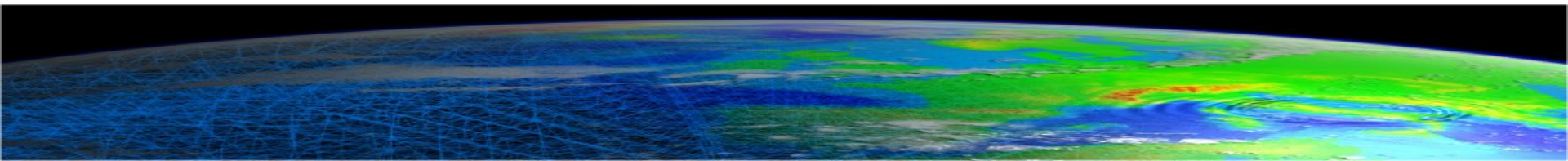


Earthquake source parameters from low-frequency normal mode data using the Neighbourhood Algorithm

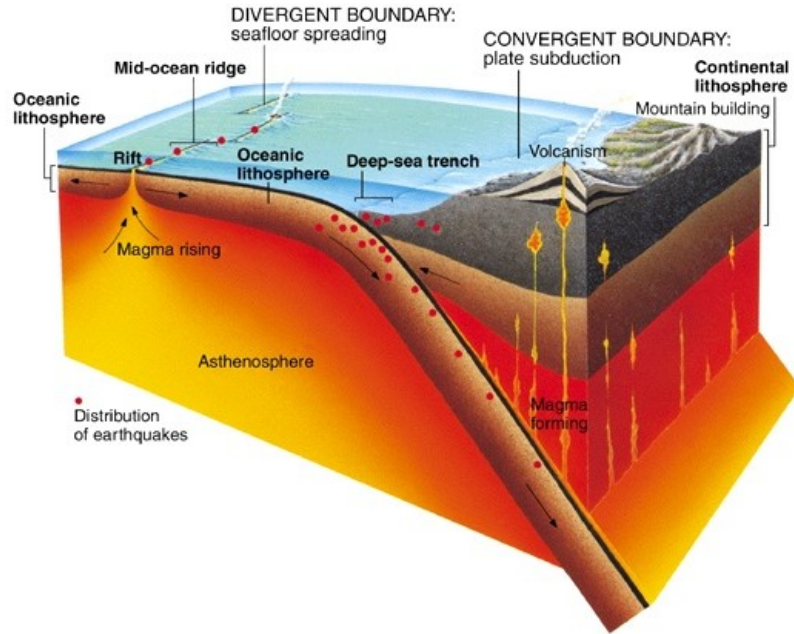
K. Lentas⁽¹⁾, A. M. G. Ferreira⁽¹⁾, E. Clévéde⁽²⁾

⁽¹⁾School of Environmental Sciences, University of East Anglia, Norwich, UK

⁽²⁾Institut du Globe de Physique, Paris, France



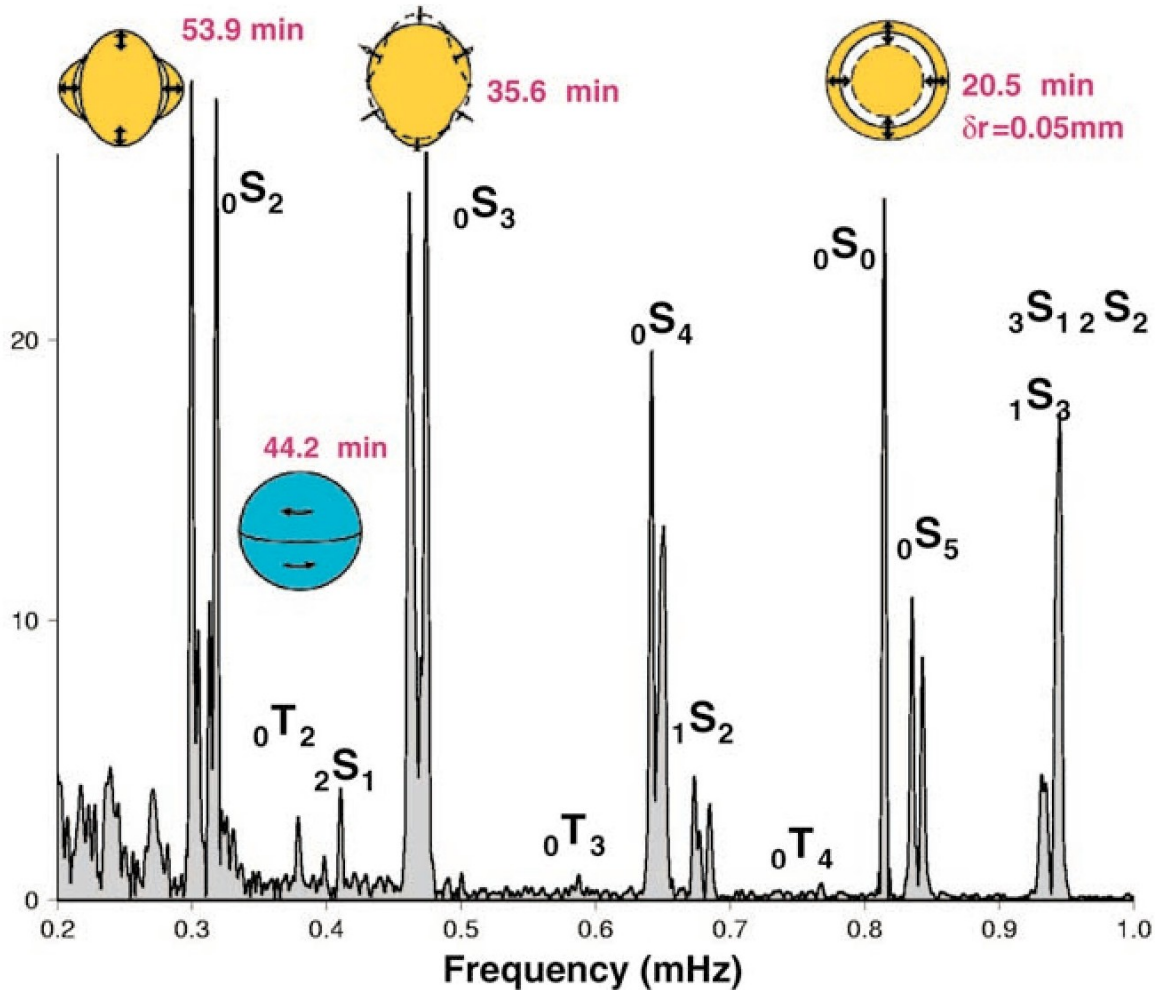
Goal and motivation



- Large magnitude – shallow earthquakes
- Tsunami excitation
- Finite character of the source
- Uncertainties in source parameters

