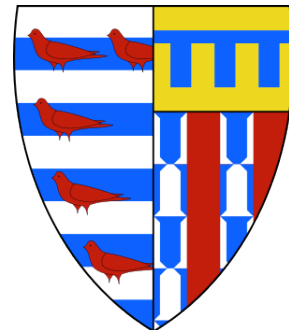


Observability of lower mantle structures in Earth's free oscillation data

Paula Koelemeijer¹

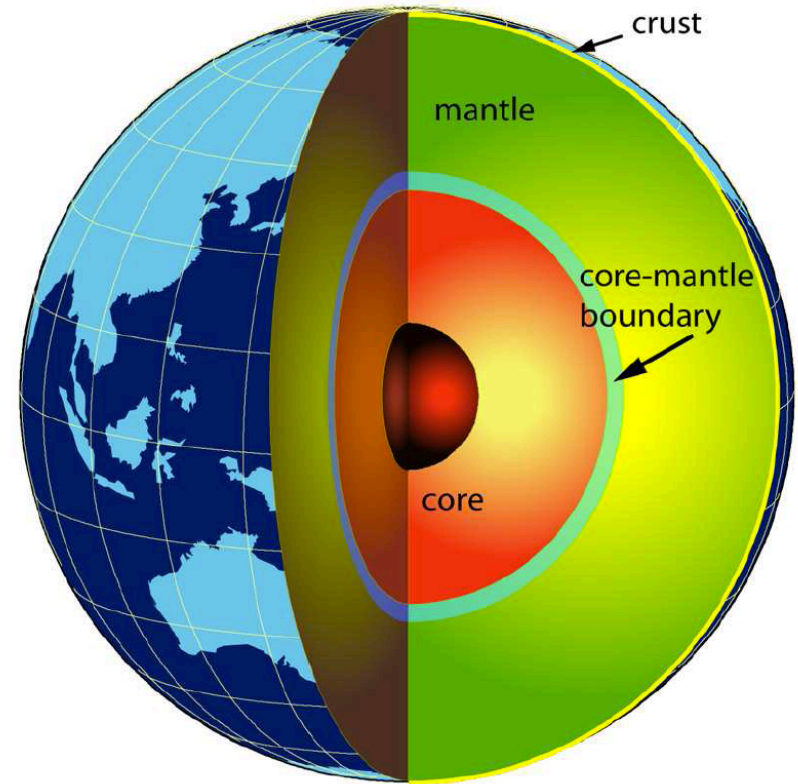
Arwen Deuss¹, Jeannot Trampert²

¹ University of Cambridge, ² Utrecht University



The D'' region

- Largest compositional and thermal interface
- Thermal boundary layer
- Origin of mantle plumes and slab graveyard?
- Constraints on boundary conditions for convection
- Evolution of the core and inner core growth



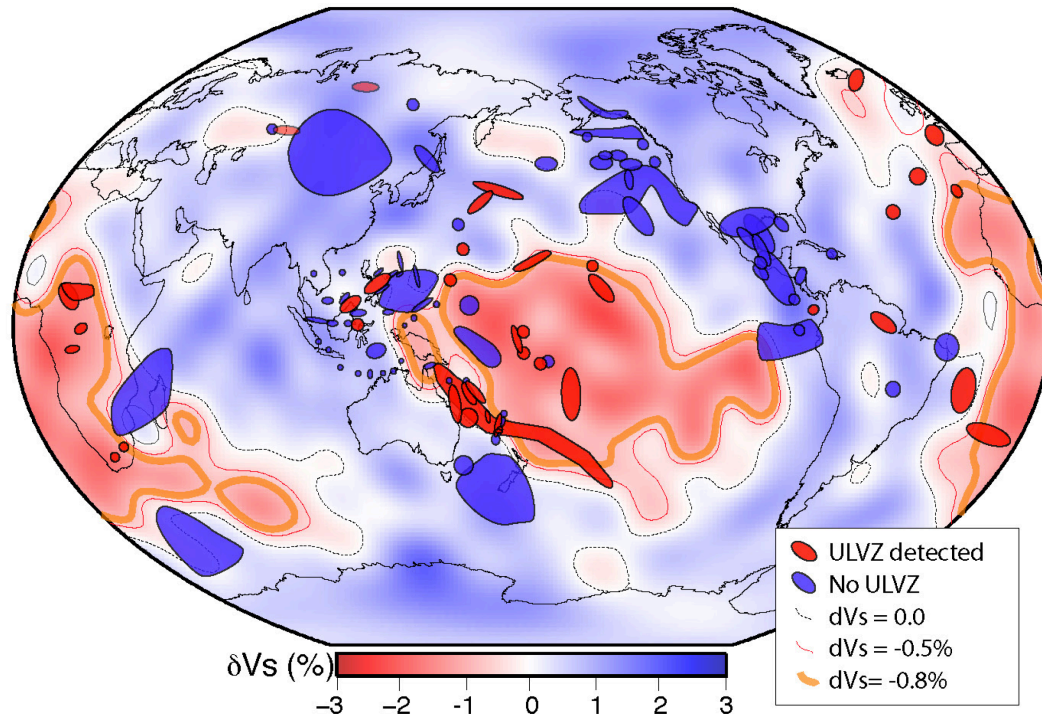
Ed Garnero, <http://garnero.asu.edu>

LLSVPs

- $\ln V_s$ reductions of $\sim 3\%$
- Large scale degree 2 structure visible in tomography
- Possible chemical origin?

