

Constraining attenuation from ambient seismic noise

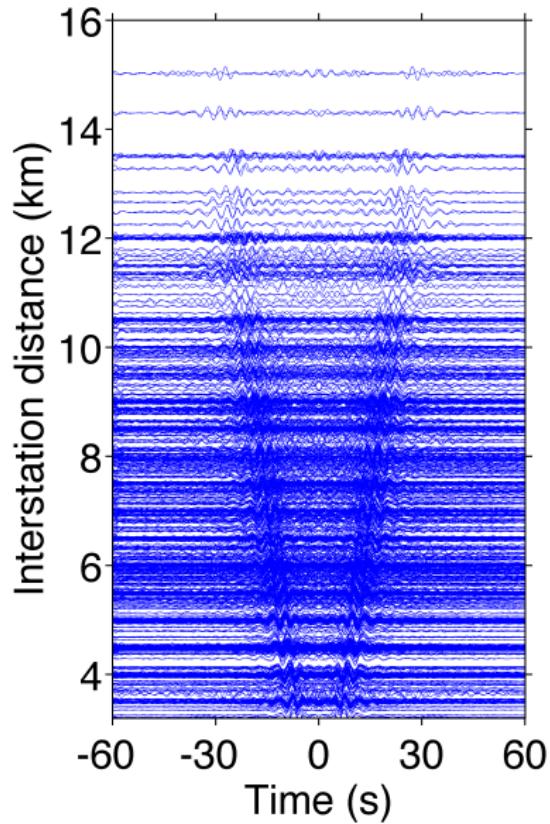
Kees Weemstra, Lapo Boschi, Roel Snieder, Alex Goertz and Brad Artman



QUEST meeting
22-05-2012



The challenge: attenuation



Cross-correlation

Normalized cross-correlation:

$$C_{x_1 x_2}(\omega) \equiv \frac{U(\mathbf{x}_1, \omega) U^*(\mathbf{x}_2, \omega)}{|U(\mathbf{x}_1, \omega)| |U(\mathbf{x}_2, \omega)|}$$

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Averaged complex coherency:

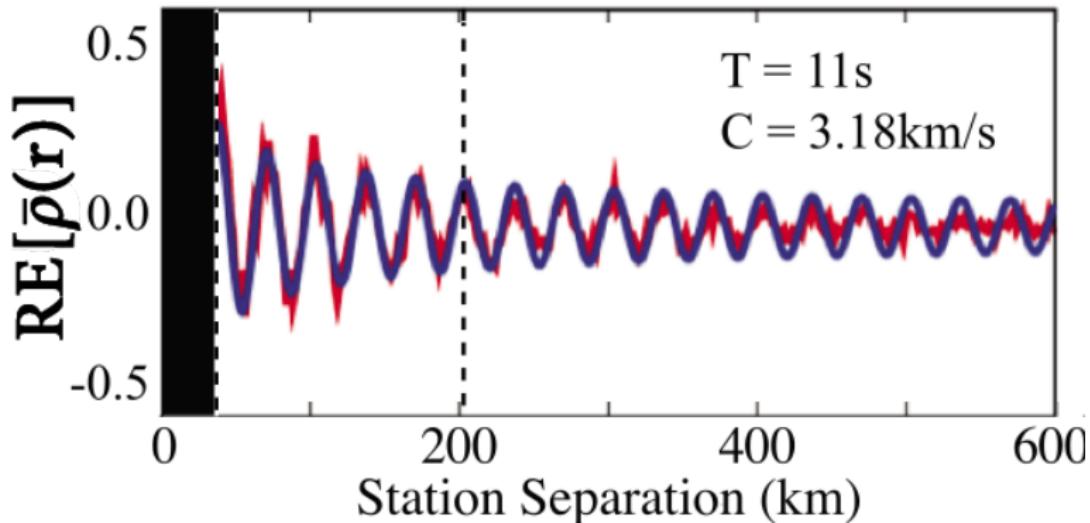
$$\bar{\rho}(\omega, r = |\mathbf{x}_2 - \mathbf{x}_1|) \equiv \sum_{azimuth} \sum_{time} C_{x_1 x_2}(\omega)$$

Bessel function fit

$$\Re[\bar{\rho}(\omega, r)] = J_0 \left(\frac{\omega r}{c(\omega)} \right)$$

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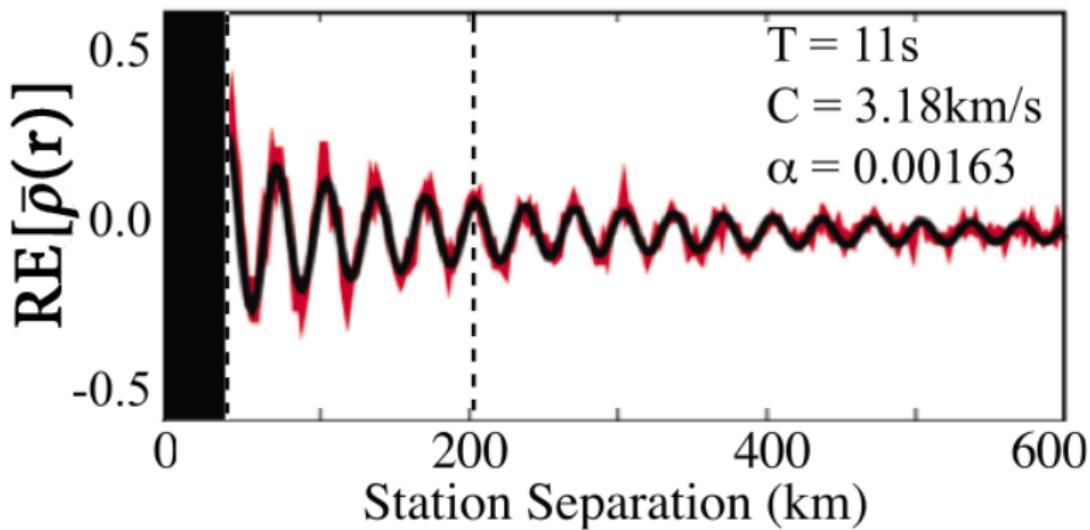
Lawrence and Prieto (2011), Journal of Geophysical Research

Damped Bessel function fit

$$\Re[\bar{\rho}(\omega, r)] = J_0\left(\frac{\omega r}{c(\omega)}\right) e^{-\alpha(\omega)r}$$