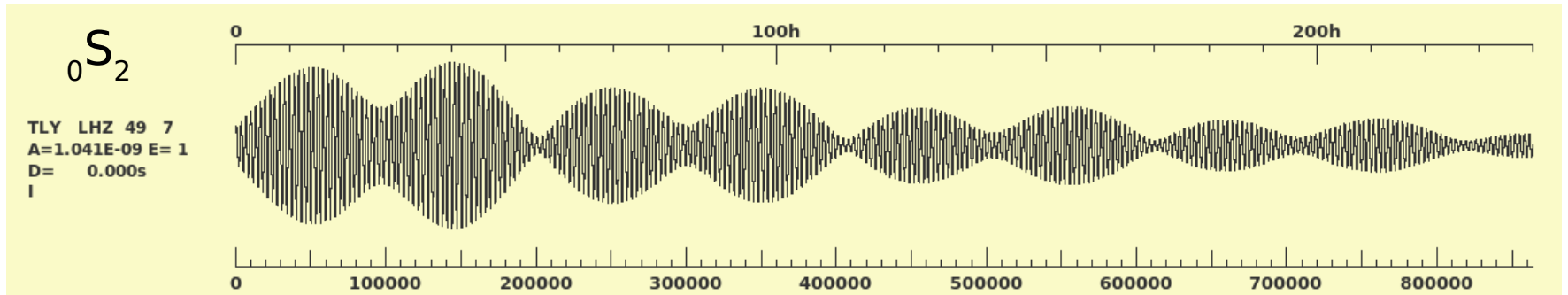
Goal and motivation

Earth's free oscillations

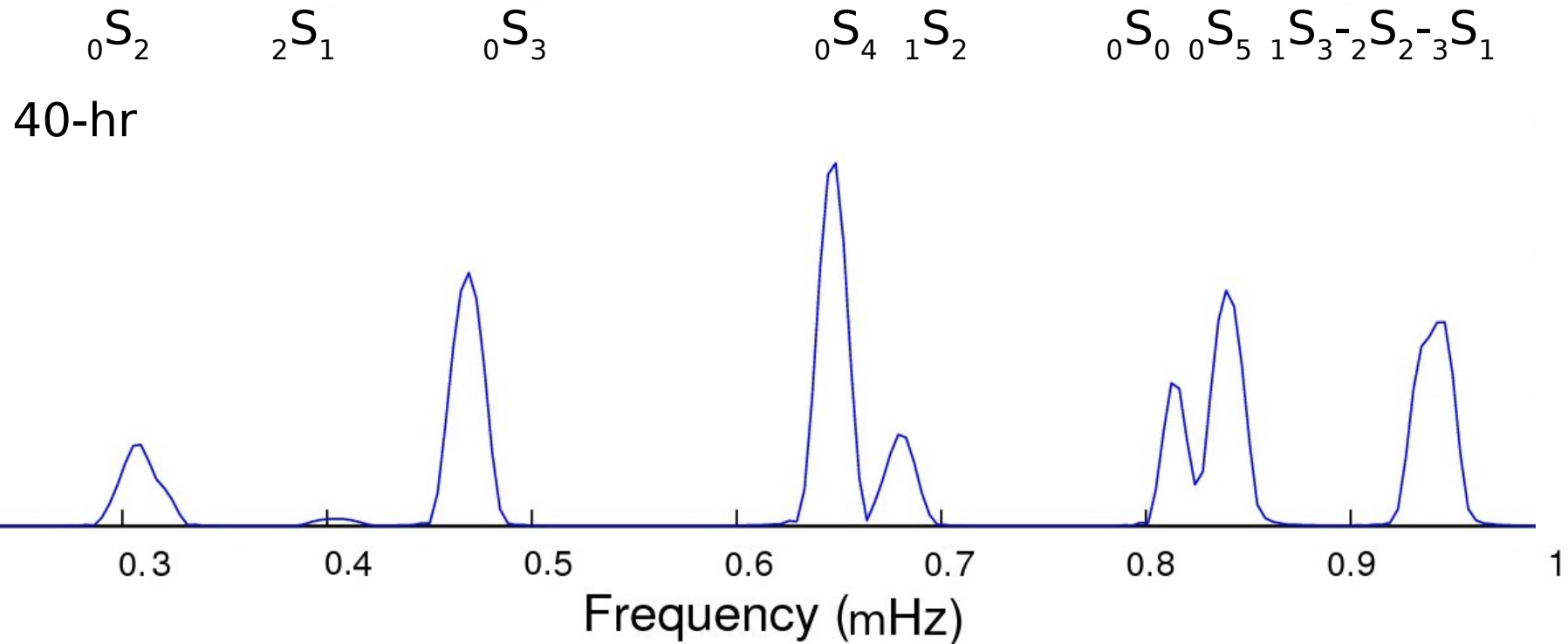
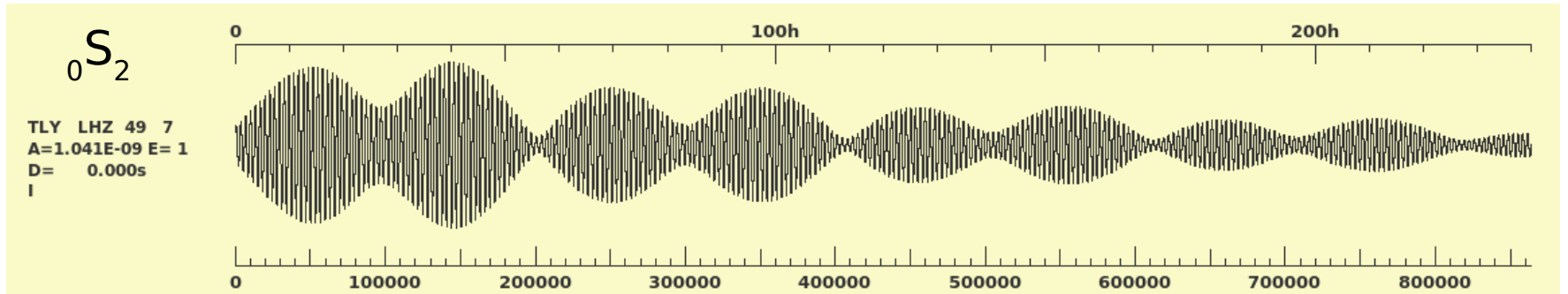


Park et al. (2005)