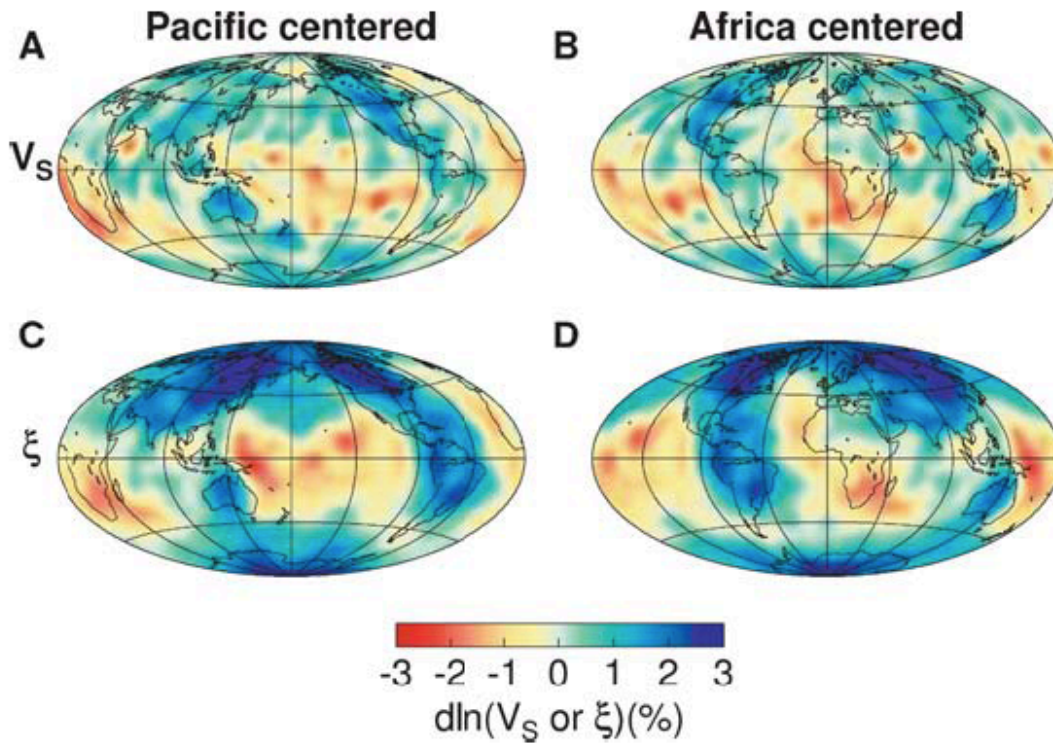
ULVZs

- Extreme reductions up to 30%
- Small scale structures observed with body waves
- Possible relation with LLSVPs
- Partial melt and/or chemical origin?
- Observable by modes?