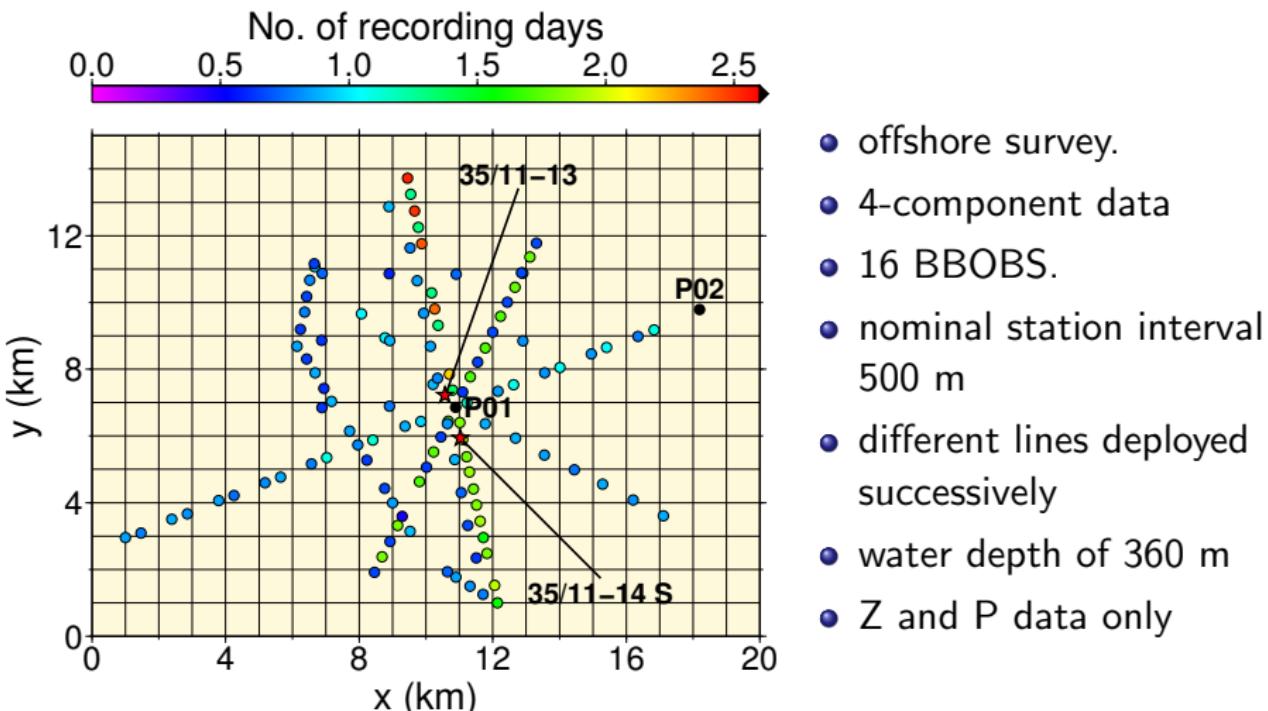
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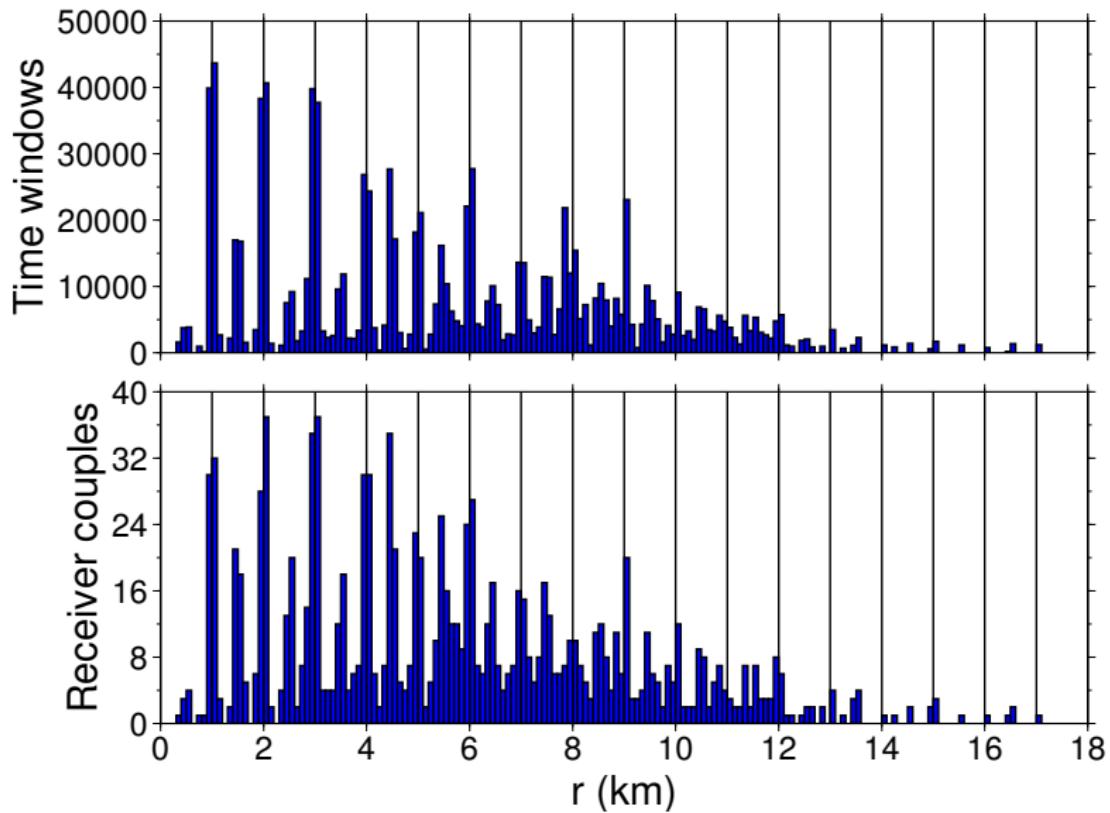