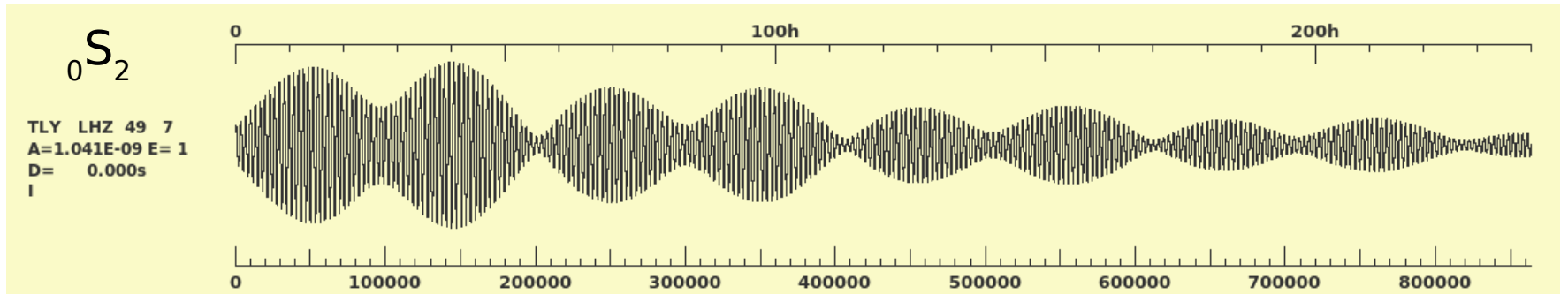
Earth's free oscillations



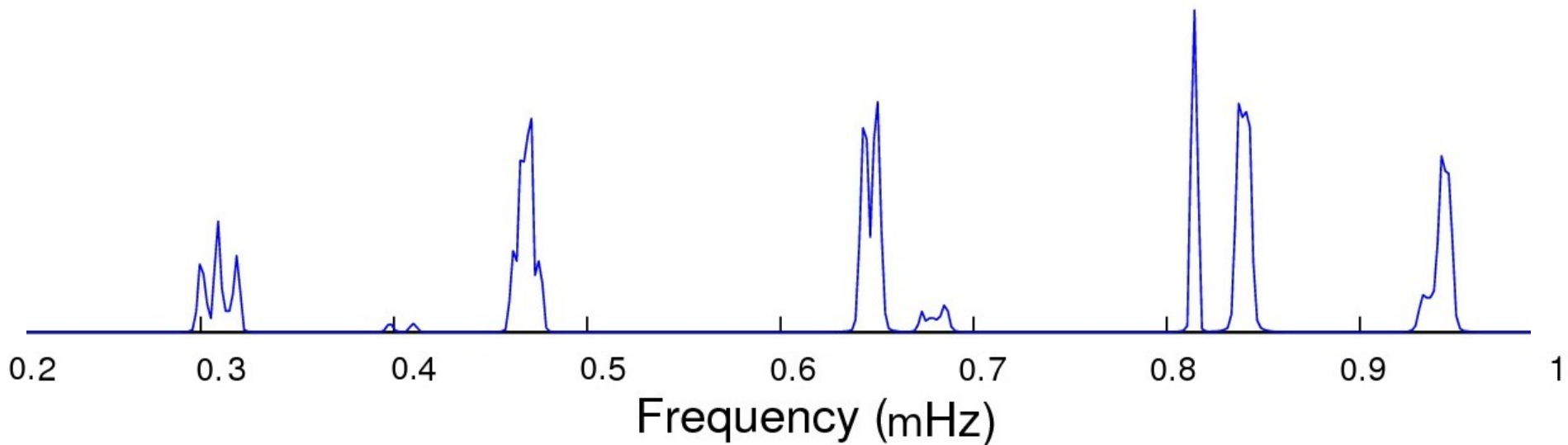
Earth's free oscillations



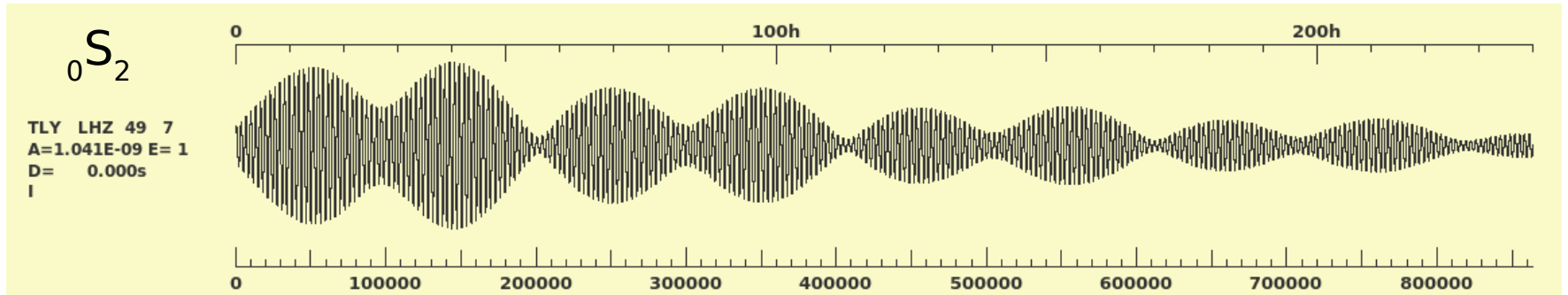
Earth's free oscillations



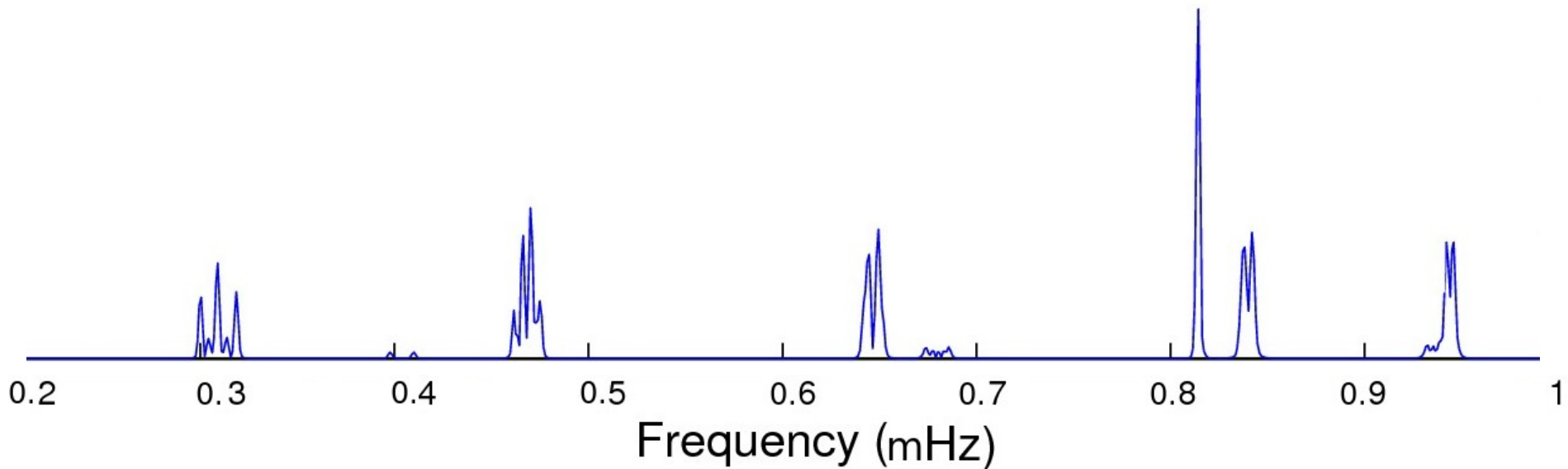
$0S_2$ $2S_1$ $0S_3$ $0S_4$ $1S_2$ $0S_0$ $0S_5$ $1S_3$ $2S_2$ $3S_1$
 144-hr