D'' anisotropy

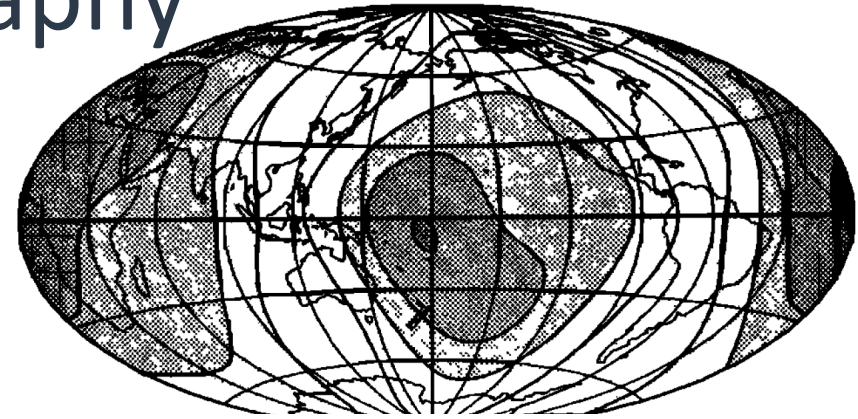
2800 km



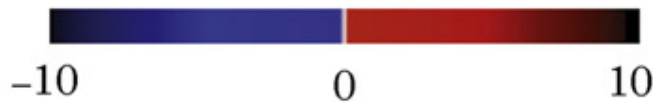
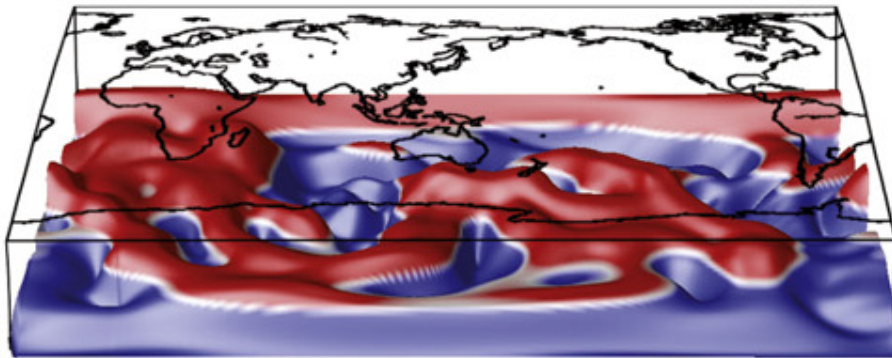
- Radial anisotropy required to match normal mode data
- Lateral varying anisotropy from S-wave splitting
- Explained by
 - deformation induced aligned crystals
 - flow aligned melt inclusions
 - pPv phase

Dynamic CMB topography

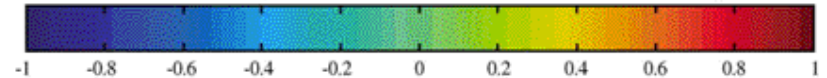
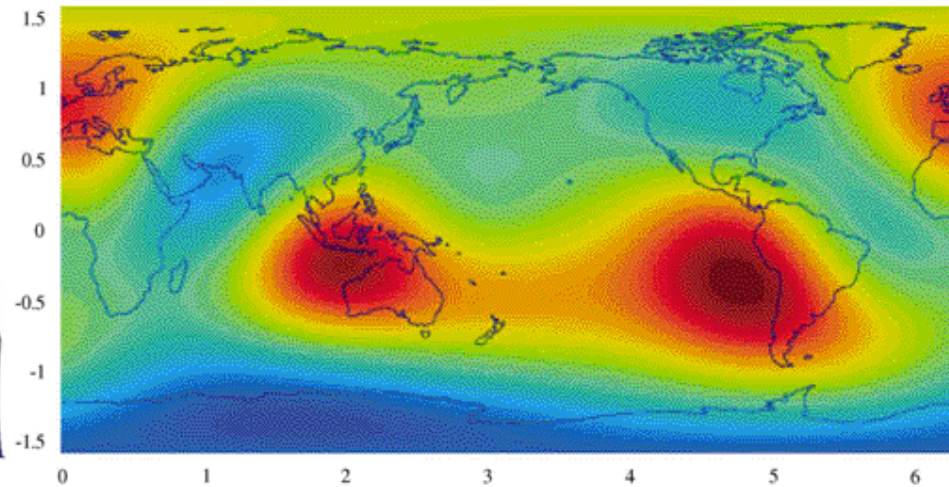
- Topography induced by convection
- Long wavelength < 10 km
short wavelength < 300 m
- Models from variety of disciplines differ in pattern and amplitude



Li et al., 1991, JGR



Lassak et al., EPSL, 2010



Sze & Van Der Hilst, 2003, PEPI

Normal mode splitting functions

- Standing waves with discrete frequencies, denoted as ${}_n S_l$
- 2/+1 singlets for a degenerate Earth – split by rotation, ellipticity and heterogeneous structure
- Describe splitting of normal modes by c_{st} :

$$c_{st} = \int_0^a \delta m_{st}(r) K_s(r) + \sum_d \delta h_{st}^d H_s^d$$

- Linearly related to Earth's structure by sensitivity kernels
- Splitting function map (similar to phase velocity map)

$$c(\theta, \phi) = \sum_{s=0}^{2l} \sum_{t=-s}^s c_{st} Y_s^t(\theta, \phi)$$

Observability

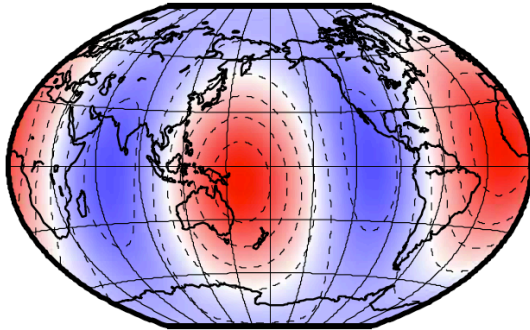
- General trends in data are well reproduced by global mantle models
- Hence, only consider splitting due to extra structure
- Calculate observability using predictions and data uncertainty:

$$O_s = \frac{1}{2s+1} \sum_{t=-s}^s \frac{|C_{st}^A - C_{st}^B|}{\sigma_{st}^{data}}$$

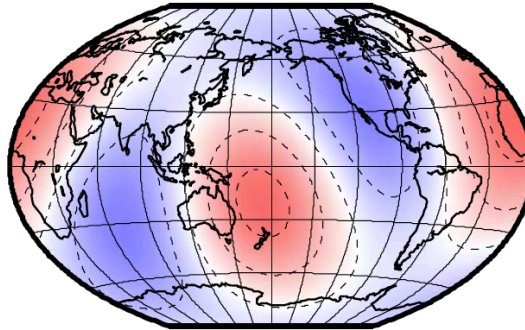
- Values larger than 1 are significant
- For selection of modes with large sensitivity to D''