Lawrence and Prieto (2011), Journal of Geophysical Research

Offshore data set

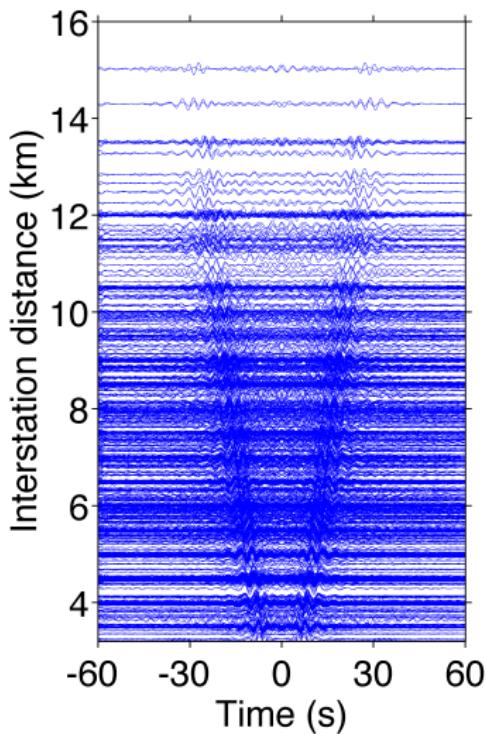


Sampling with offset



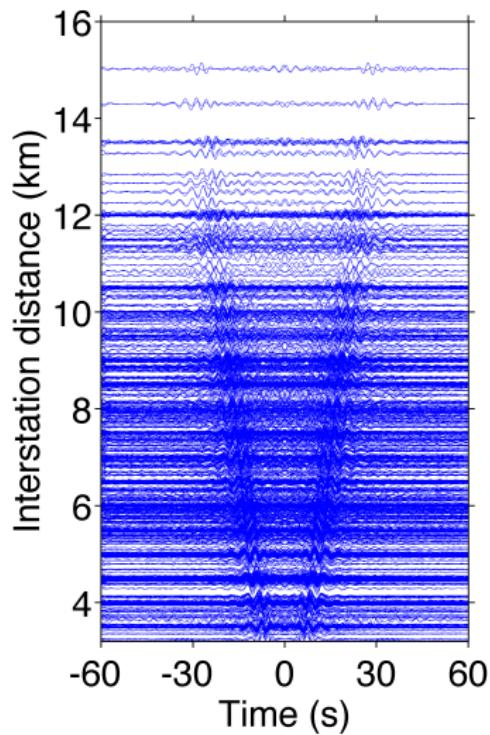
Green's function gathers

Z-component

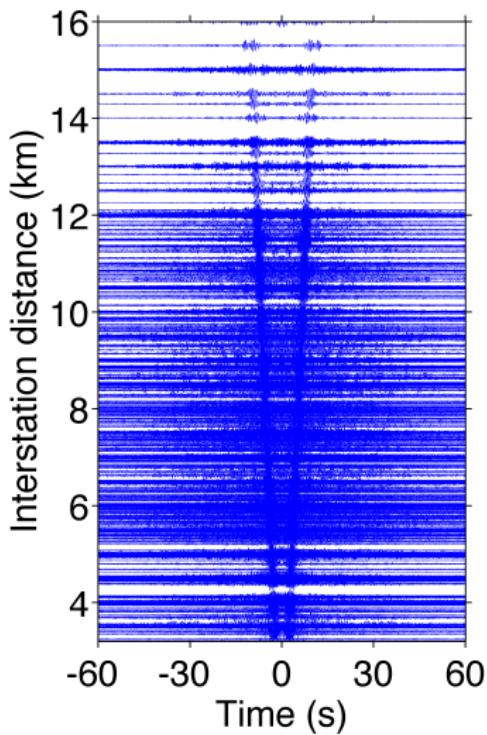


Green's function gathers

Z-component

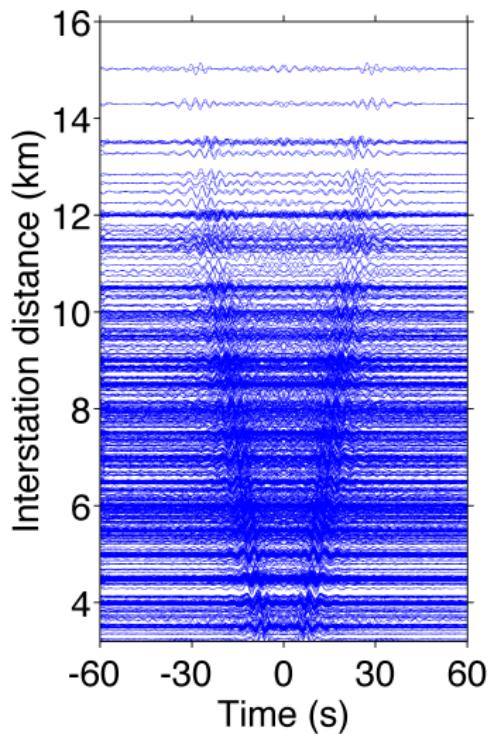


P-component