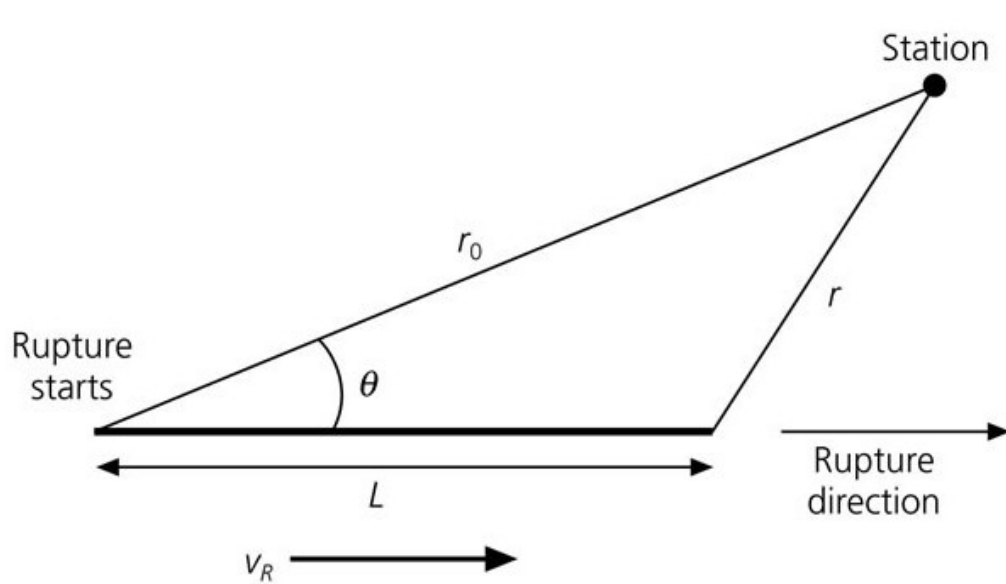
Earth's free oscillations



$0S_2$ $2S_1$ $0S_3$ $0S_4$ $1S_2$ $0S_0$ $0S_5$ $1S_3$ $2S_2$ $3S_1$
 240-hr

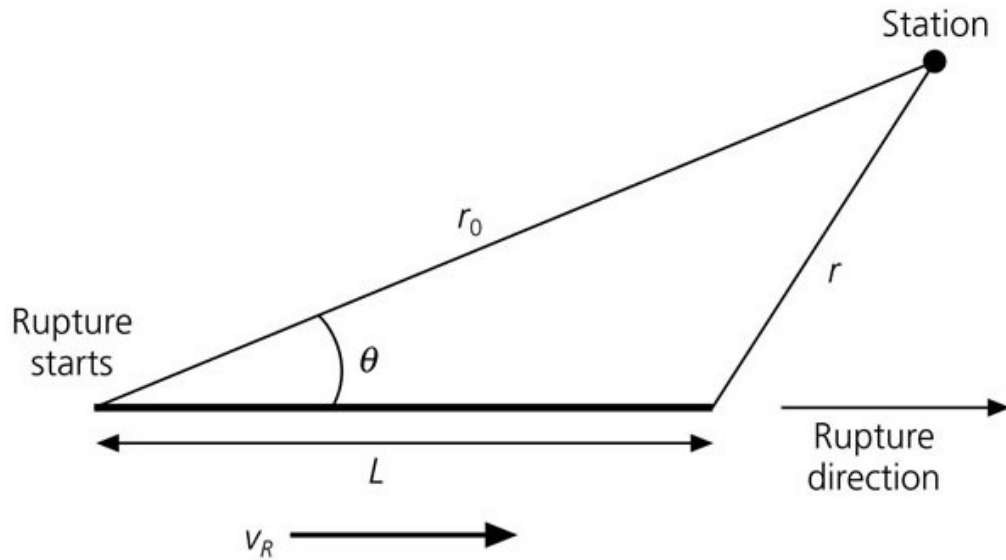


Finite source description



$$a_{fs}^m(x, \omega) = a_{ps}^m(x, \omega) \cdot F_m$$

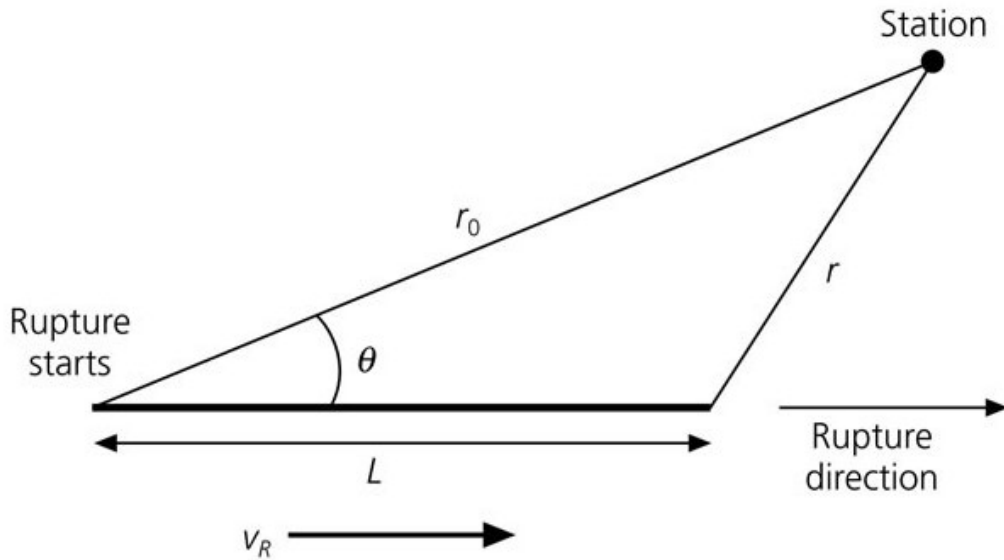
Finite source description



$$a_{fs}^m(x, \omega) = a_{ps}^m(x, \omega) \cdot F_m$$