CMB topography input

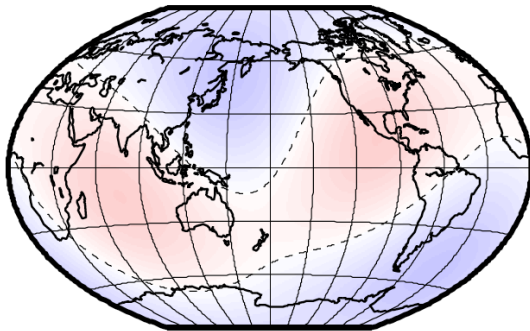
(a) LGW1991SAT



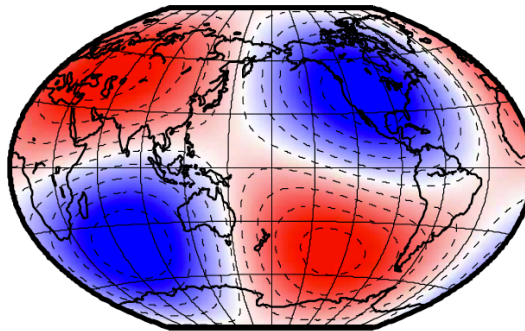
(b) LMGZ2010PC1



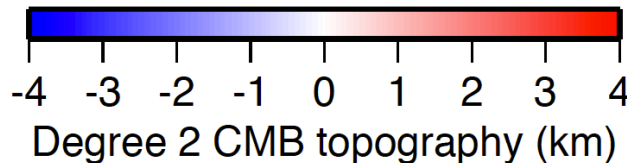
(c) SV2003



(d) MD1987



- Models taken from different disciplines
- Peak-to-peak amplitude is also varied



a) *Li et al., JGR, 1991*

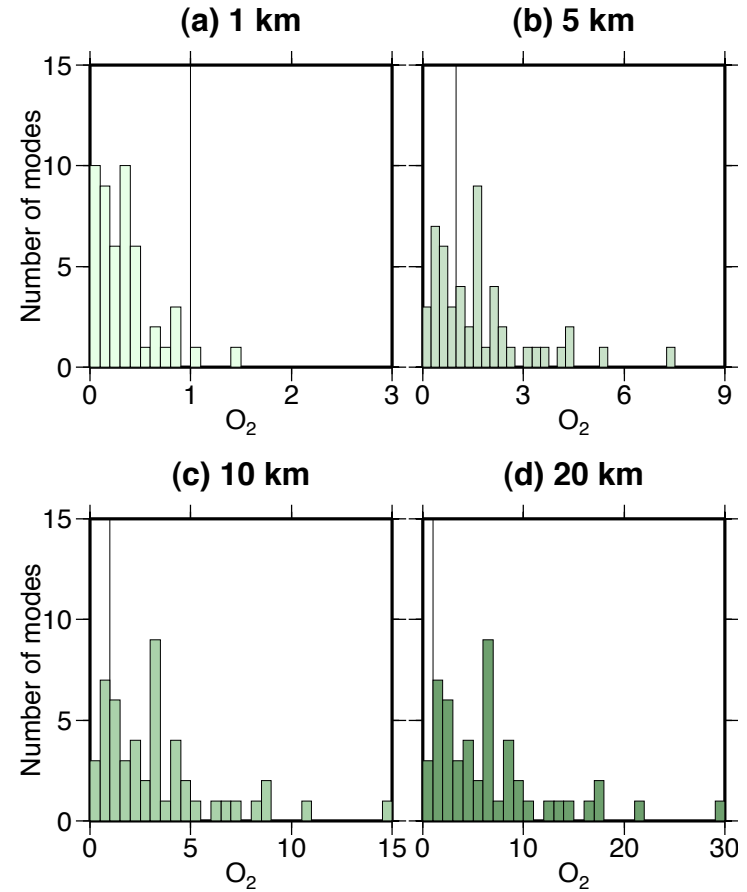
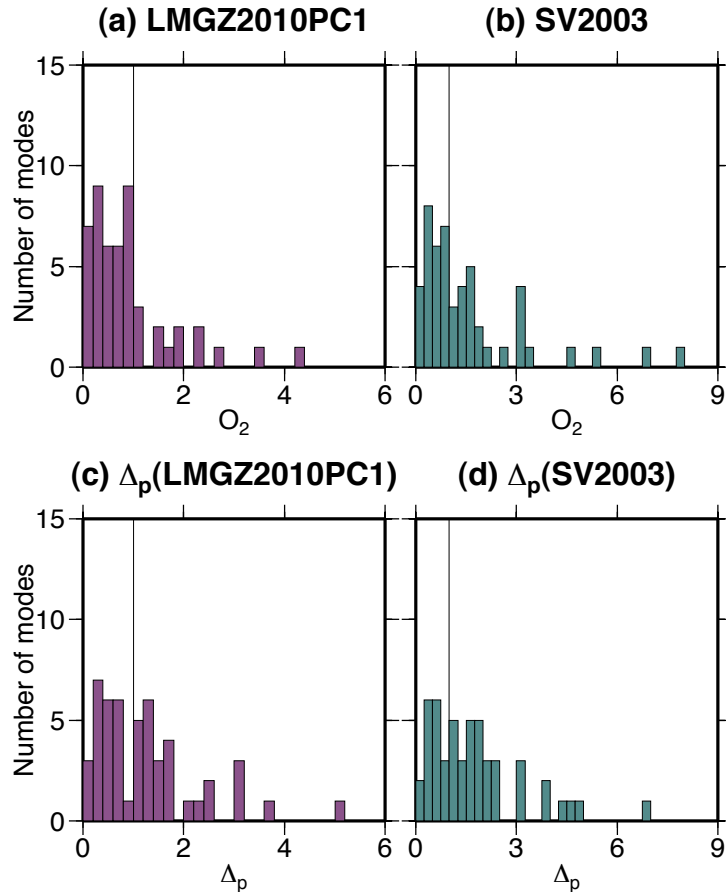
b) *Lassak et al., EPSL, 2010*

