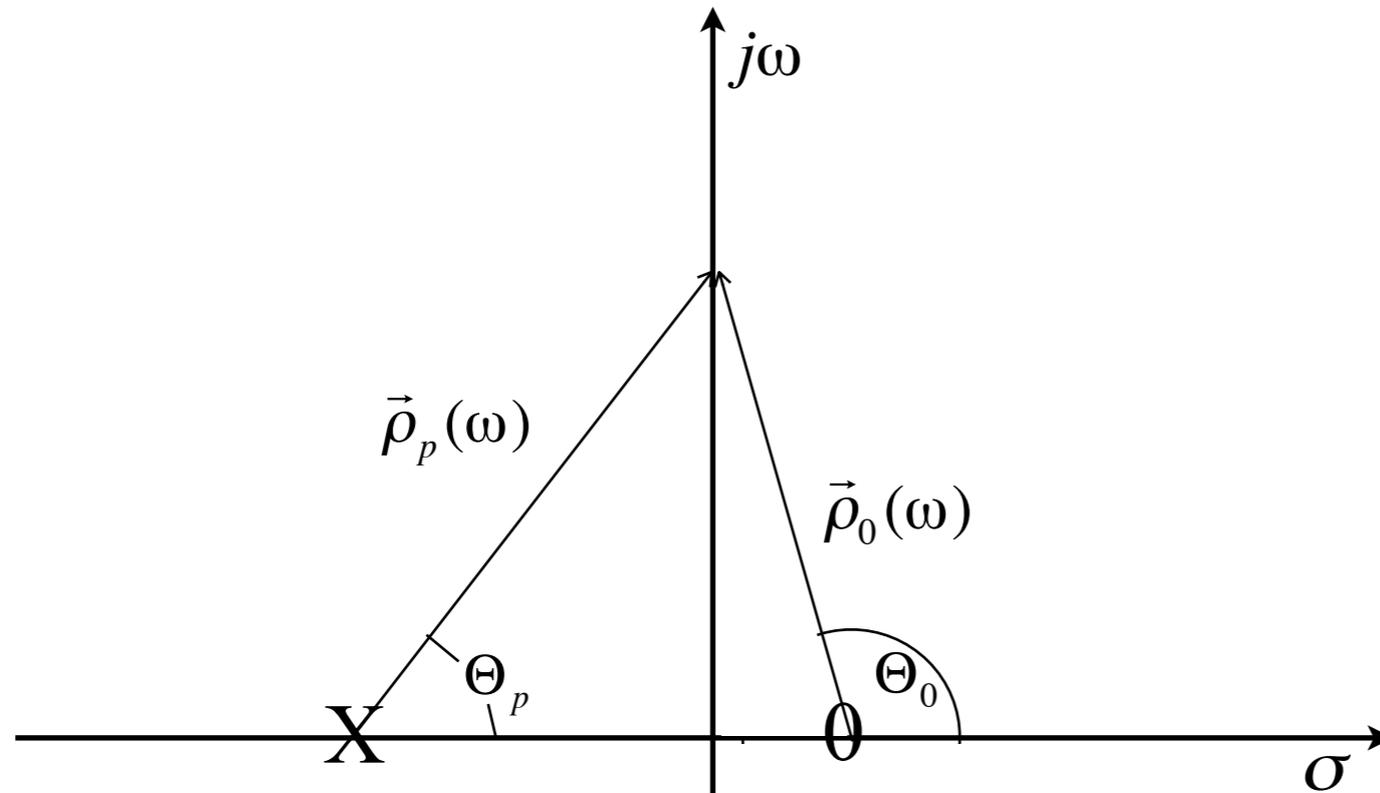


**Fig. 3.2** Complex  $s$  plane representation of a system with a single pole and zero. The pole and zero locations are marked by an X, and a 0, respectively.

**Transfer function:**  $T(s) = \frac{s - s_0}{s - s_p}$   $s_0$  and  $s_p$ : position of the zero and the pole, respectively.

**Frequency response function:** ( $s = j\omega$ )  $T(j\omega) = \frac{j\omega - s_0}{j\omega - s_p}$

# Graphical estimation of the frequency response function



**Fig. 3.2** Complex  $s$  plane representation of a system with a single pole and zero. The pole and zero locations are marked by an X, and a 0, respectively.

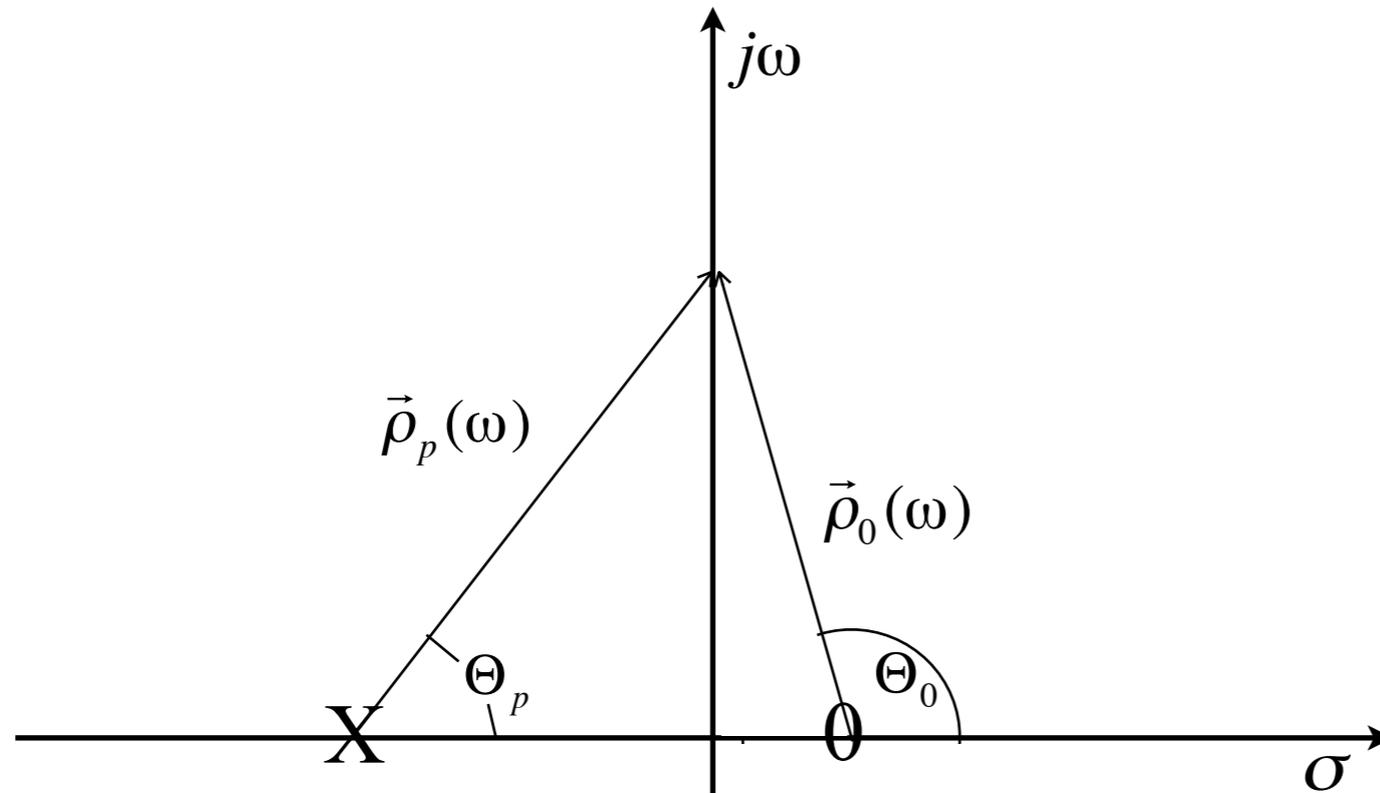
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$j\omega - s_p \rightarrow$  vector  $\vec{\rho}_p(\omega)$

$j\omega - s_0 \rightarrow$  vector  $\vec{\rho}_0(\omega)$

# Graphical estimation of the frequency response function



**Fig. 3.2** Complex  $s$  plane representation of a system with a single pole and zero. The pole and zero locations are marked by an X, and a 0, respectively.

**Transfer function:**  $T(s) = \frac{s - s_0}{s - s_p}$   $s_0$  and  $s_p$ : position of the zero and the pole, respectively.