$$a_{fs}^m(x, \omega) = \sum_{i=1}^6 (\psi_i^m(x, \omega) \cdot M_i) \cdot F_m$$

Finite source description



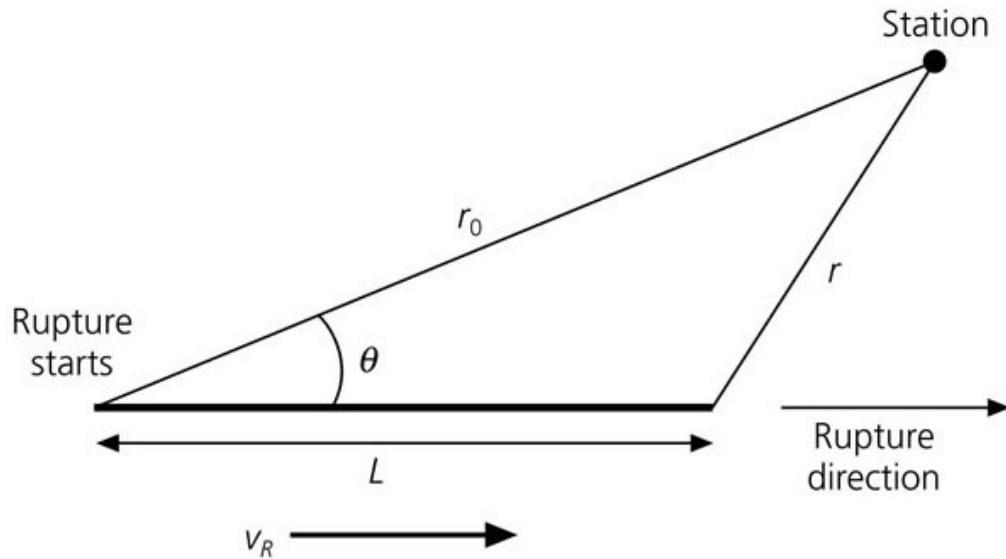
$$a_{fs}^m(x, \omega) = a_{ps}^m(x, \omega) \cdot F_m$$

$$a_{fs}^m(x, \omega) = \sum_{i=1}^6 (\psi_i^m(x, \omega) \cdot M_i) \cdot F_m$$

$$F_m = \frac{\sin(X_m)}{X_m} e^{-iX_m}$$

$$X_m = f(L, T_r)$$

Finite source description



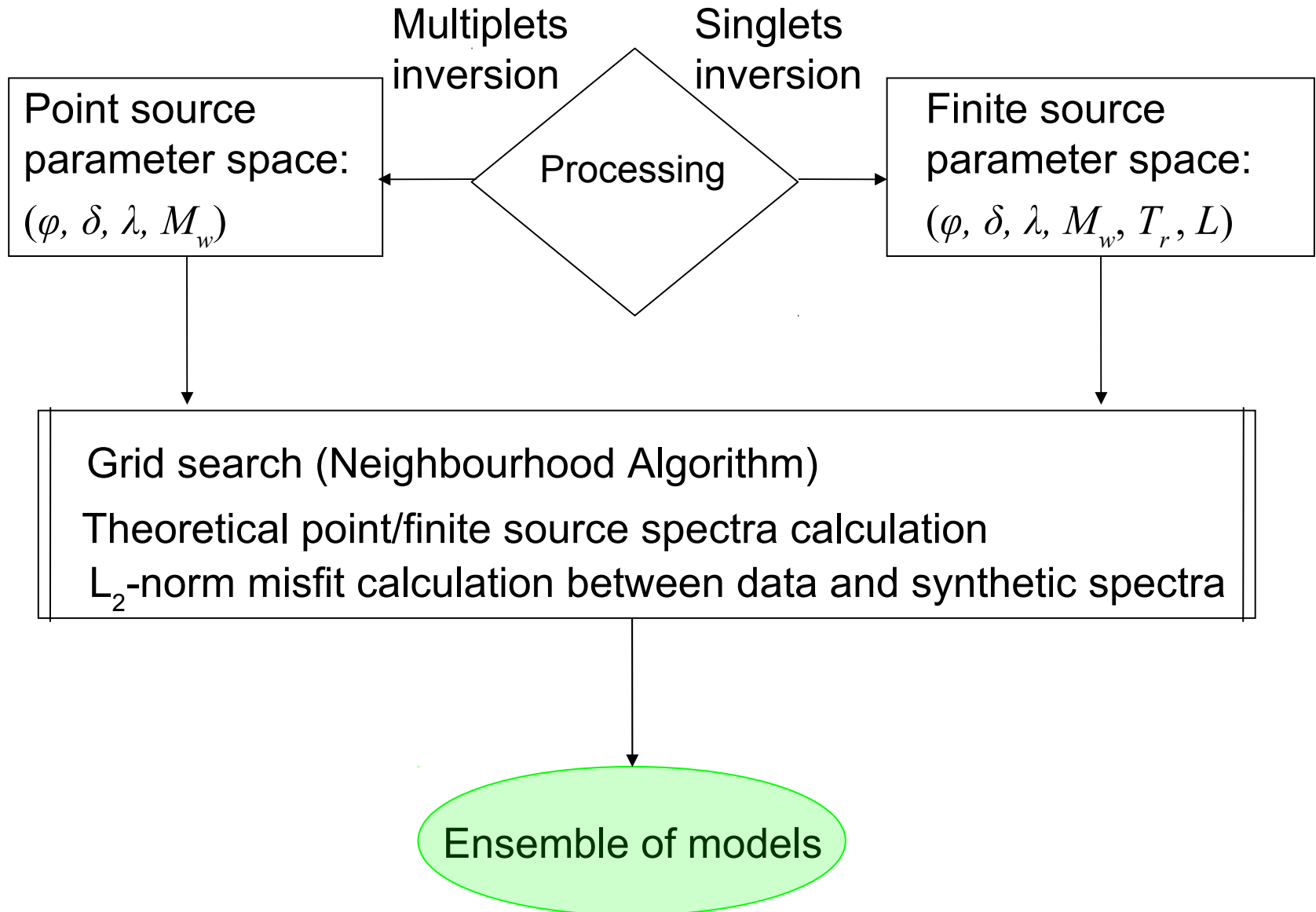
$$a_{fs}^m(x, \omega) = a_{ps}^m(x, \omega) \cdot F_m$$