c) *Sze & Van Der Hilst, PEPI, 2003*

d) *Morelli & Dziewonski, Nature, 1987*

Pattern

Amplitude

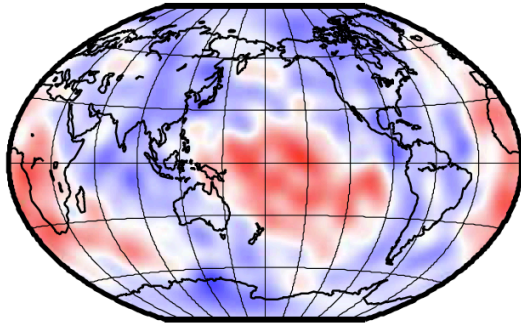


Koelemeijer et al., GJI, 2012

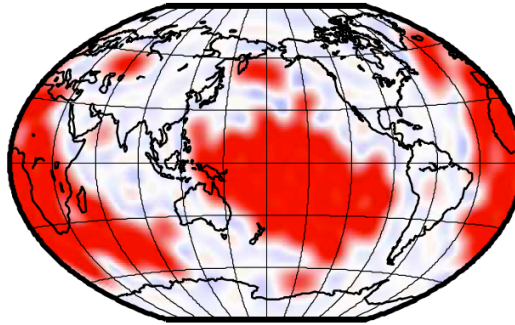
- Observability of patterns in the limit of the data
- Topography smaller than 5 km is not observable

ULVZ input

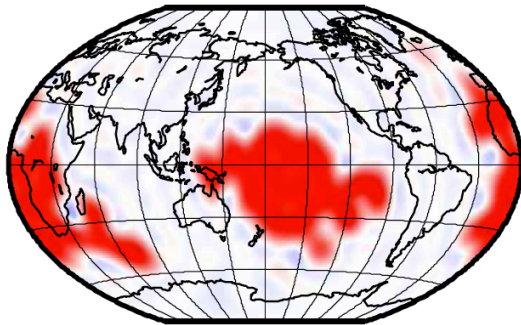
(a) S20RTS (x10)



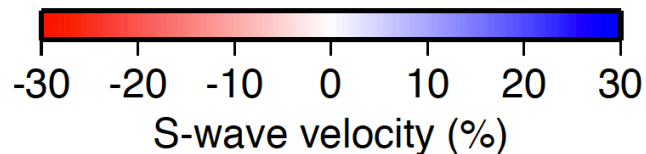
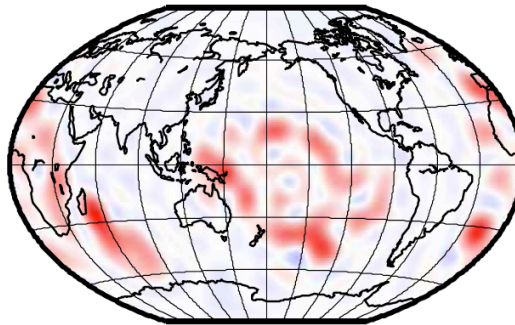
(b) Global ULVZ