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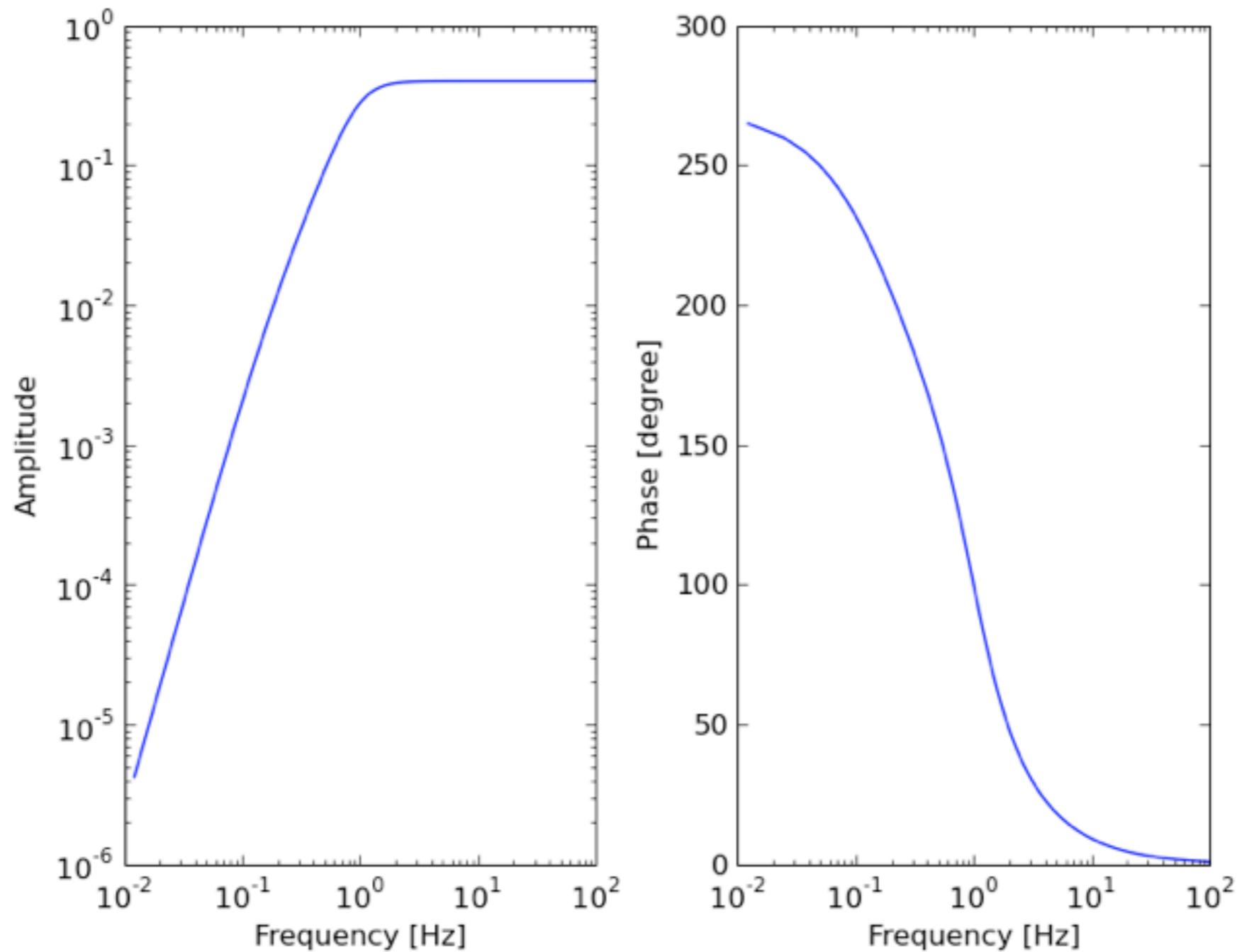
$j\omega - s_p \rightarrow$  vector  $\vec{\rho}_p(\omega)$

$j\omega - s_0 \rightarrow$  vector  $\vec{\rho}_0(\omega)$

$$T(j\omega) = |\rho_0(\omega)| e^{j\Theta_0} \frac{1}{|\rho_p(\omega)|} e^{-j\Theta_p}$$

# Simulation Process

Frequency Response of LE-3D/1s Seismometer



# **Inverse and simulation filtering of digital seismograms**

# **Inverse and simulation filtering of digital seismograms**

**NEXT:** From filter problem to the simulation problem - the conversion of digital (broad-band) records into those from different seismograph systems.

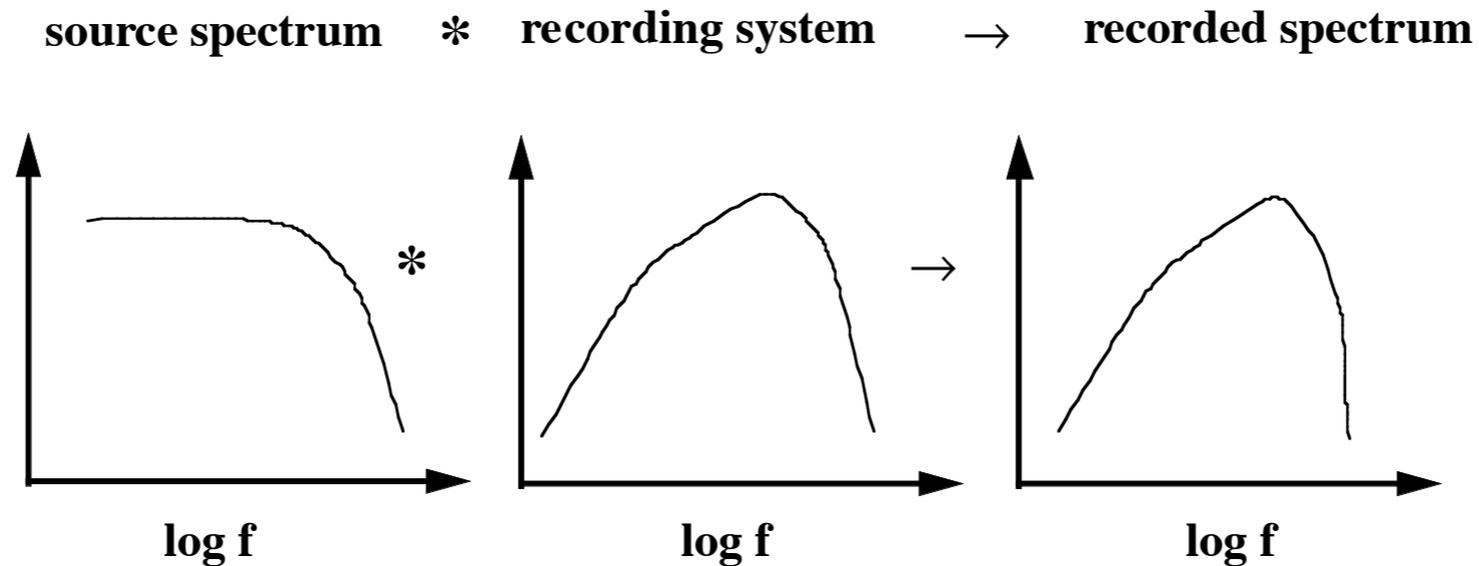
# Inverse and simulation filtering of digital seismograms

**NEXT:** From filter problem to the simulation problem - the conversion of digital (broad-band) records into those from different seismograph systems.

**REASON:** Signal amplitudes or onset time determination in a manner consistent with other observatories. Simulated systems will most commonly belong to the standard classes of instruments described by Willmore (1979) because **there is no single, optimum class of instruments for the detection and analysis of different types of seismic waves. The different seismic magnitude definitions are based on different instruments!**