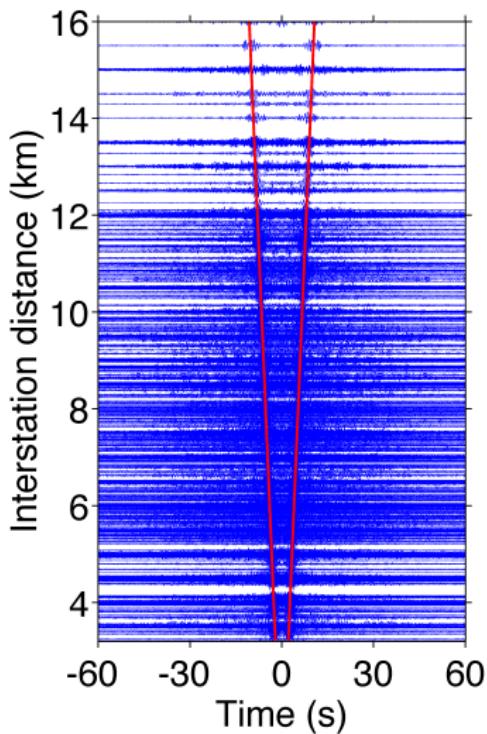


Green's function gathers

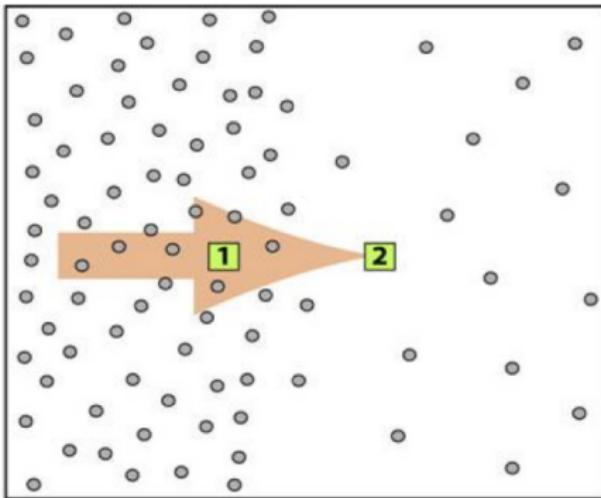
Z-component



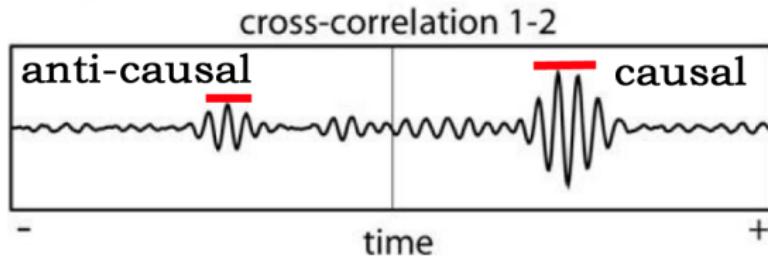
P-component



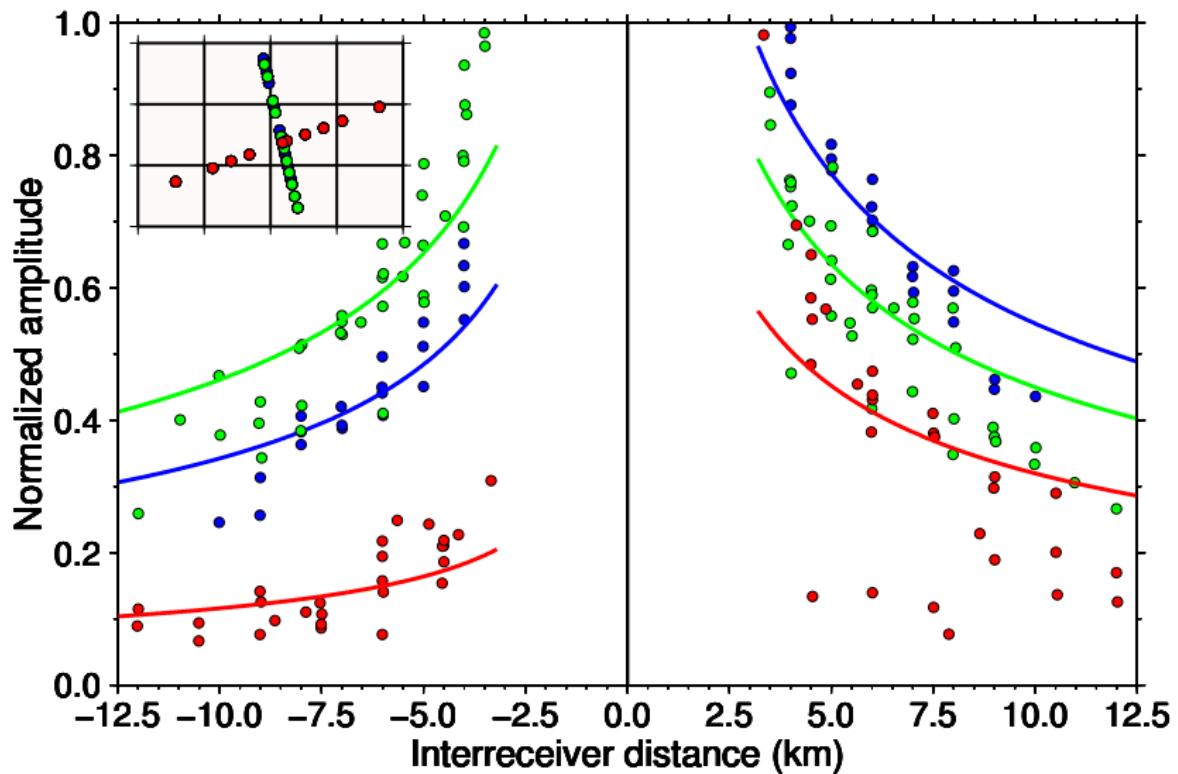
Relation to source distribution



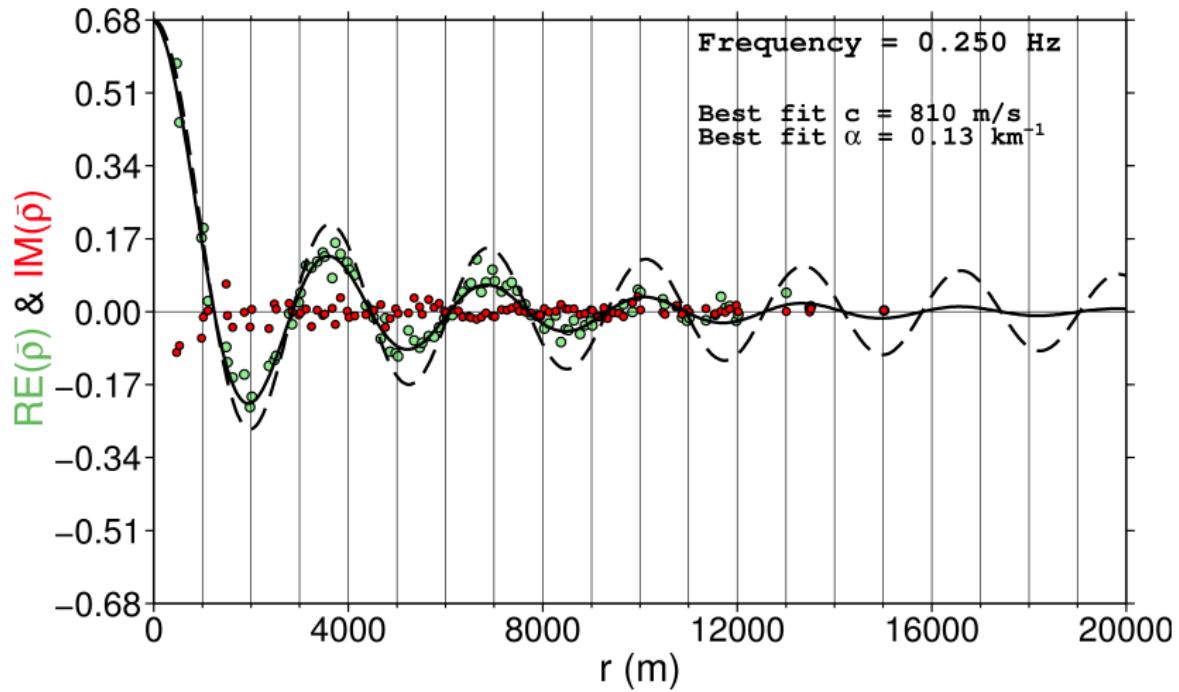
Modified from Stehly et al. (2006), Journal of Geophysical Research