(c) Regional ULVZ

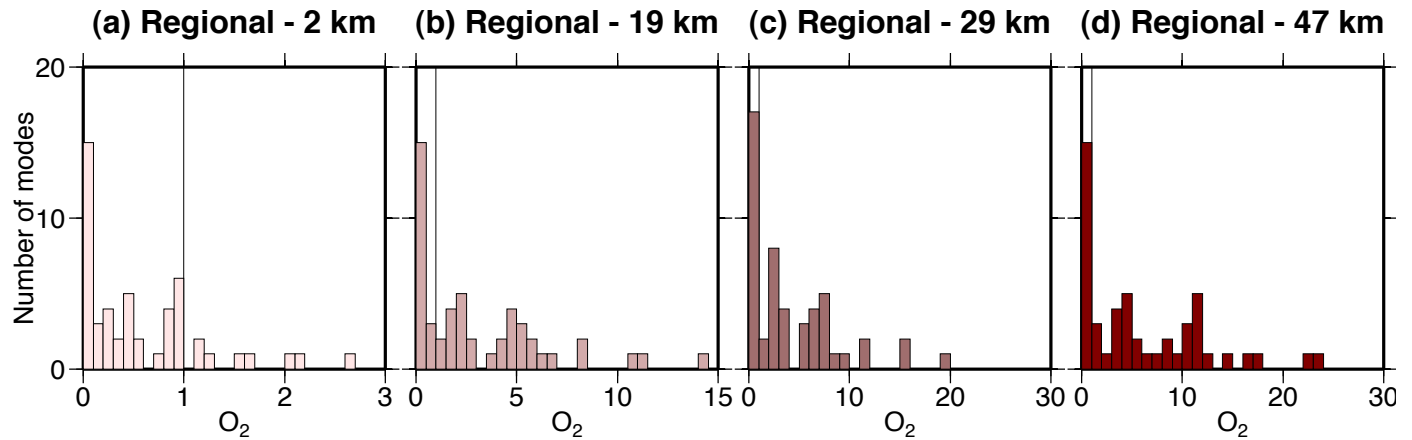


(d) Banded ULVZ

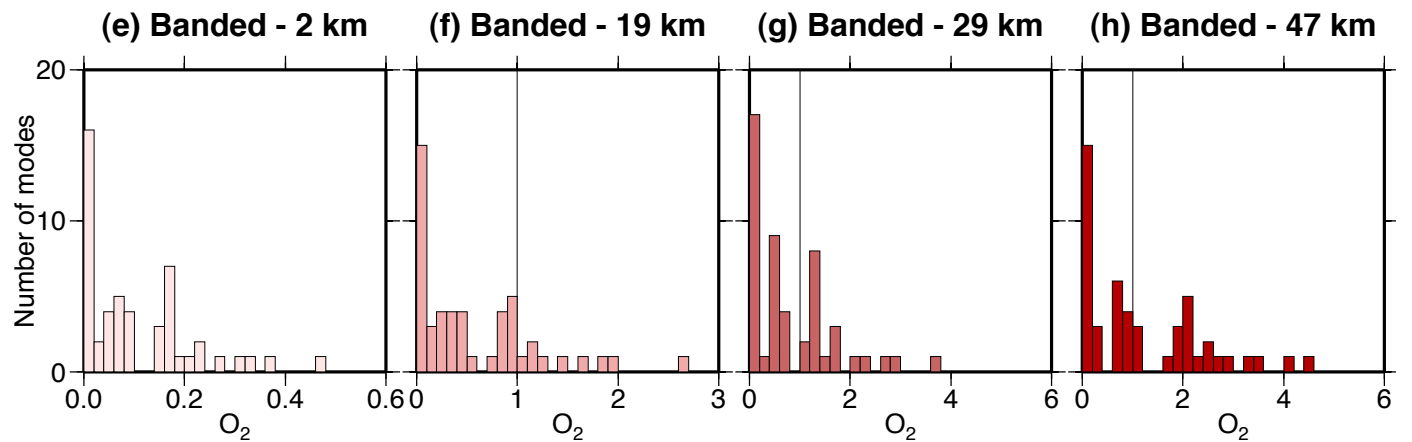


- Use variations in S20RTS for parameterization
- Banded ULVZs synthesized are consistent with the edges of LLSVPs

Regional



Banded

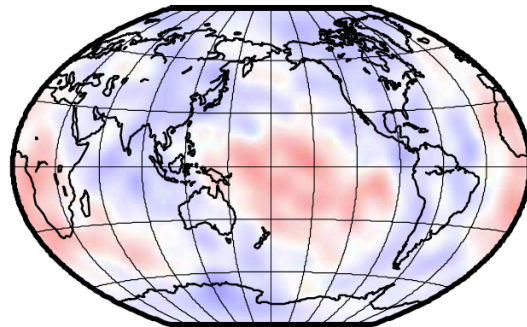


- Regional ULVZs larger than 19 km are observable
- For banded ULVZs the thickness needs to be larger than 29 km

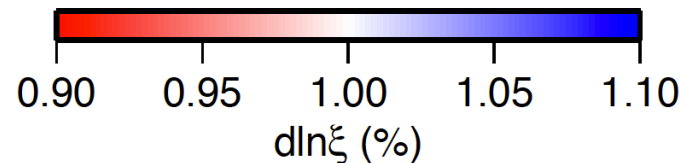
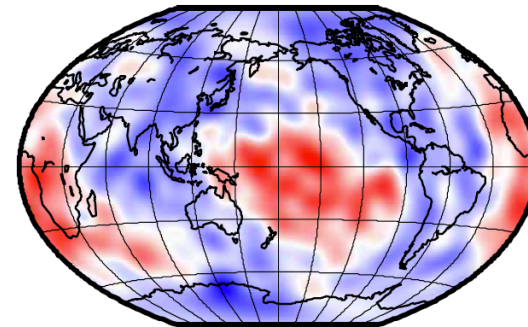
Anisotropy input