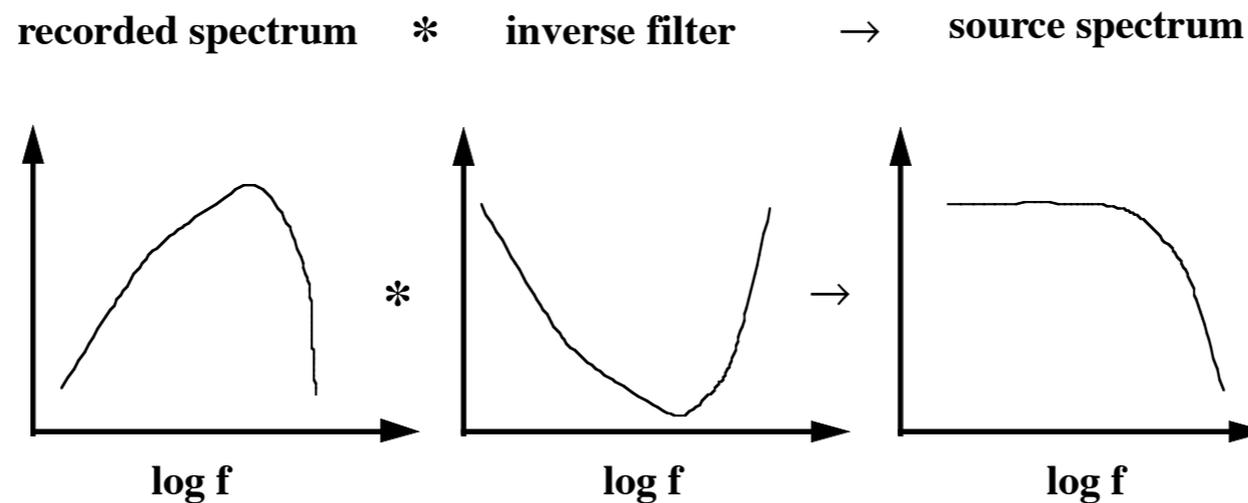
# Stability problems

## Noise free situation



**Fig. 9.3** Recording the displacement spectrum of an idealized earthquake source.

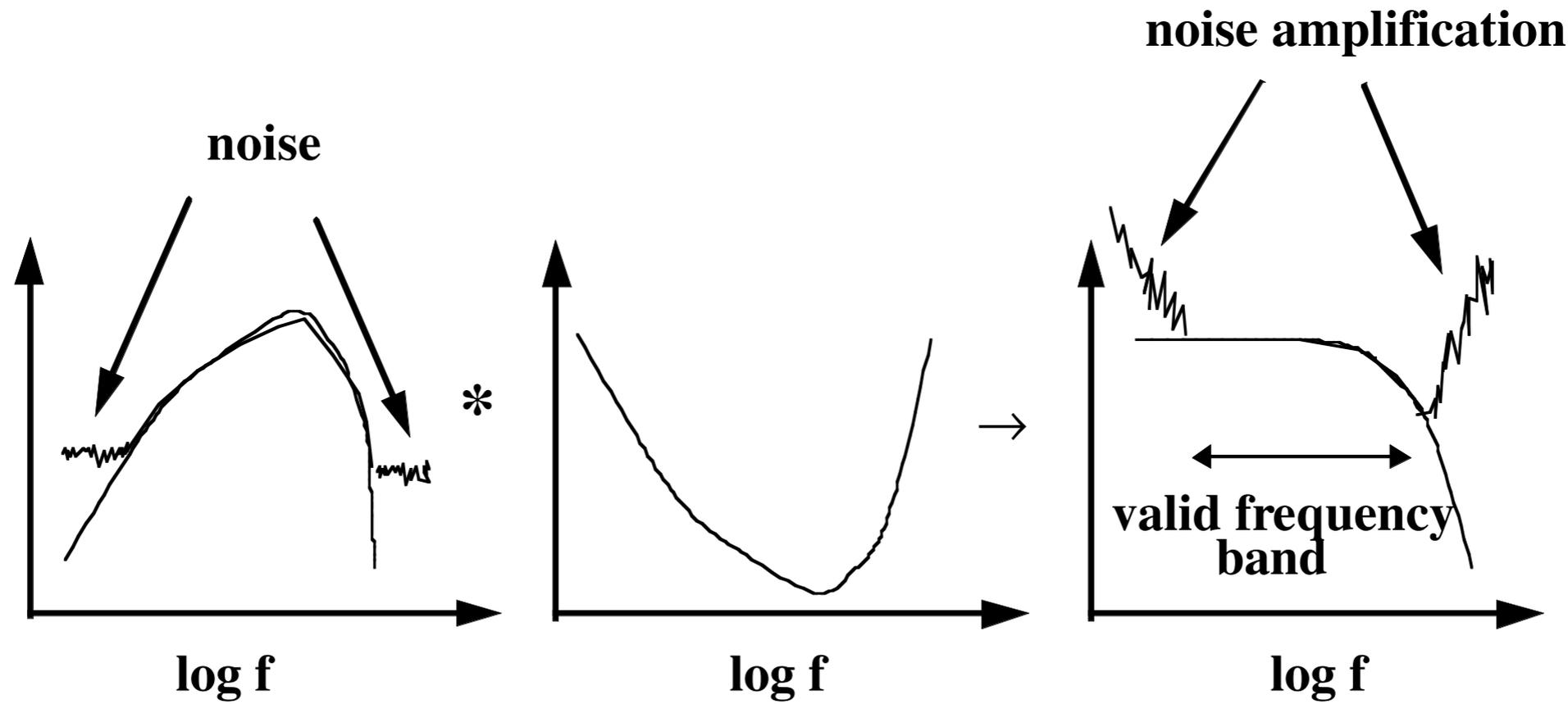
## Recovery of source spectrum:



**Fig. 9.4** Recovering the source spectrum by inverse filtering in the noise-free case.

# Noisy situation

noisy' spectrum \* inverse filter → 'noisy' source spectrum



**Fig. 9.5** Noise amplification by inverse filtering. The solid line in the left panel shows the signal plus noise while the noise-free signal is shown by the dashed line.

# Noisy situation

# Noisy situation

## Problem:

- Decrease of signal-to-noise ratio (SNR) outside the pass-band of the recording instrument
- magnification of the inverse filter is largest where SNR is smallest. Thus, noise in this frequency band will be amplified (instability!).

# Noisy situation

## Problem:

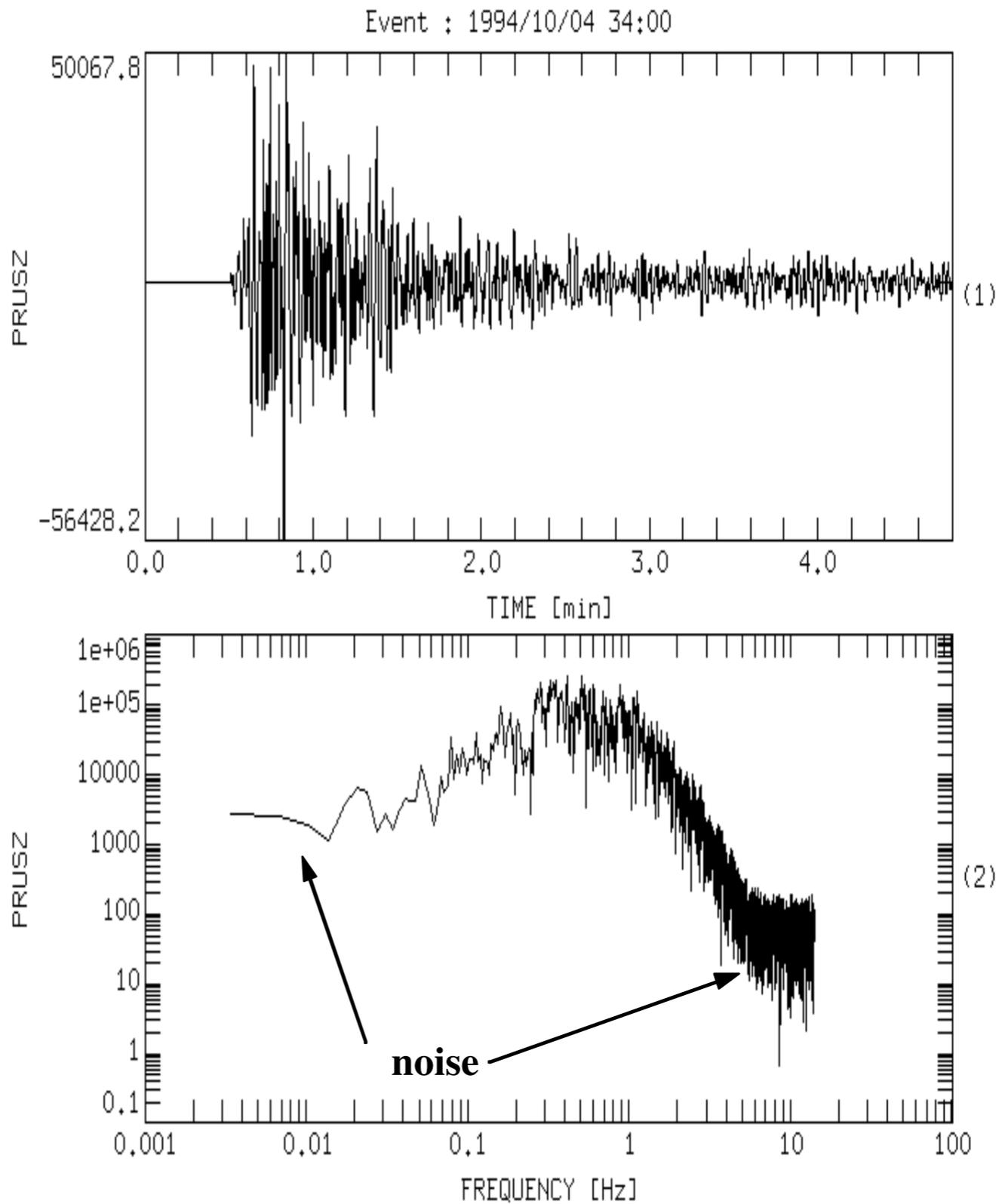
- Decrease of signal-to-noise ratio (SNR) outside the pass-band of the recording instrument
- magnification of the inverse filter is largest where SNR is smallest. Thus, noise in this frequency band will be amplified (instability!).

## Consequence:

- The instrument response can only be deconvolved within a certain *valid frequency band* in the presence of noise. The valid frequency band depends on both the signal-to noise ratio and the slope of the frequency response function of the recording systems.