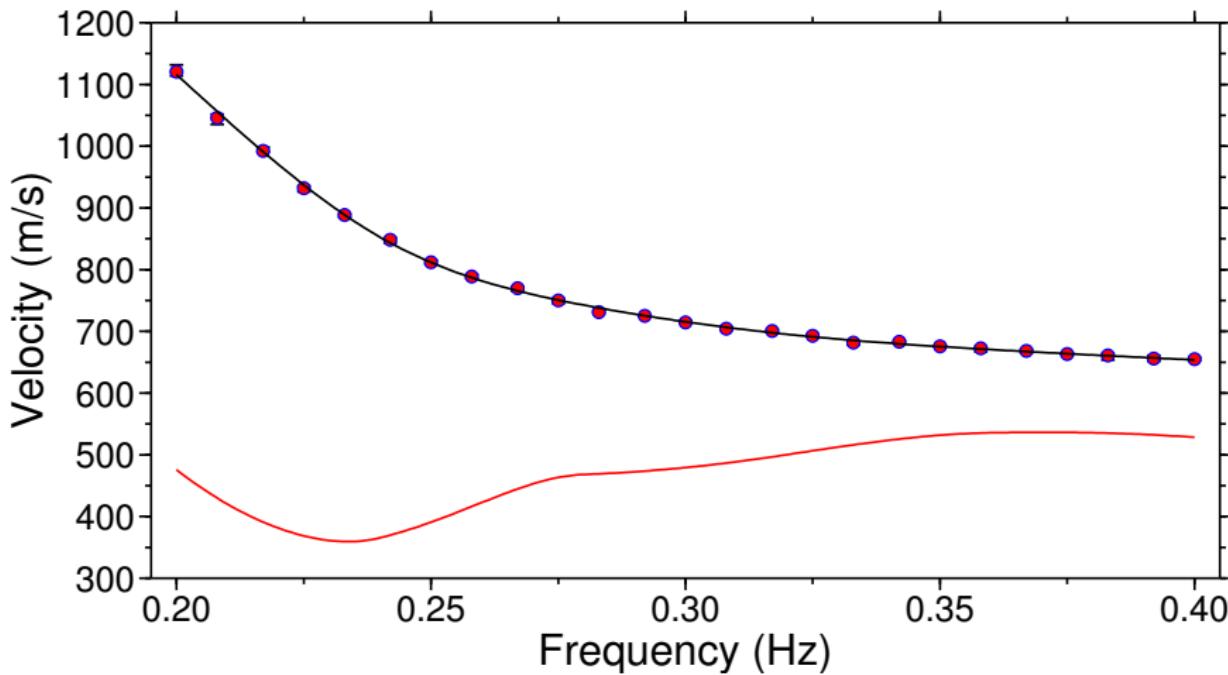
Decay in time-domain



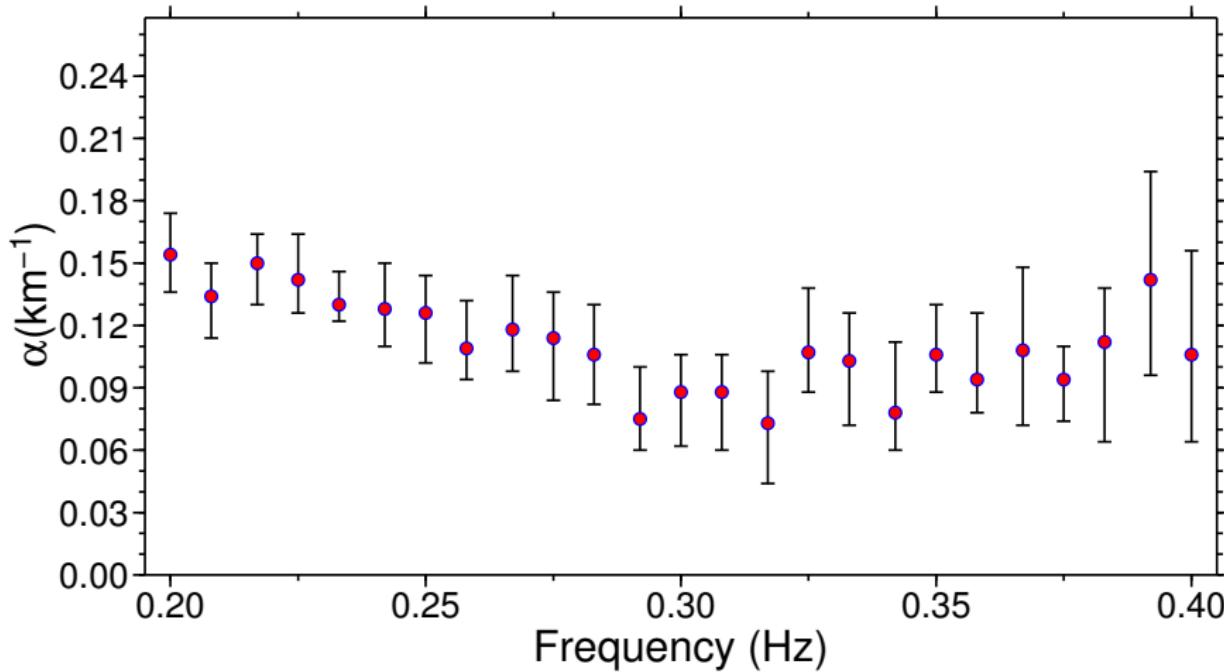
Coherency for a single frequency



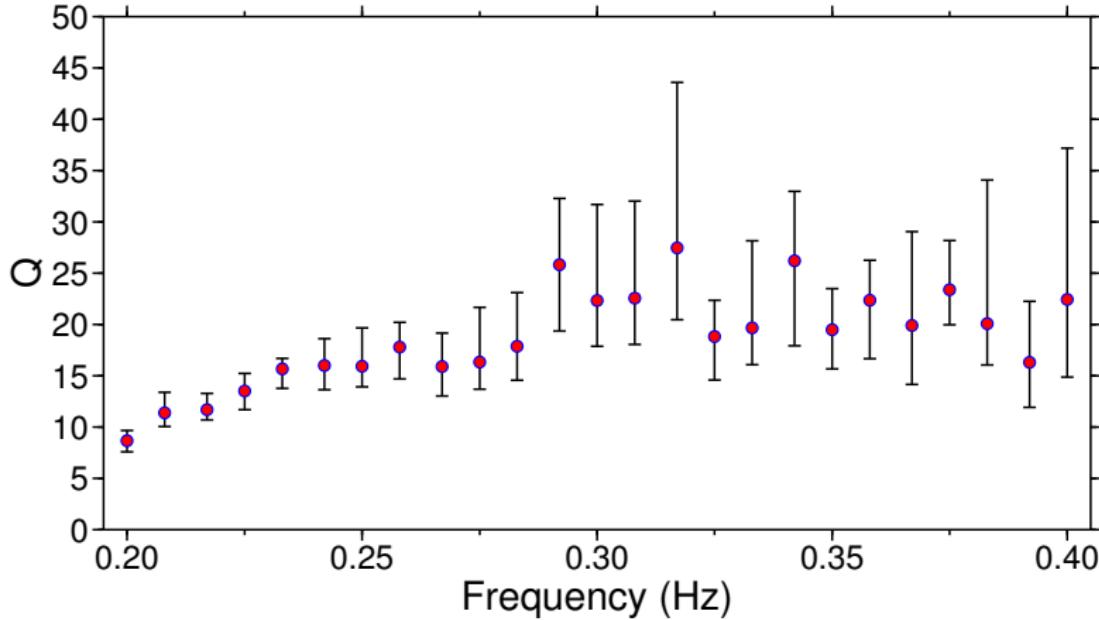
Phase and group velocities



Attenuation coefficients

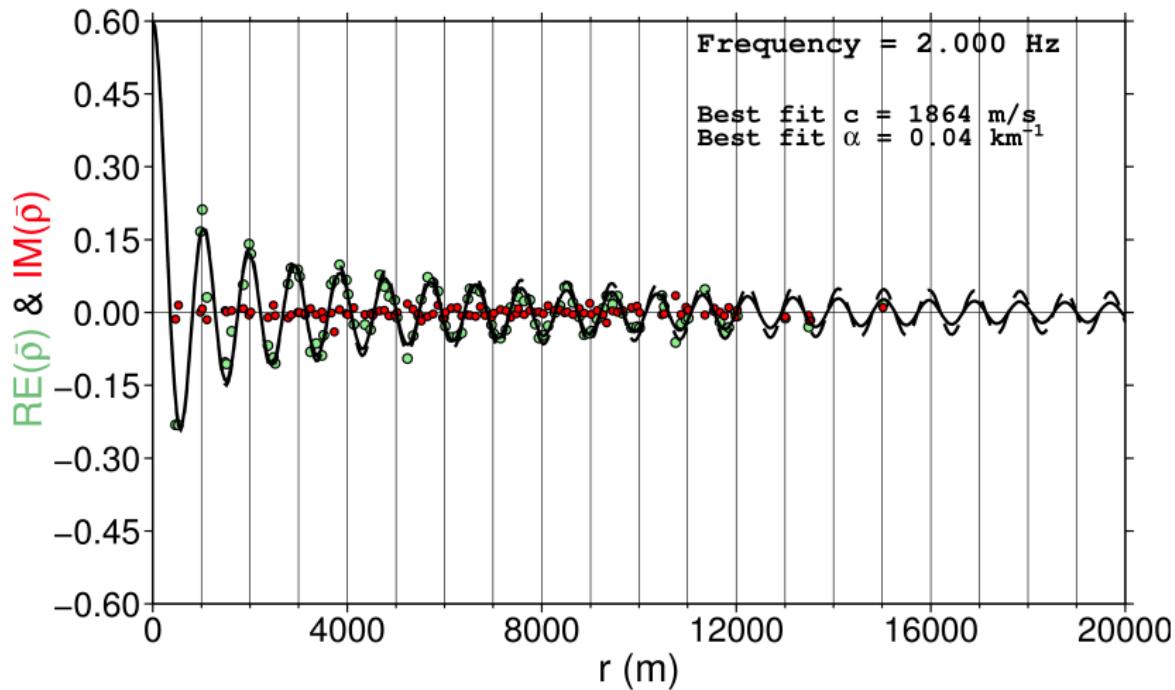


Quality factors

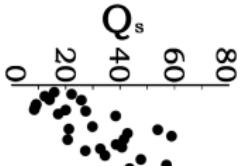
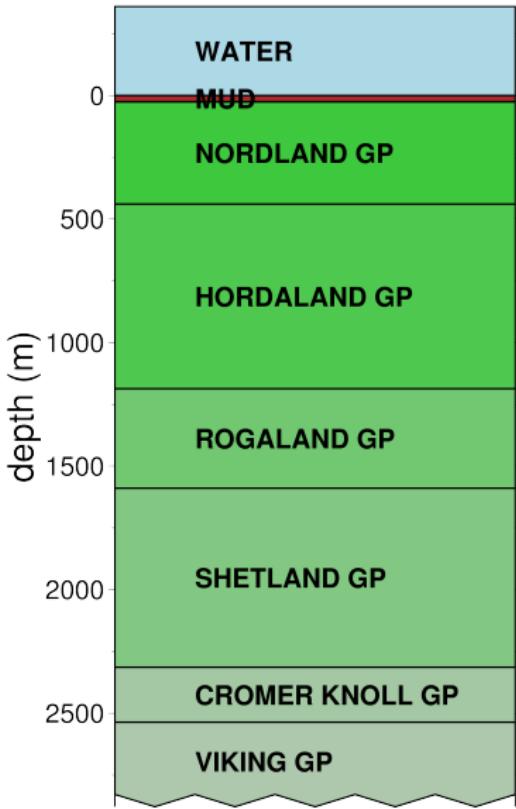


$$Q(\omega) = \left(\frac{\omega}{2\alpha(\omega)U(\omega)} \right)$$

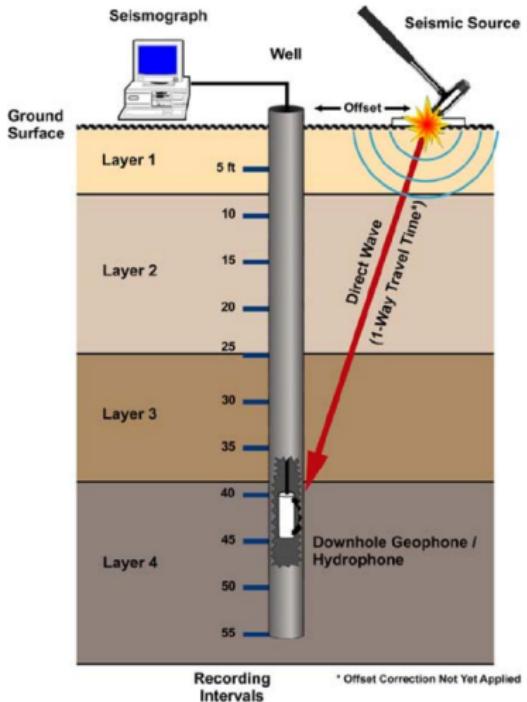
Attenuation of seawater?



Interpretation



*Reid et al.
(2001),
SEG Expanded
Abstract.*



Conclusions

- stable Green's functions
- reasonable fit to damped Bessel functions
- 1-D estimate of phase velocities
- reasonable quality factors
- first order comparison with geology

Acknowledgements

- QUEST Initial Training Network.
- Statoil and especially Peter Hanssen.
- Julie Verbeke, Sacha Bussat, Clotaire Michel and Steve Della Mora.



THANK YOU



References