$$a_{fs}^m(x, \omega) = \sum_{i=1}^6 (\psi_i^m(x, \omega) \cdot M_i) \cdot F_m$$

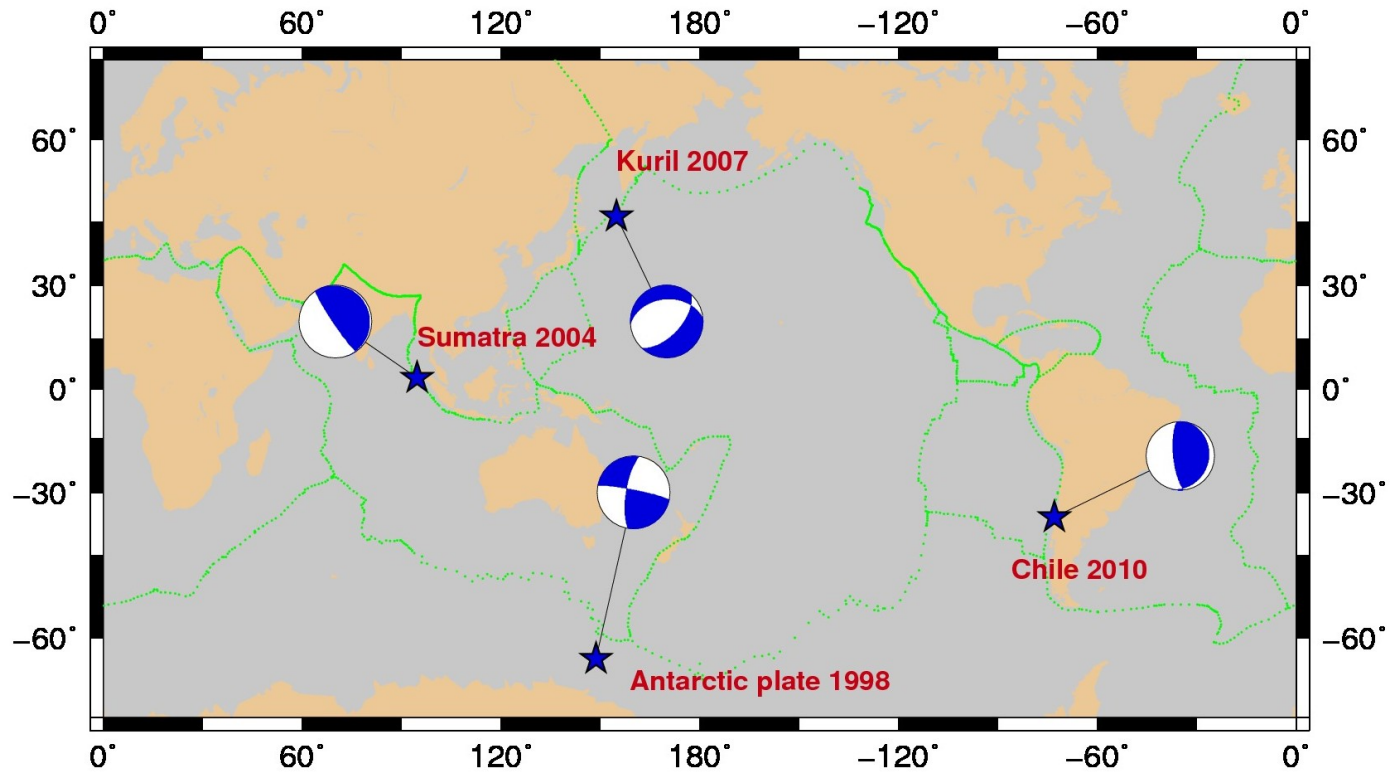
$$F_m = \frac{\sin(X_m)}{X_m} e^{-iX_m}$$

$$X_m = f(L, T_r) \rightarrow \text{Average Rupture Velocity}$$

Probabilistic normal mode source inversion



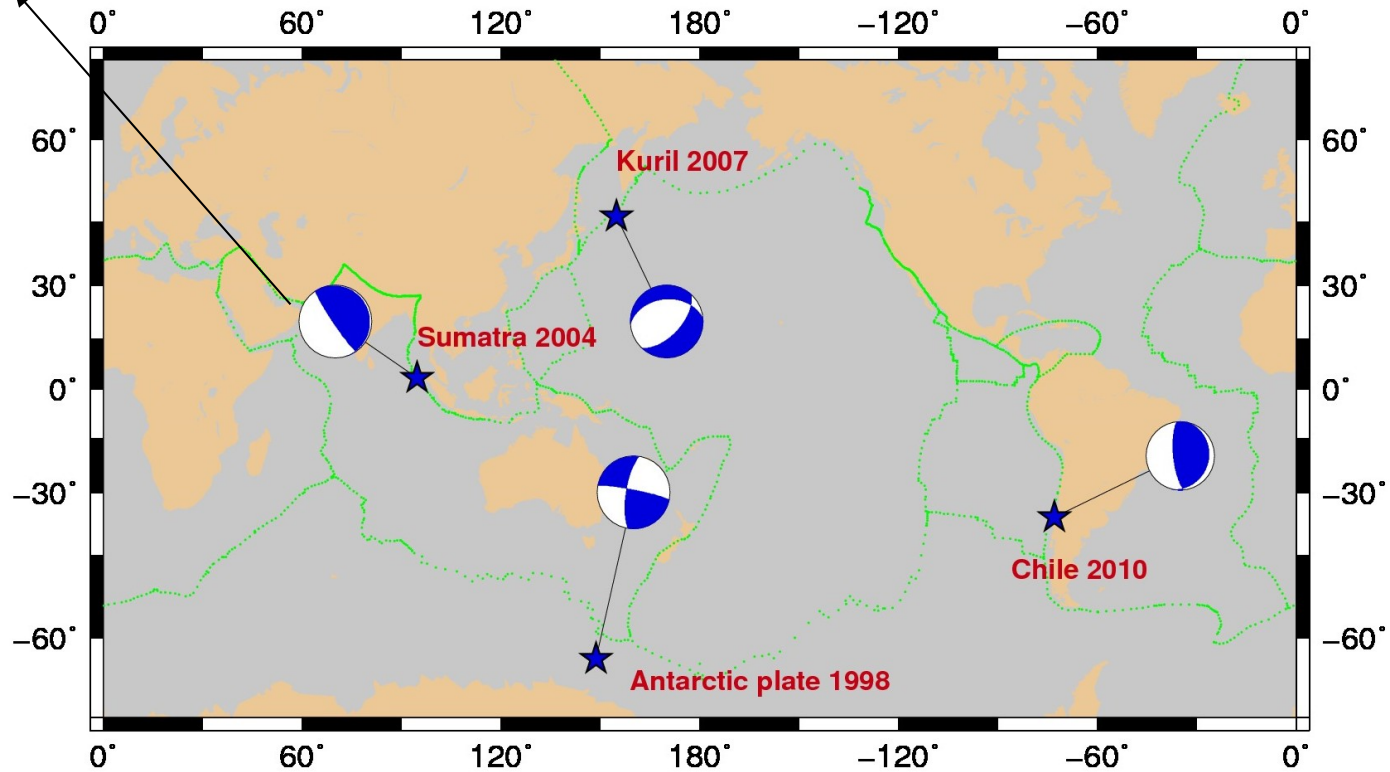
Synthetic tests



- Neglecting the finiteness of the source
- Noise in data
- Earth's structure
- Location and origin time errors

$M_w = 9.3$
 $(T_r, L) = (545s, 1140km)$
Tsai et al. (2005)