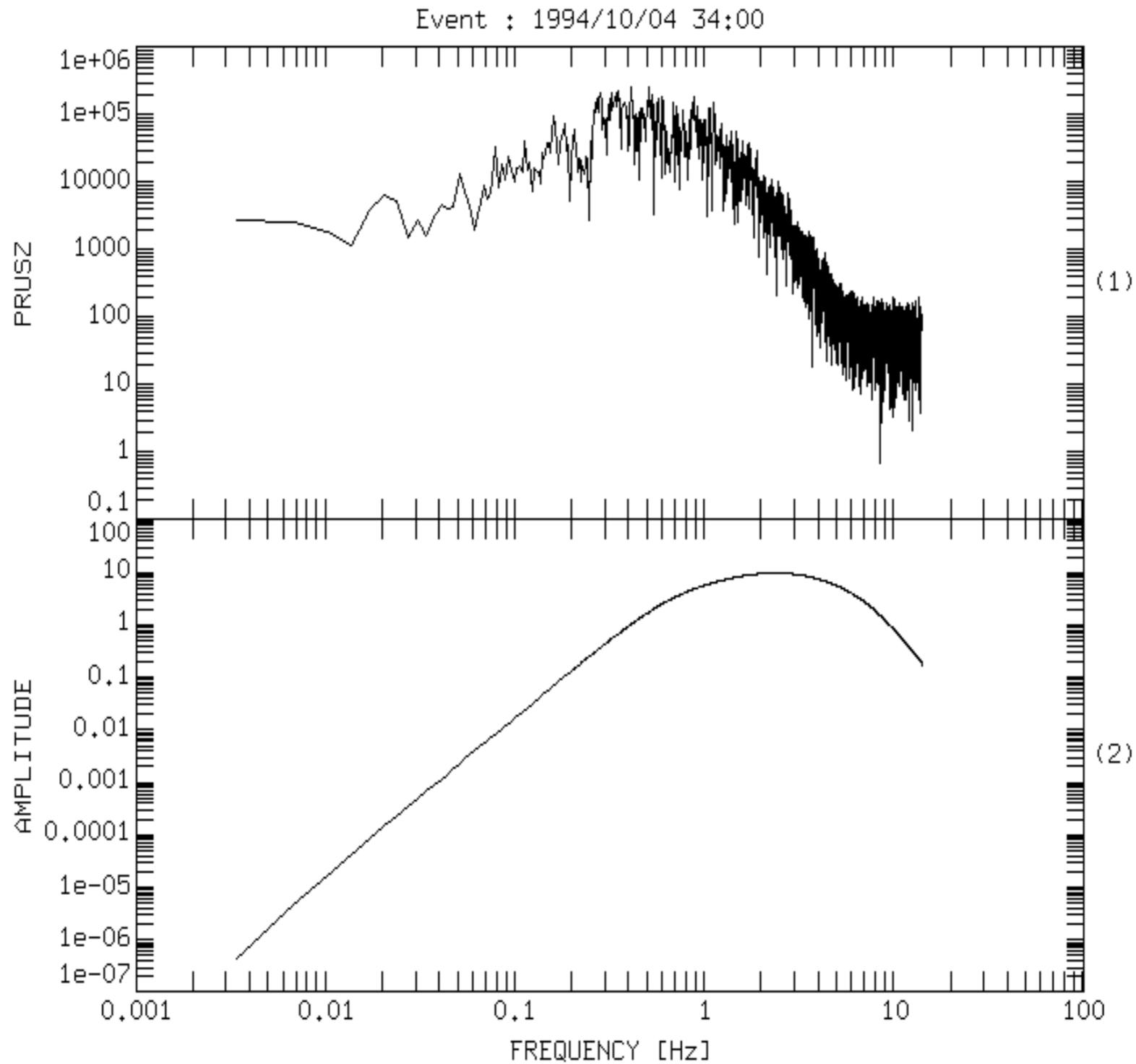
# Example

Station Pruhonice (PRU) of the Czech Academy of Sciences.



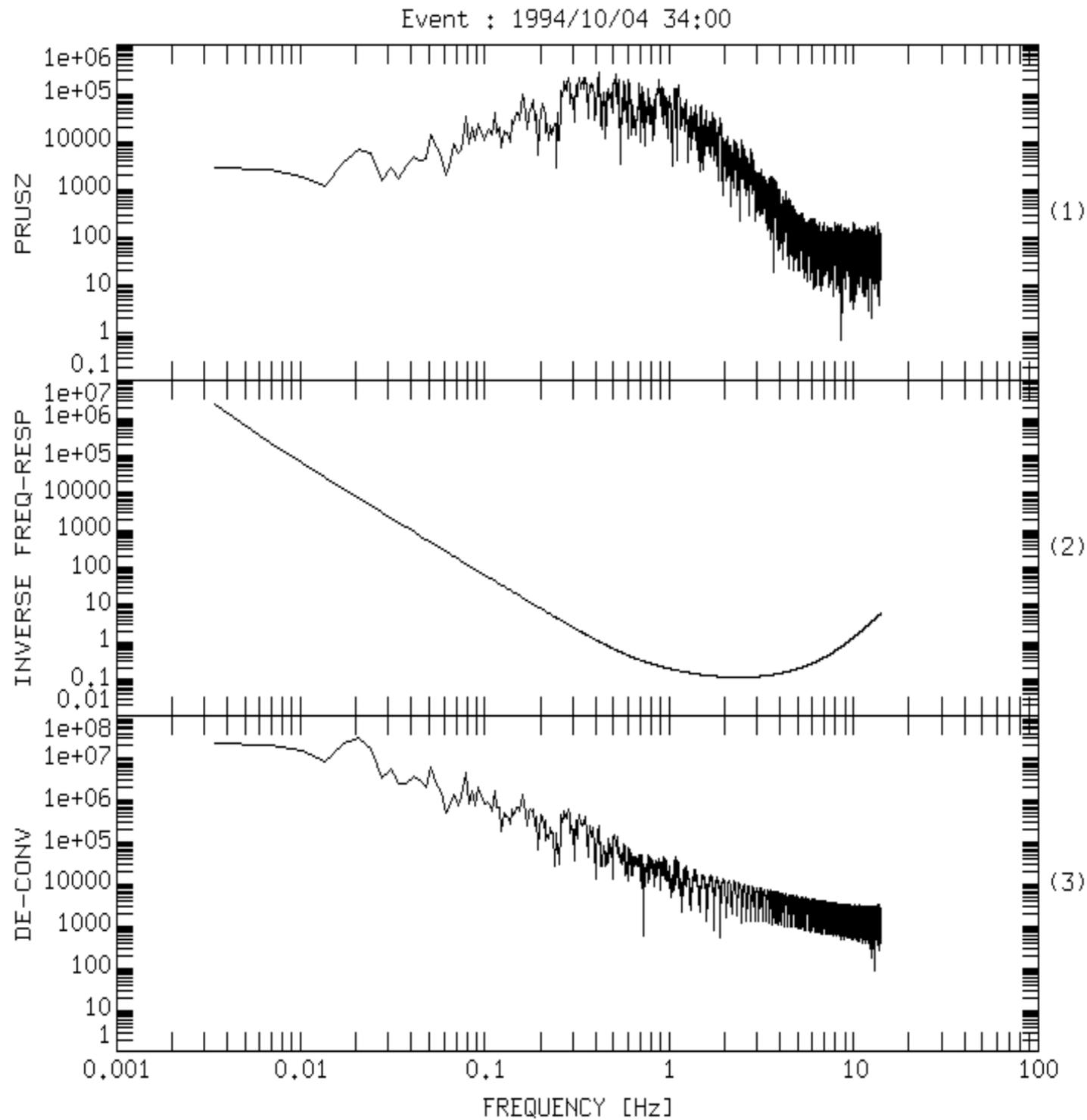
**Fig. 9.6** Vertical component record of an  $m_b = 7.5$  earthquake (1994 April 4) in the Kurile islands (upper panel). The units are counts with offset removed. The lower panel shows the corresponding amplitude spectrum. Notice the noise at both the low frequency and high frequency ends of the amplitude spectrum.

# Amplitude spectrum and displacement frequency response function of the recording system.



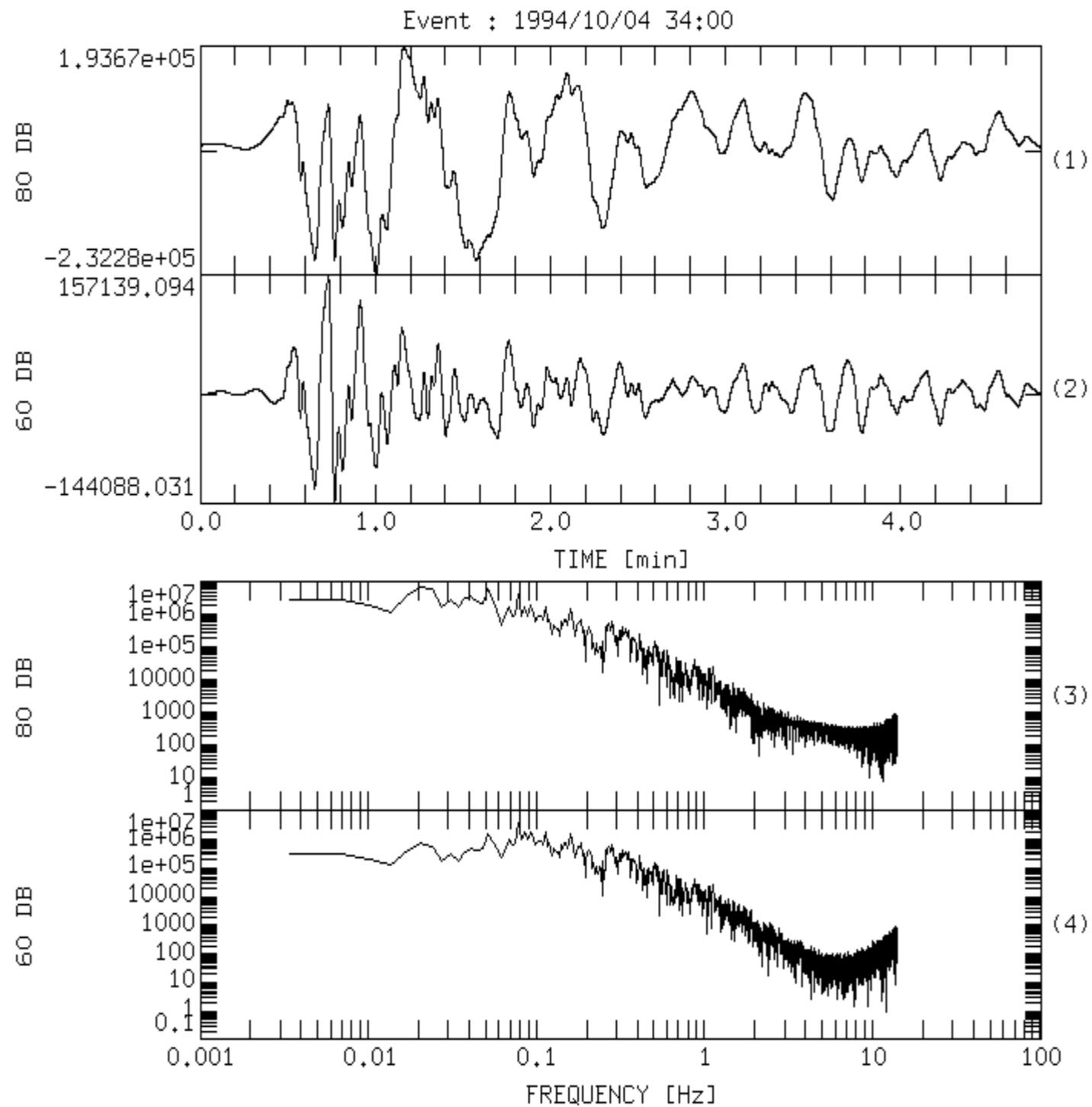
**Fig. 9.7** Amplitude spectrum from Fig. 9.6 compared to the modulus of the displacement frequency response function at station PRU (lower panel).