- Bussat, S., and S. Kugler, 2011, Offshore ambient-noise surface-wave tomography above 0.1 Hz and its applications: *The Leading Edge*, **30**, 514–524.
- Lawrence, J. F., and G. A. Prieto, 2011, Attenuation tomography of the western united states from ambient seismic noise: *Journal of Geophysical Research*, **116**.
- Reid, F. J. L., P. H. Nguyen, C. MacBeth, and R. A. Clark, 2001, Q estimates from north sea vsps: *SEG Technical Program Expanded Abstracts*, **20**, 440–443.
- Stehly, L., M. Campillo, and N. M. Shapiro, 2006, A study of the seismic noise from its long-range correlation properties: *Journal of Geophysical Research*, **111**.

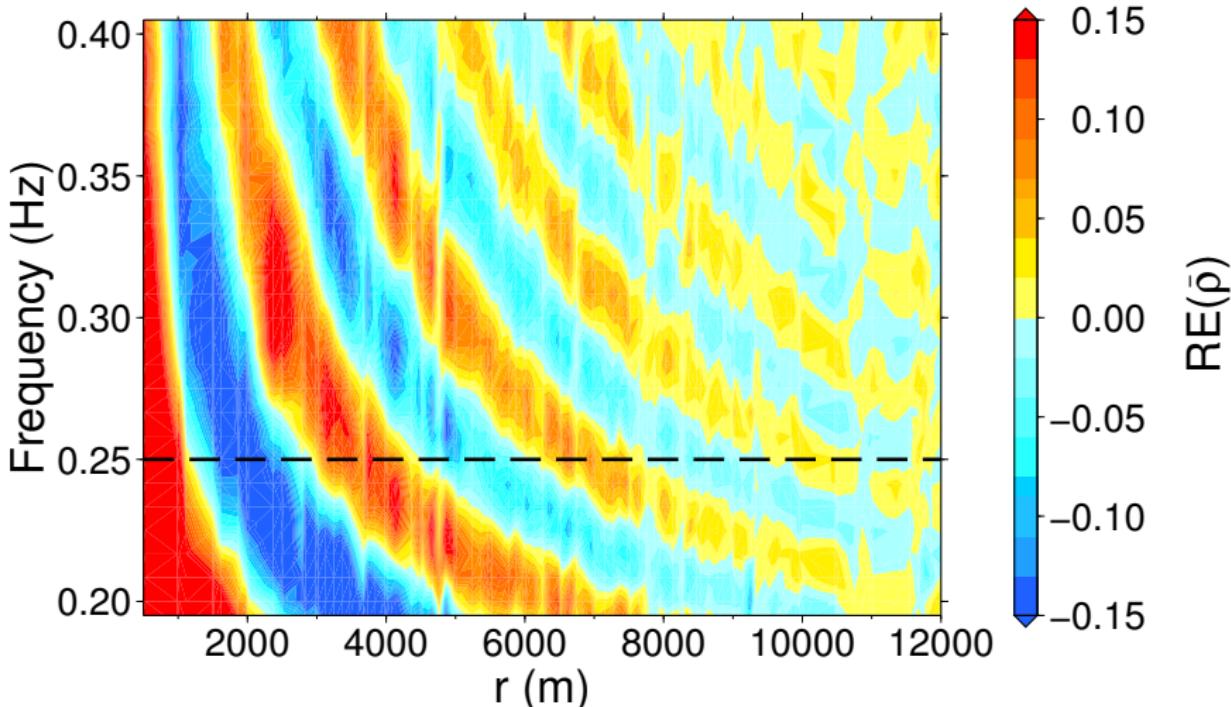
Processing sequence

- ① synchronous periods selected
- ② shorter time windows with 75% overlap
- ③ time windows are detrended
- ④ Fourier transformation
- ⑤ whitening of the amplitude spectra
- ⑥ cross-correlation
- ⑦ time averaging
- ⑧ time domain: inverse Fourier transformation
- ⑨ frequency domain: azimuthal averaging