Synthetic tests



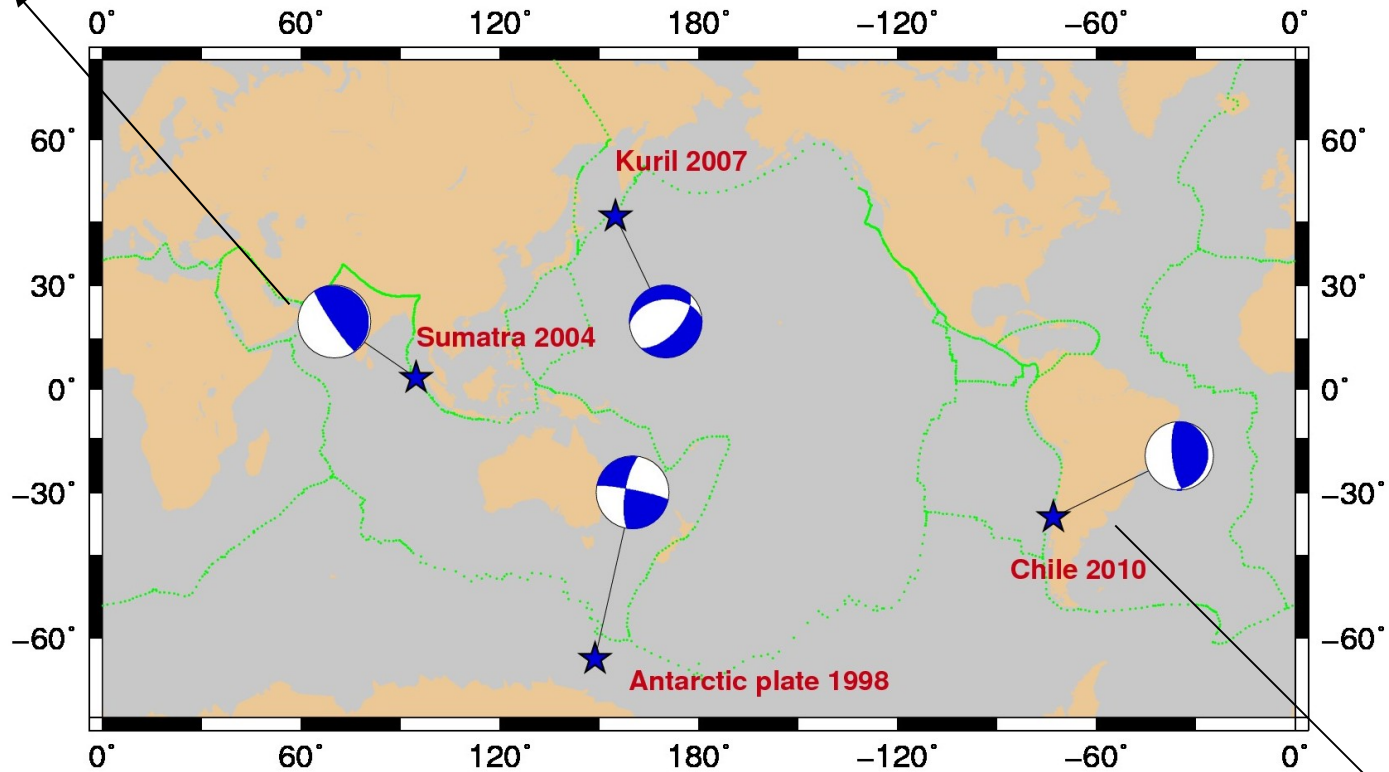
- Neglecting the finiteness of the source
- Noise in data
- Earth's structure
- Location and origin time errors

Synthetic tests

$M_w = 9.3$

$(T_r, L) = (545\text{s}, 1140\text{km})$

Tsai et al. (2005)



- Neglecting the finiteness of the source
- Noise in data
- Earth's structure
- Location and origin time errors

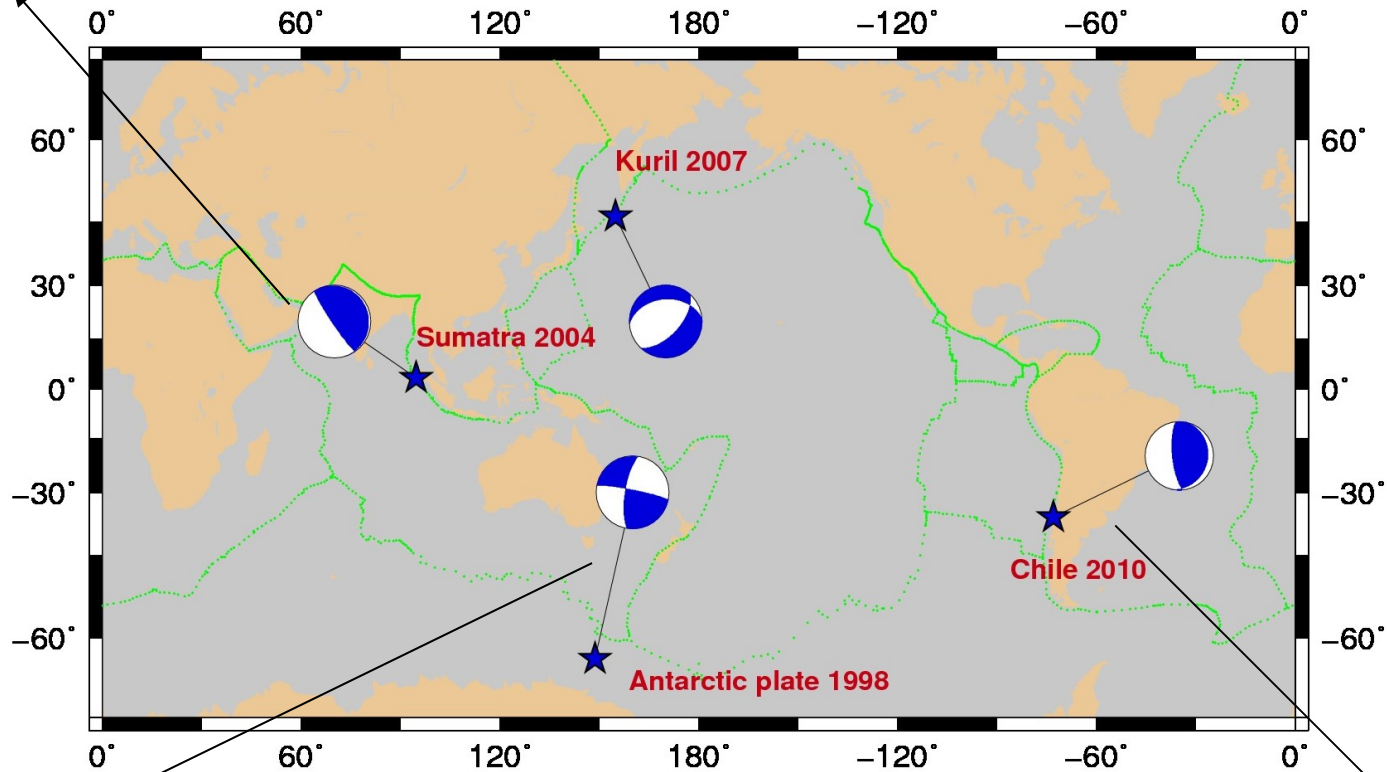
$M_w = 8.8$

$(T_r, L) = (230\text{s}, 600\text{km})$

Delouis et al. (2011)