# Frequency domain results



**Fig. 9.9** Deconvolution illustrated in the frequency domain. From top to bottom, the amplitude spectrum of the observed trace, the frequency response function of the inverse filter, and the amplitude spectrum of the deconvolved trace are displayed.

# Waterlevel correction



**Fig. 9.10** Deconvolution by spectral division using a waterlevel stabilization of 80 dB (top trace) and 60 dB (second trace) of the signal shown in Fig. 9.6. The corresponding amplitude spectra are shown in the two bottom traces.

# Simulation = Deconvolution + Filtering

Be aware that in the digital world you have to change from s- to z-transform

$$Y_{sim}(z) = \frac{T_{syn}(z)}{T_{act}(z)} \cdot Y_{act}(z) = T_{sim}(z) \cdot Y_{act}(z)$$

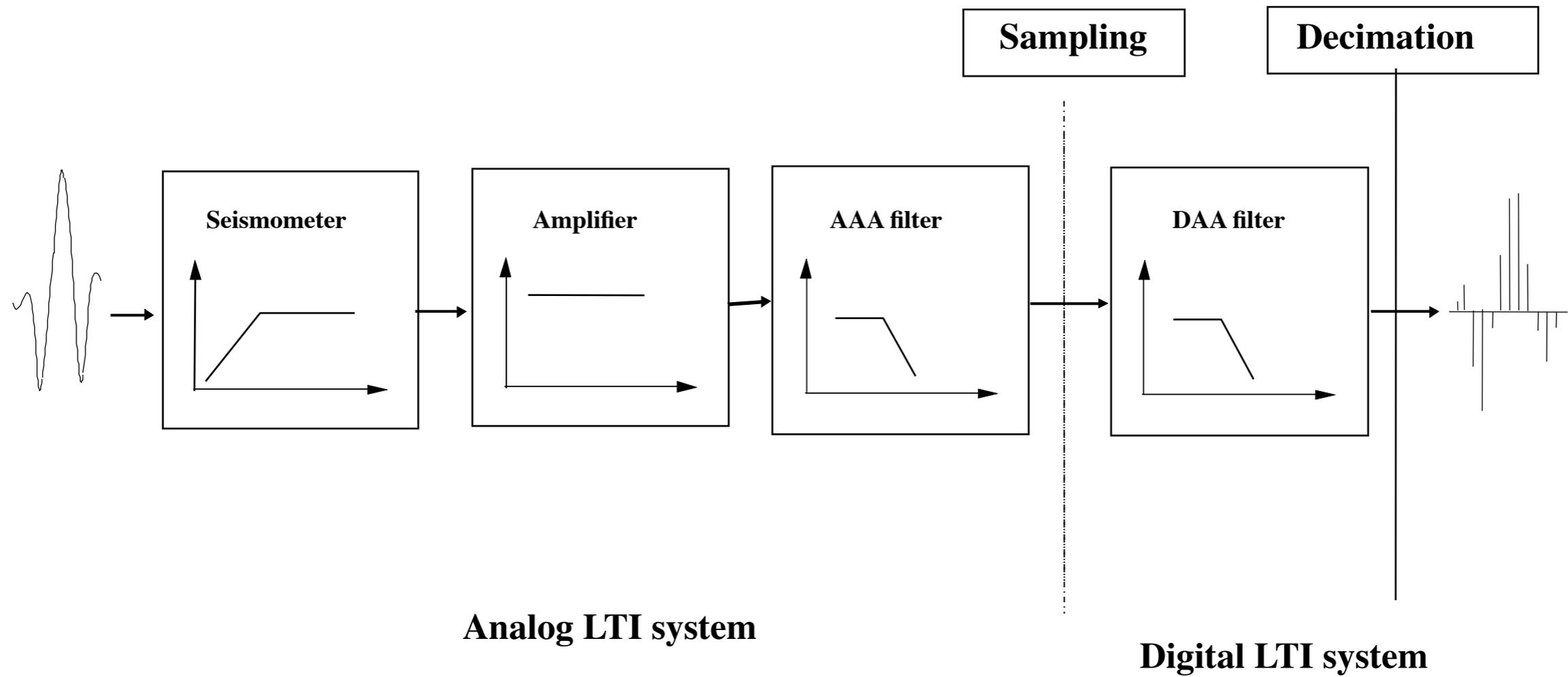
$T_{act}(z)$  = transfer function of actual recording system

$T_{syn}(z)$  = transfer function of the instrument to be synthesized

$Y_{act}(z)$  = z- transform of the recorded seismogram

$Y_{sim}(z)$  = z- transform of the simulated seismogram

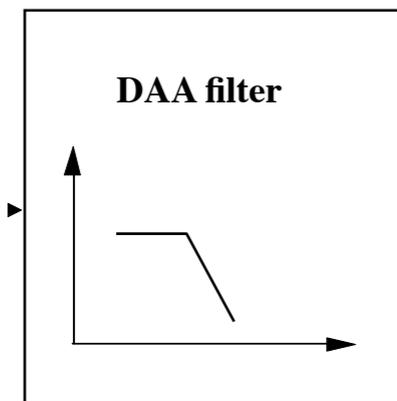
# FIR - Filter Effects



# **What is the reason for doing FIR filtering and decimating?**

Nearly all seismic recorders use the oversampling technique to increase the resolution of recordings. In order to achieve an optimum valid frequency band, the filters are very steep.

Besides its advantages this also bears new problems.



```

#          +          +-----+          +
#          +          | FIR response, RJOB ch EHZ |          +
#          +          +-----+          +
#
B061F03   Stage sequence number:          3
B061F05   Symmetry type:                  A
B061F06   Response in units lookup:       COUNTS - Digital Counts
B061F07   Response out units lookup:      COUNTS - Digital Counts
B061F08   Number of numerators:           96
#        Numerator coefficients:
#        i, coefficient
B061F09   0 3.767143E-09
B061F09   1 5.277283E-07
B061F09   2 2.184651E-06
B061F09   3 -5.639535E-06
B061F09   4 -1.233773E-06
B061F09   5 9.386712E-06
B061F09   6 4.859924E-06
B061F09   7 -1.644319E-05
...
#
#          +          +-----+          +
#          +          | Decimation, RJOB ch EHZ |          +
#          +          +-----+          +
#
B057F03   Stage sequence number:          4
B057F04   Input sample rate:              1.000000E+03
B057F05   Decimation factor:              5
B057F06   Decimation offset:              0
B057F07   Estimated delay (seconds):      1.490000E-01
B057F08   Correction applied (seconds):    0.000000E+00

```

# Linear Difference Equation

$$\sum_{k=0}^N a_k y[n-k] = \sum_{l=0}^M b_l x[n-l]$$

Infinite Impulse Response:  $a_k \neq 0$

Finite Impulse Response:  $a_0 = 1; a_{k \neq 0} = 0$

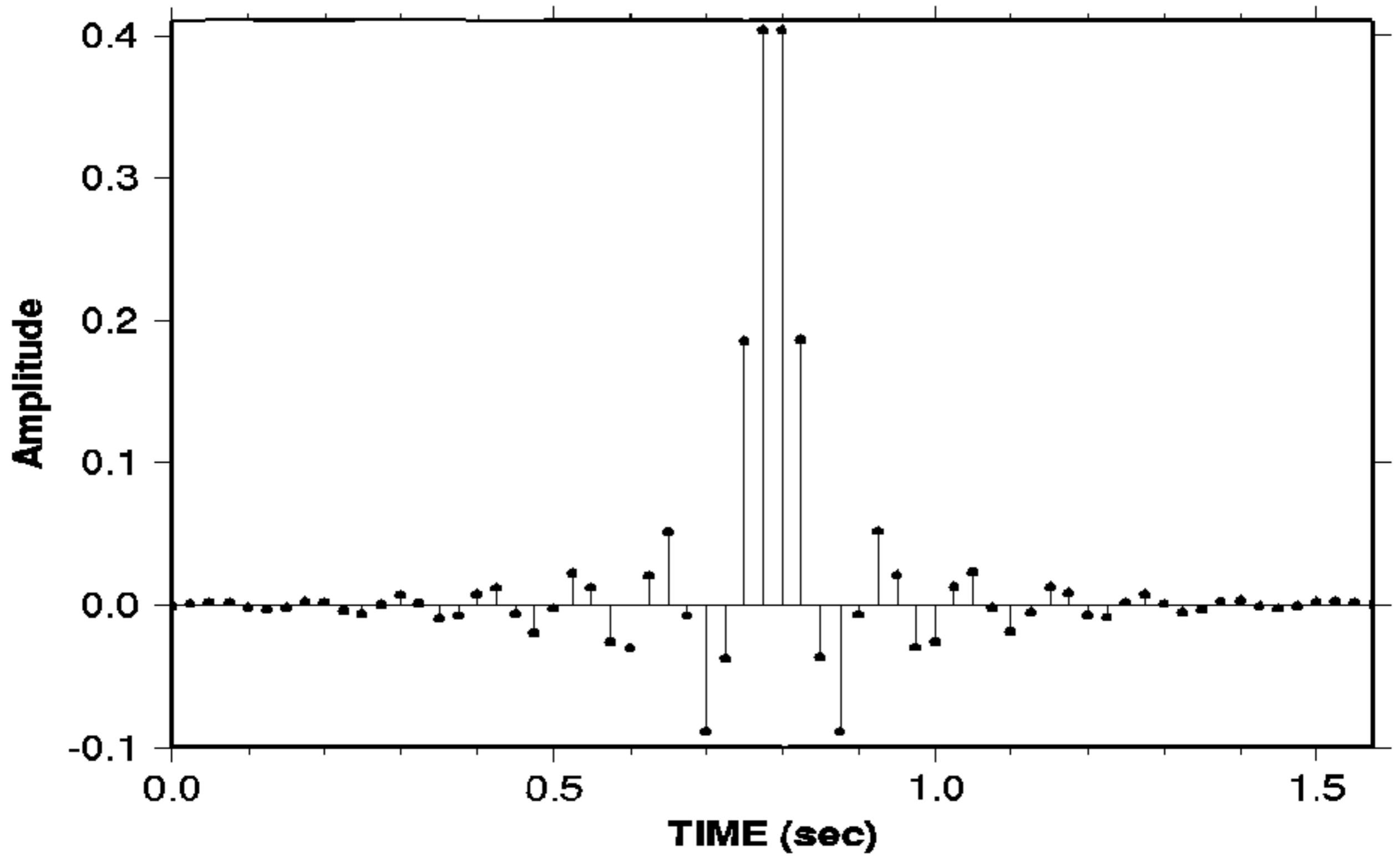
- FIR filters :