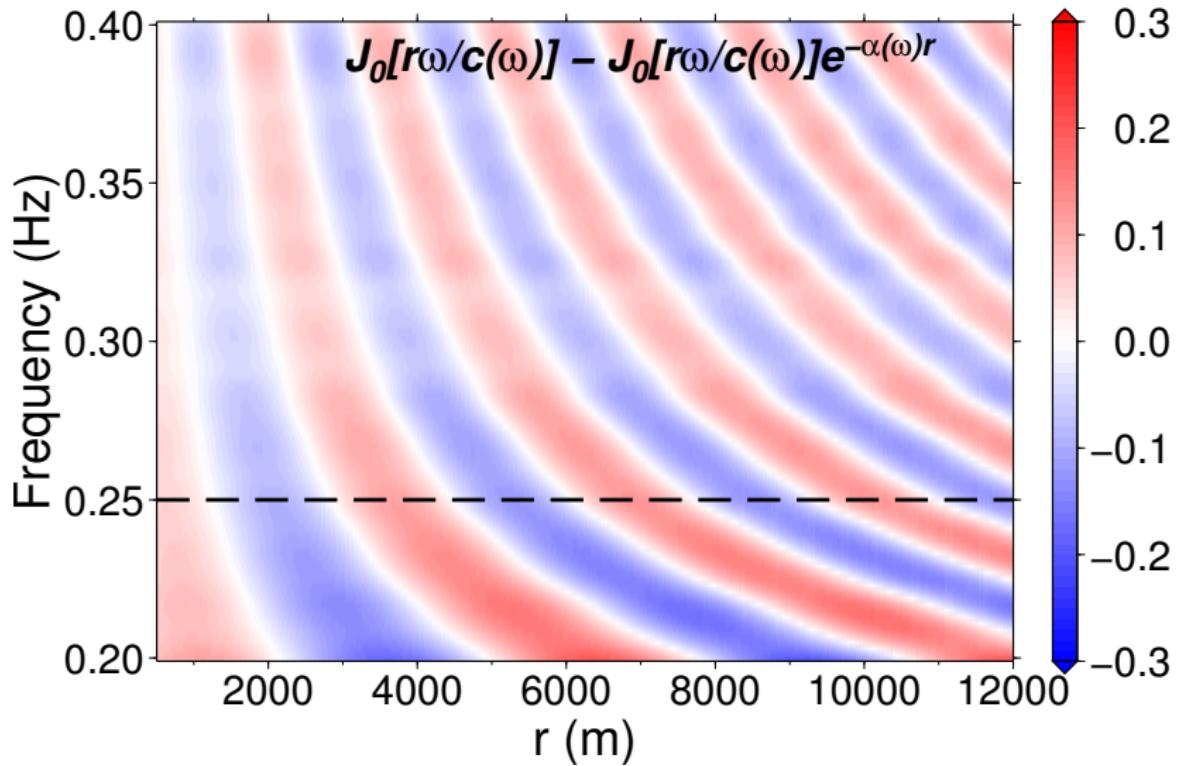
$$\frac{U(\mathbf{x}_1, \omega) U^*(\mathbf{x}_2, \omega)}{|U(\mathbf{x}_1, \omega)| |U(\mathbf{x}_2, \omega)|}$$