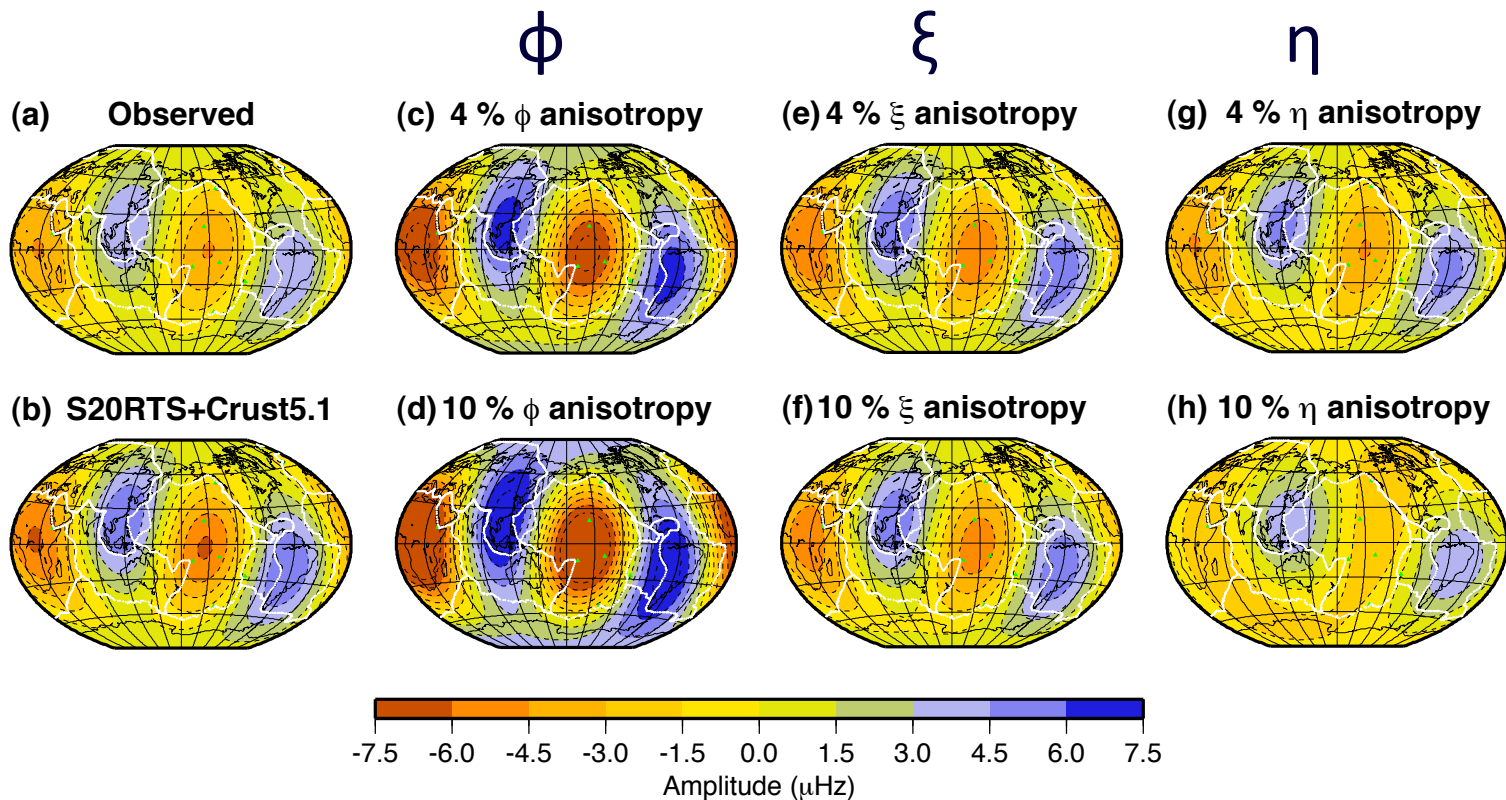
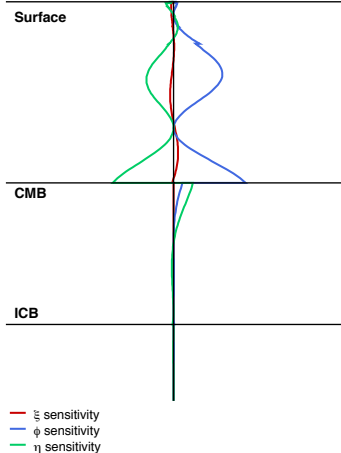
- Relate to S20RTS variations
- Parameterize in Love parameters $\phi=C/A$, $\xi=N/L$ and η
- $0.9 < \phi, \xi, \eta < 1.1$ for ξ : > 1 parallel to CMB
 < 1 perpendicular to CMB