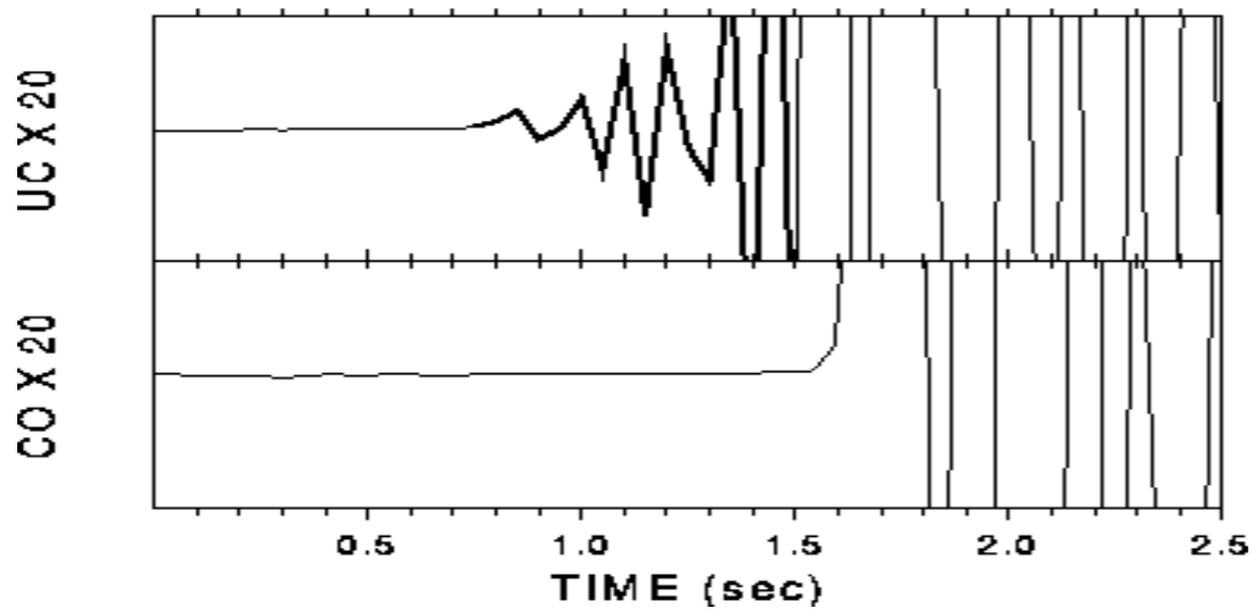
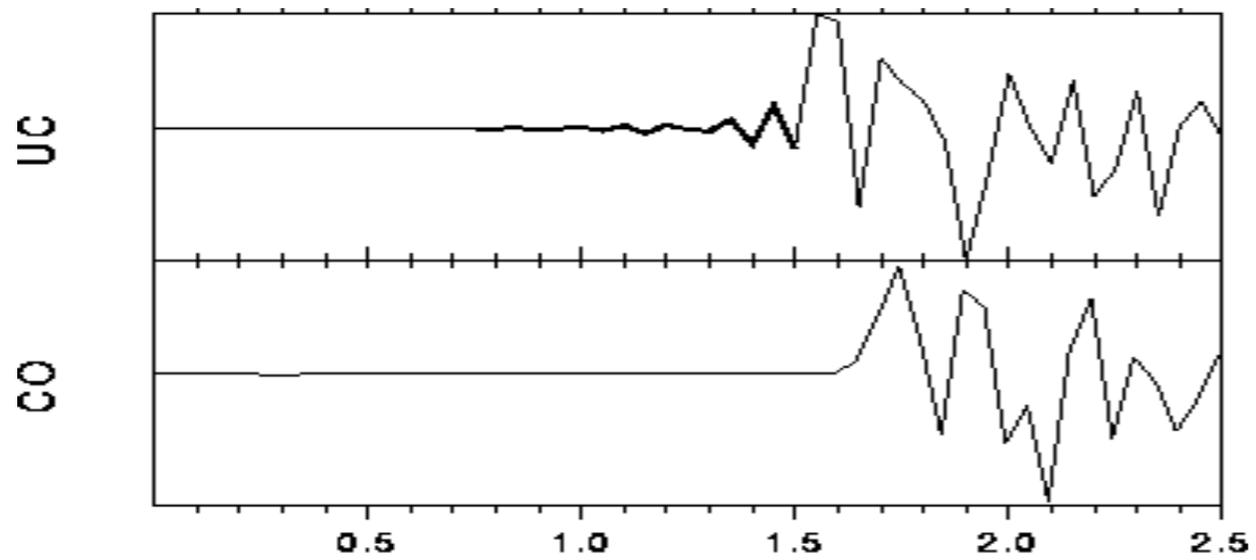
- + Always stable.
- Steep filters need many coefficients.
- + Both causal and noncausal filters can be implemented.
- + Filters with given specifications are easy to implement!

- IIR filters :

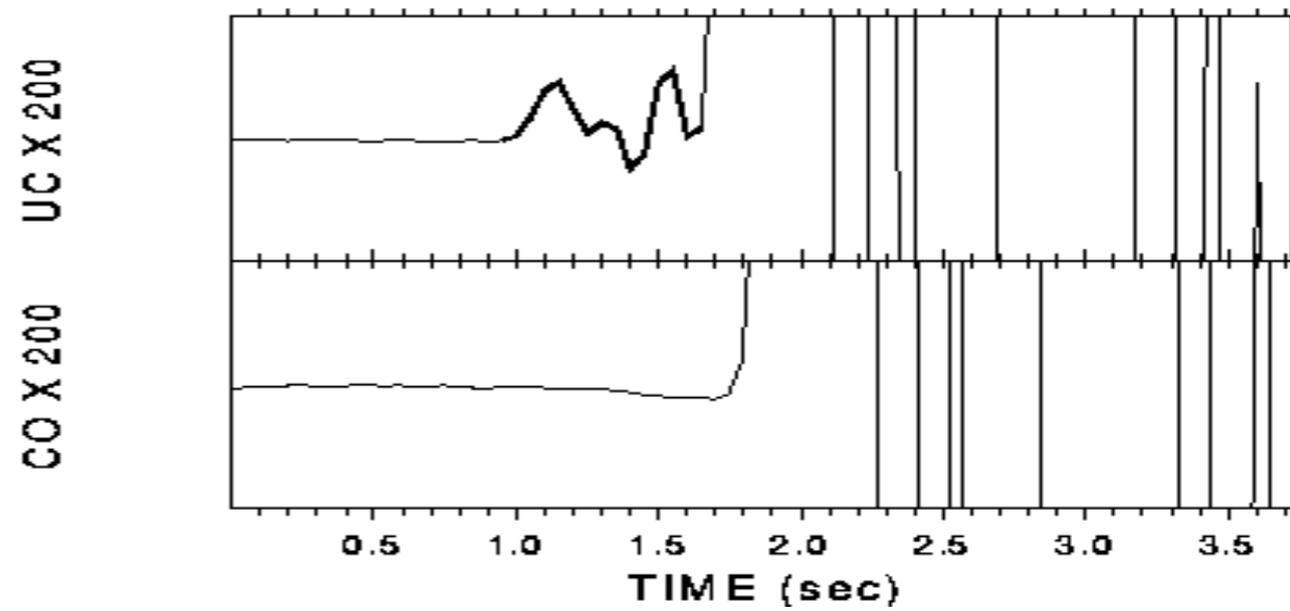
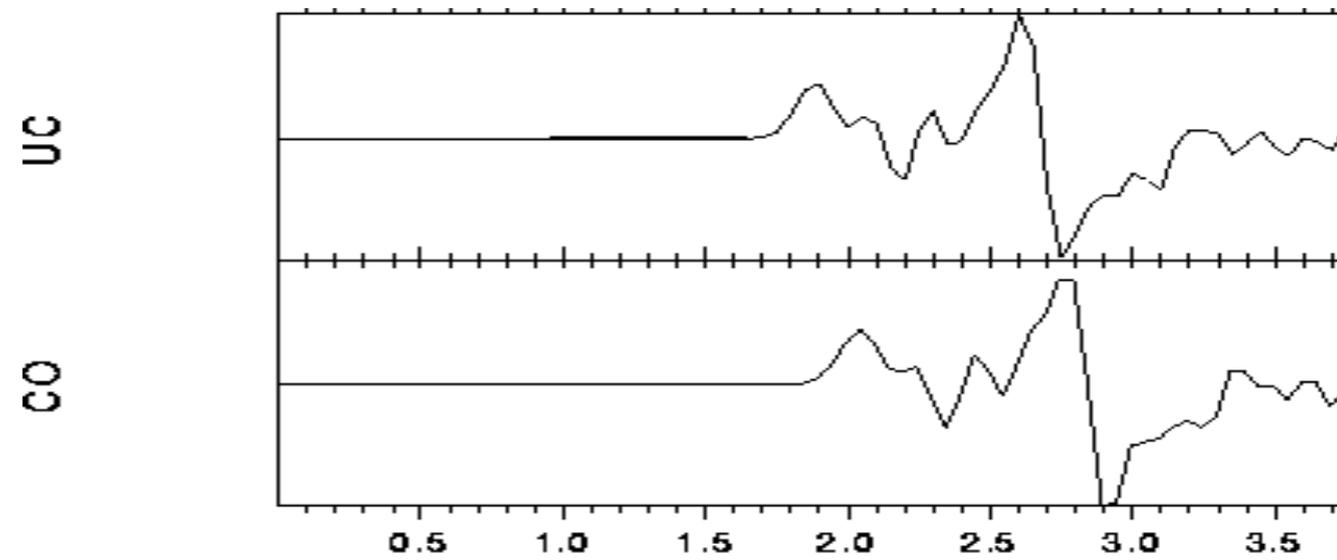
- Potentially unstable and subject to quantization errors.
- + Steep filters can easily be implemented with a few coefficients. Speed.
- Filters with given specifications are in general, difficult, if not impossible, to implement *exactly(!)*.