$$\sum_{\text{azimuth}} \sum_{\text{time}} C_{x_1 x_2}(\omega)$$

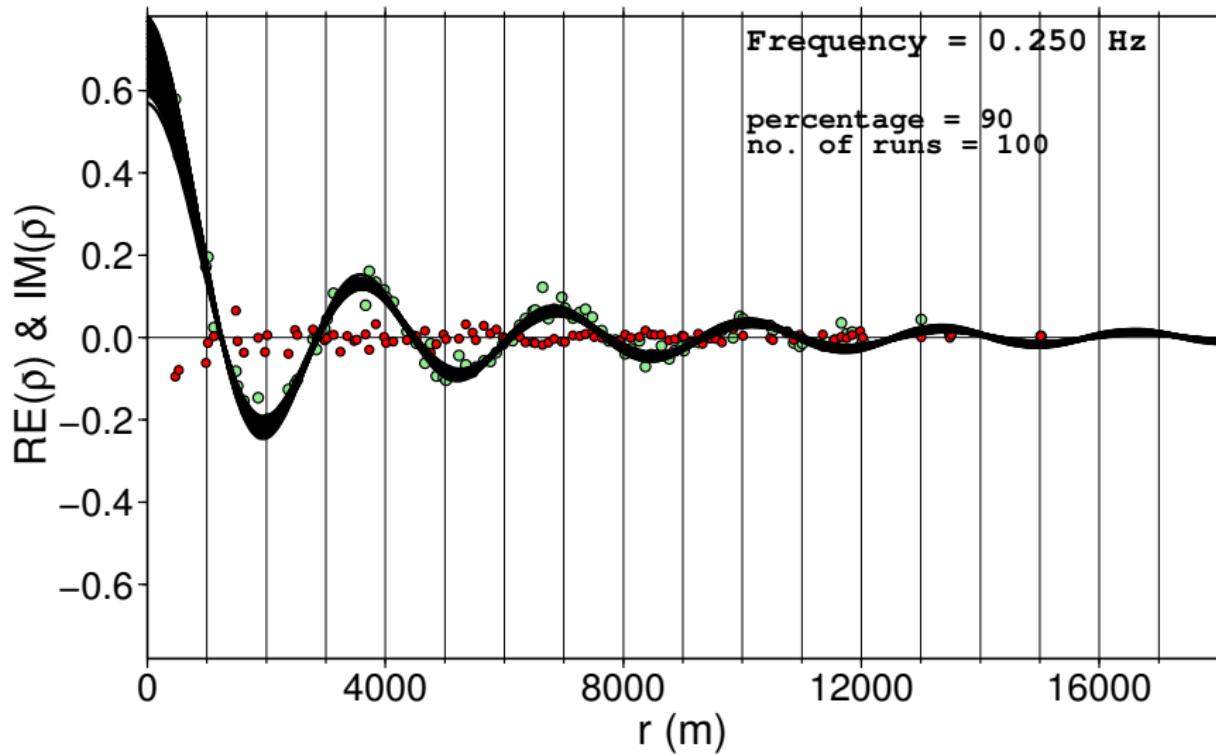
Coherency with frequency



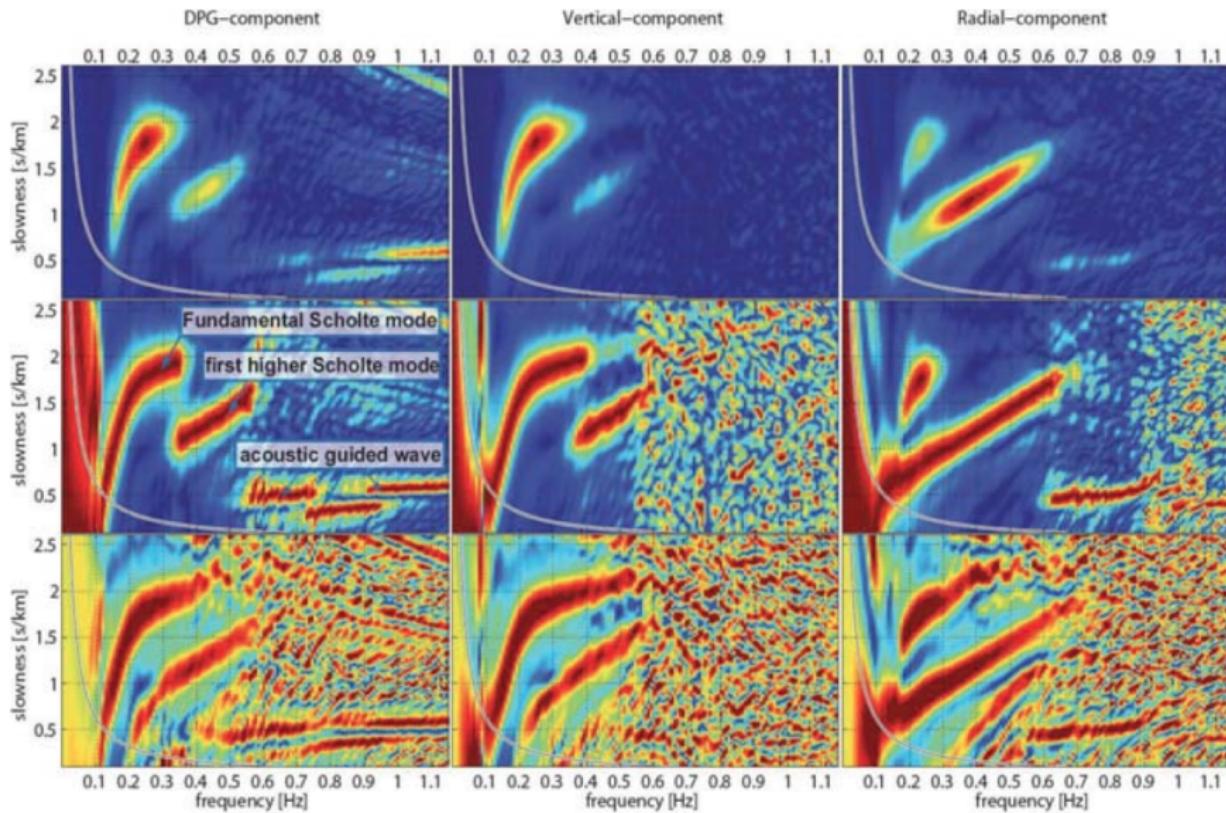
Difference between models



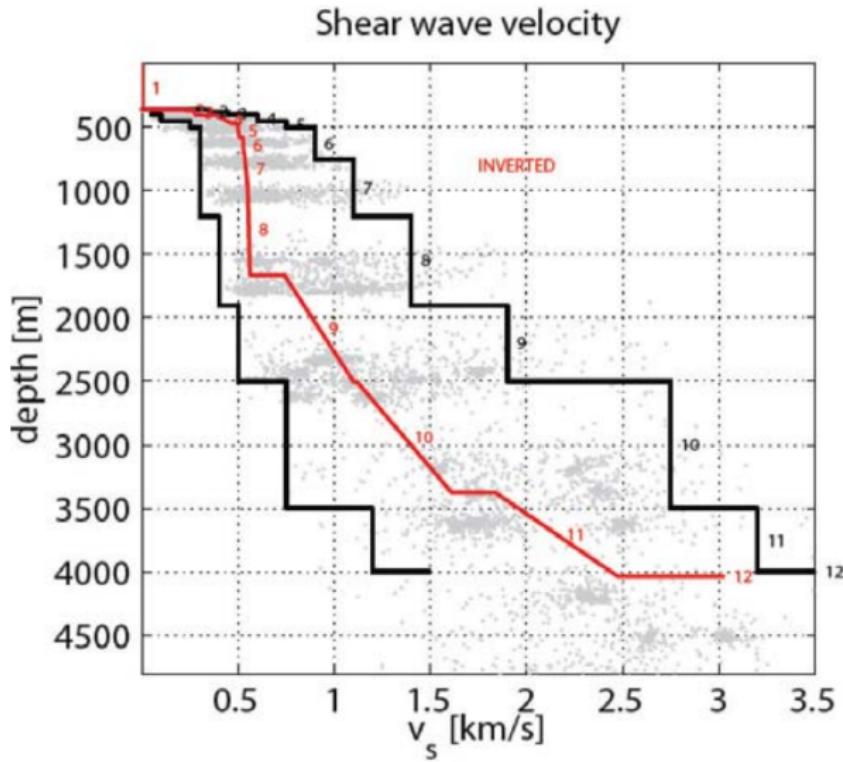
Bootstrapping



Dispersion (Bussat and Kugler, 2011)

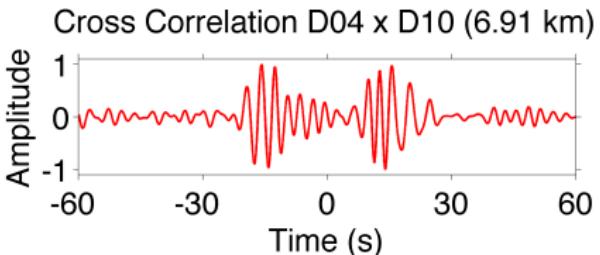
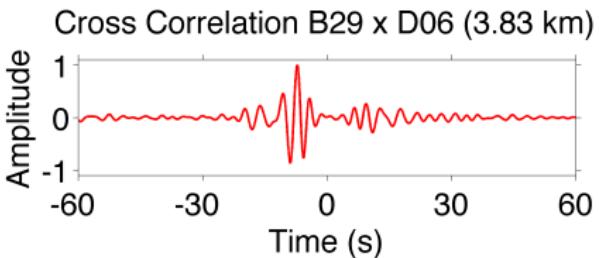
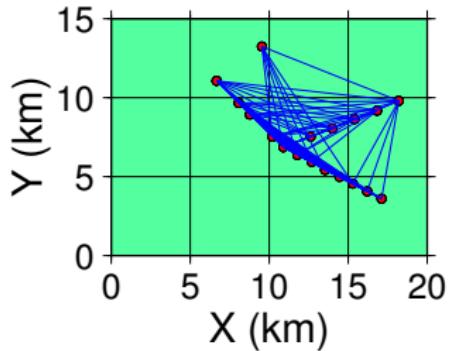
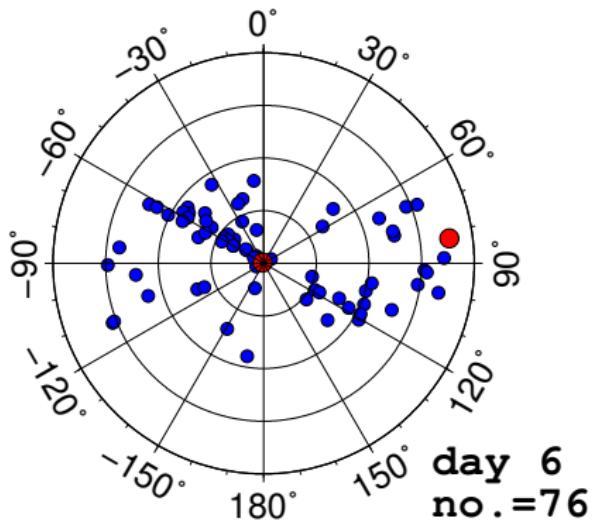


Velocity inversion



Bussat and Kugler (2011), *The Leading Edge*

Isotropic wavefield?



Wavefield over time