(a) 4 % anisotropy



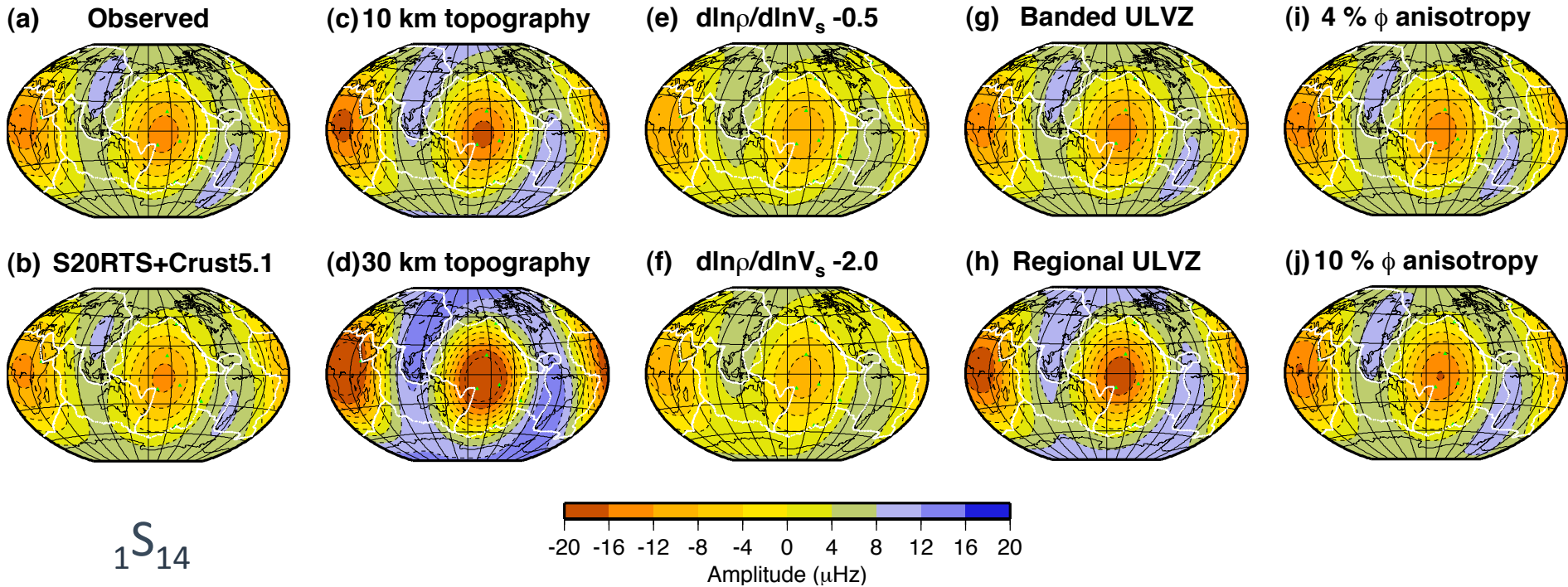
(b) 10 % anisotropy



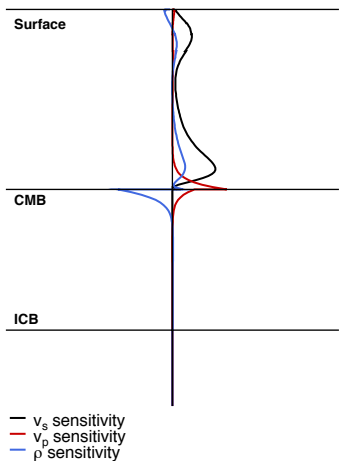
$4S_4$ 

- Small variations due to ξ except for fundamentals
- Modes mainly sensitive to ϕ and η
- However, large trade-offs exist between the two

Trade-offs between structures



$1S_{14}$



- CMB topography and ULVZs large effect
- $d\ln\rho/d\ln V_s$ scaling effect cannot even out large topography
- Observability anisotropy dependent on mode

Higher degree observability

	Topography		ULVZs		Scaling	Anisotropy		
	T_p	T_a	U_r	U_b	S	A_ϕ	A_ξ	A_η
O_2	X	X	X	X	X	X	X	X
O_4	X	X	X	X	X	X	-	X
O_6	X	X	X	-	X	X	-	X
O_8	-	-	-	-	-	-	-	-

Koelemeijer et al., GJI, 2012

- Most structures observable up to degree 6
- Banded ULVZs only up to degree 4 and S-wave anisotropy only up to degree 2
- However, observability dependent on available data

Conclusions

Normal modes are sensitive to small scale D'' structures

- CMB topography smaller than 5 km cannot be resolved
- Effect of different patterns close to limit of the data
- To be visible, regional ULVZs should be thicker than 19 km and banded ULVZs thicker than 29 km
- S-wave anisotropy is difficult to resolve, P-wave and anisotropy in η easier, but show a strong trade-off
- Trade-offs between all structures depend on the mode
- Observability generally large enough up to degree 6



Thank you for you attention