# QDP 380 Stage 4





a)



b)

# Routine Quality Control at DCs



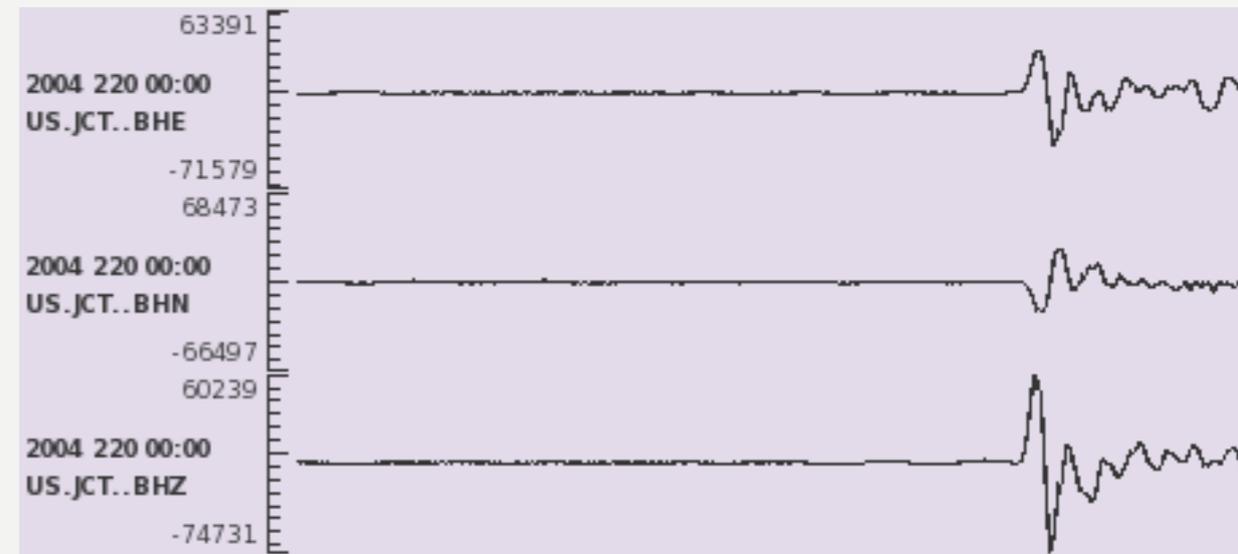
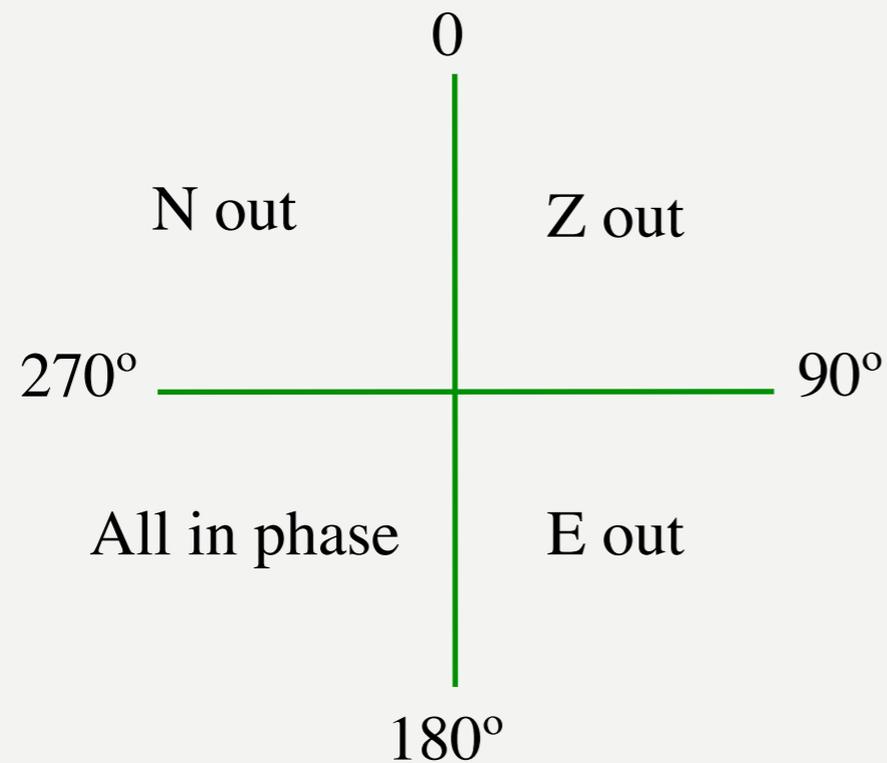
- The sooner problems are detected the sooner they can be fixed
- Sensor malfunctions, misconfigurations, aging
- Digitizer & recorder malfunctions
- Vault problems: tilting, settling, etc
- Cable & connection problems
- Telemetry issues
- Timing problems
- Many, many other potential issues

# Quick Checks: Polarization



The "quadrant method" allows an analyst to perform a rough check of 3-component sensor horizontal polarity.

Compare the P wave first motion of a relatively large event between the 3 components to determine back azimuth:



Aluetian Island event :: Texas, USA station (BA: ~317°)

\* Assumes Z component polarity is correct.

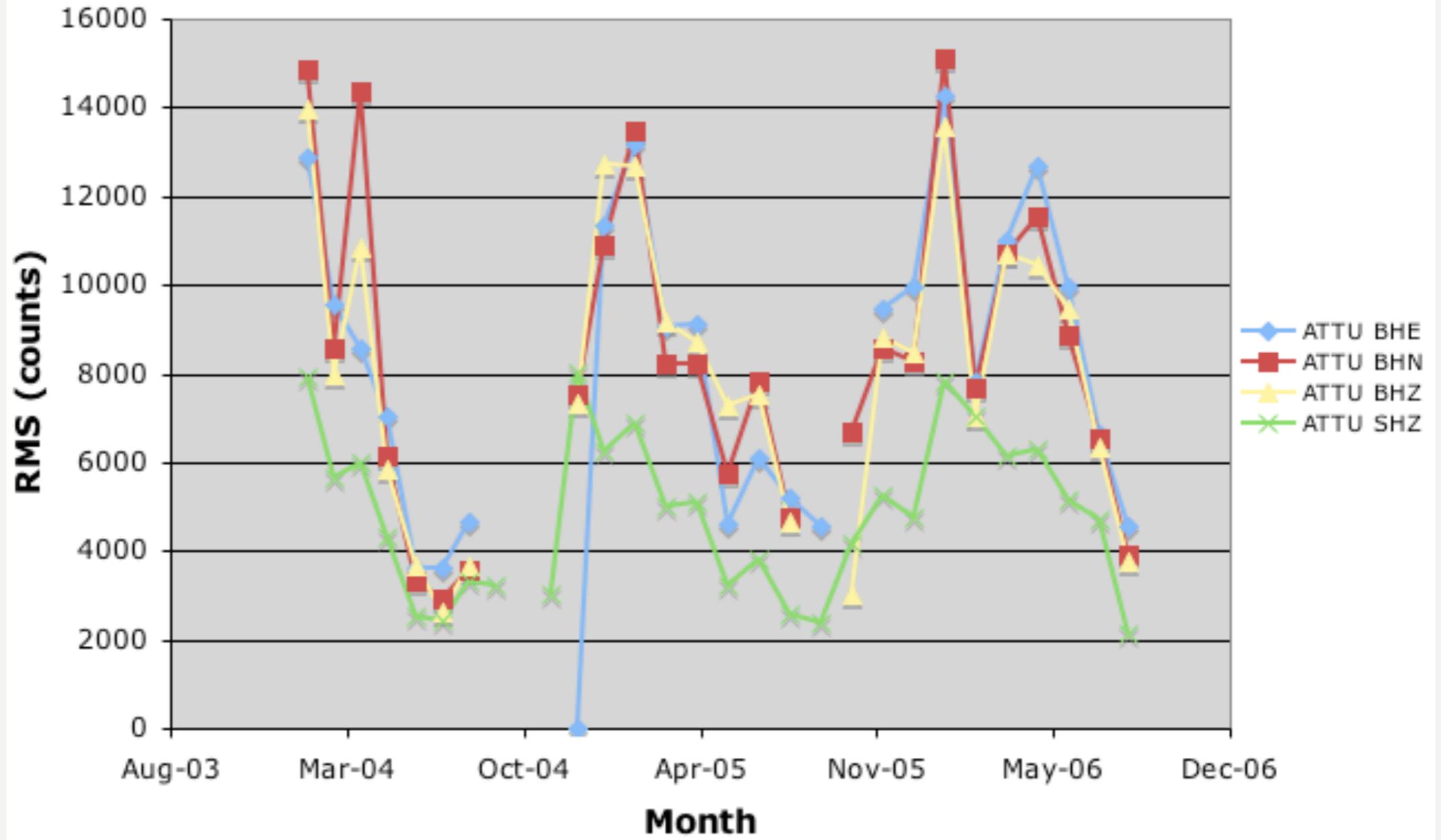


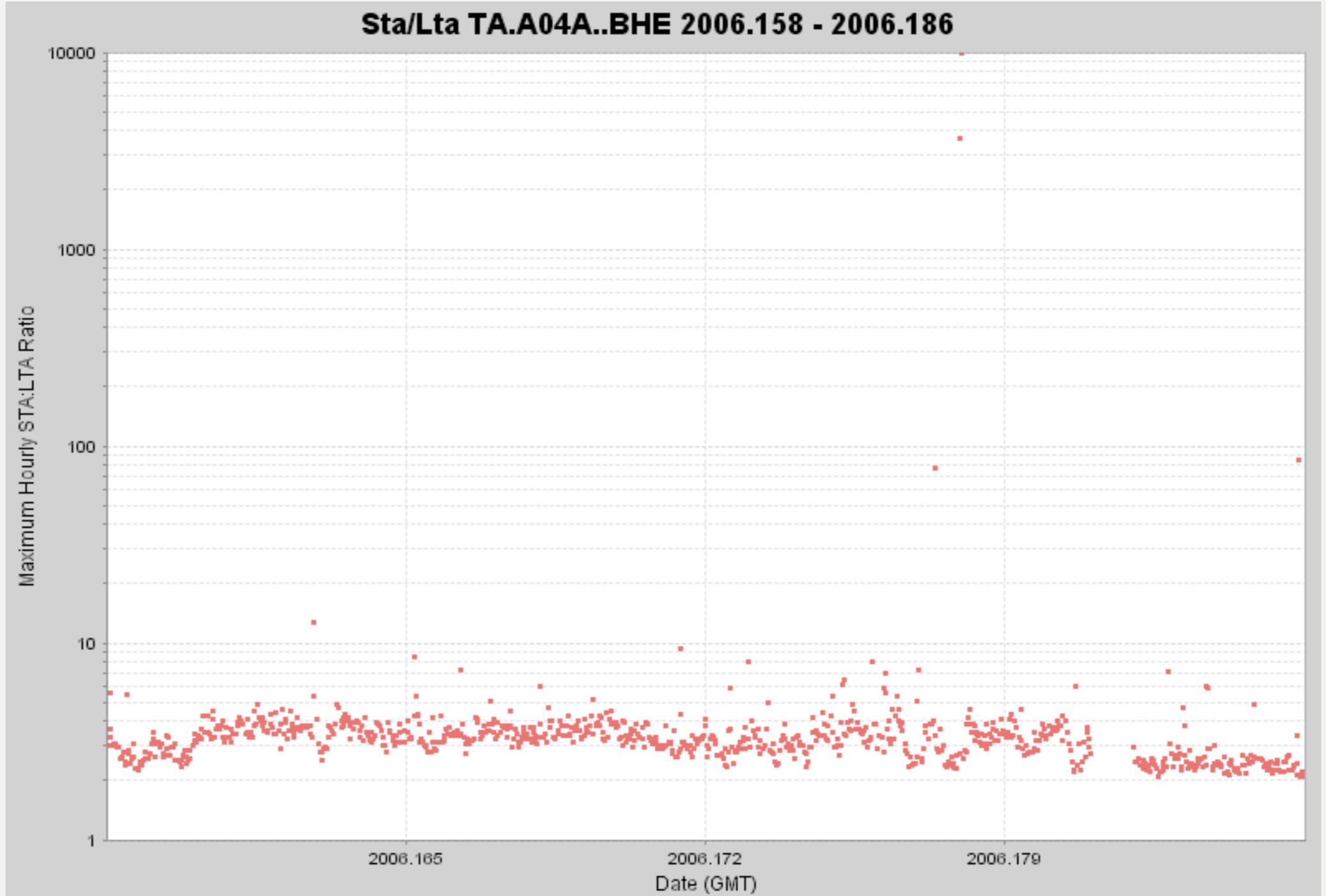
Automated QC measurements for incoming real-time data at the DMC:

- Tracks a number of simple parameters (signal RMS, mean, gaps, overlaps, etc.) in addition to more complicated analyses (PSD/PDF, STA/LTA)
- Generates daily reports, using thresholds to control what information is included in the report in order to reduce the number of issues that need attention

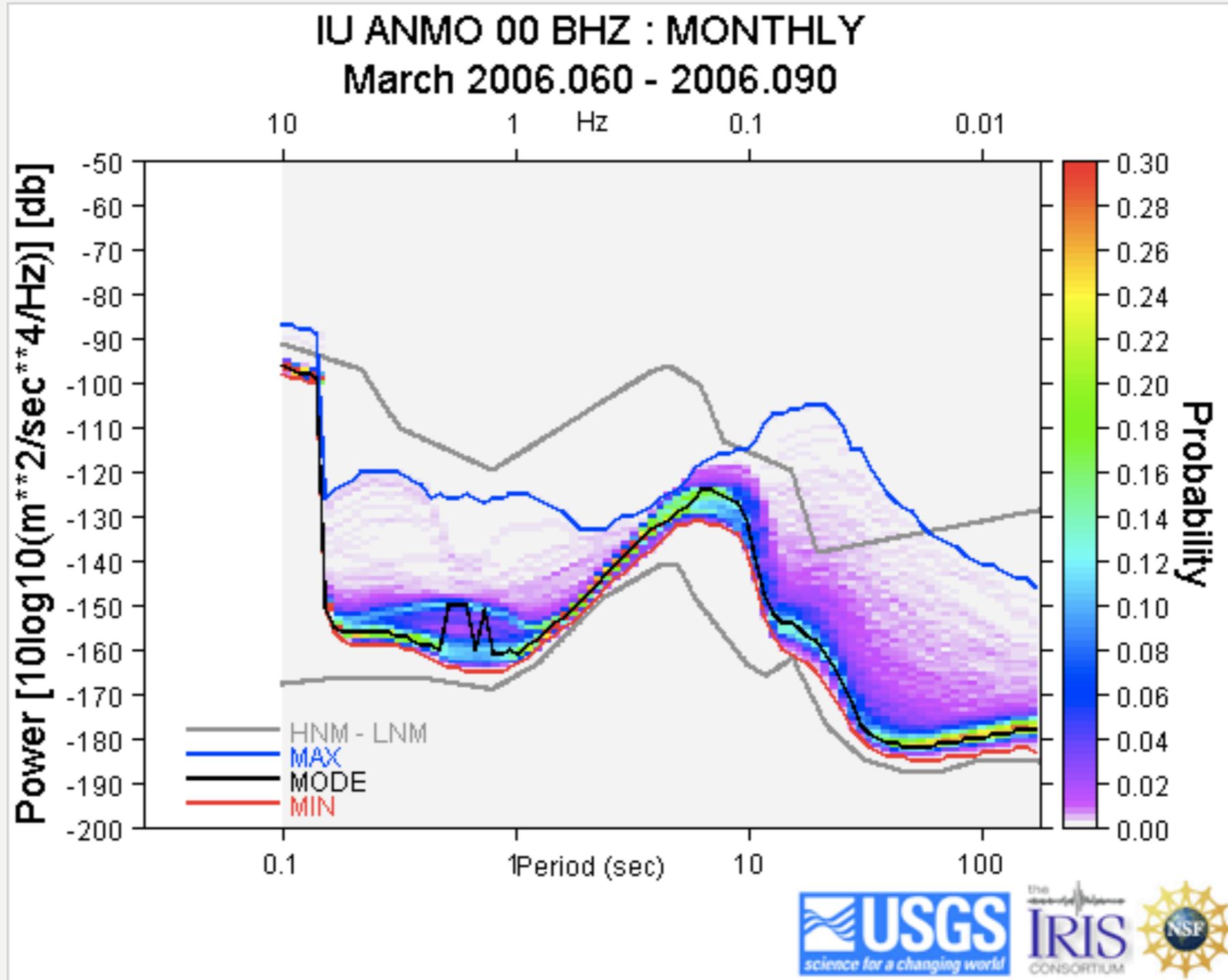
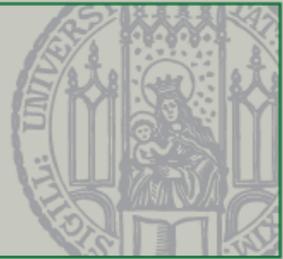


### ATTU Monthly RMS





# Prob. Density of Power Spectra





- problem if digitizer don't report (GPS) timing problems
  - miniSEED has only restricted possibilities for reporting timing problems
- ➔ Way out by stacked cross correlation of noise between distant stations (by-product of cross correlating diffusive wave field)

# Two Stations CrossCorrelation