Synthetic tests

$M_w = 9.3$
 $(T_r, L) = (545s, 1140km)$
Tsai et al. (2005)



$M_w = 8.1$
 $(T_r, L) = (90s, 240km)$
Nettles et al. (1999)

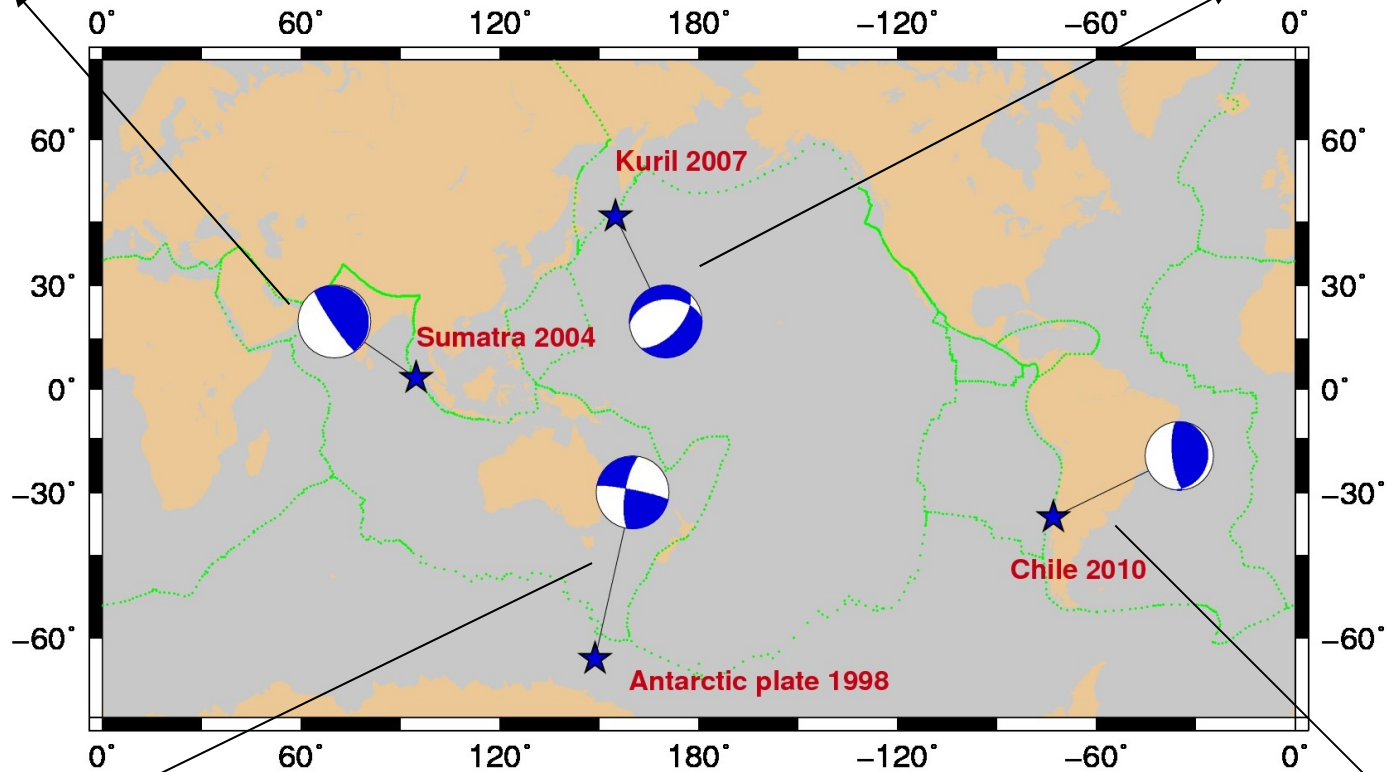
- Neglecting the finiteness of the source
- Noise in data
- Earth's structure
- Location and origin time errors

$M_w = 8.8$
 $(T_r, L) = (230s, 600km)$
Delouis et al. (2011)

Synthetic tests

$M_w = 9.3$
 $(T_r, L) = (545s, 1140km)$
Tsai et al. (2005)

$M_w = 8.1$
 $(T_r, L) = (60s, 220km)$
Lay et al. (2009)



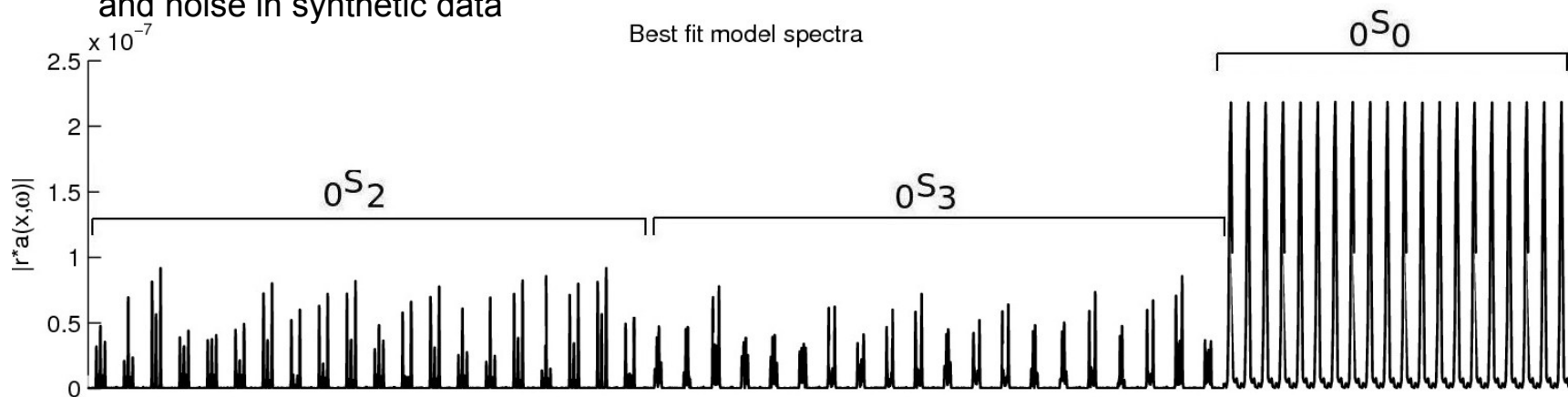
$M_w = 8.1$
 $(T_r, L) = (90s, 240km)$
Nettles et al. (1999)

- Neglecting the finiteness of the source
- Noise in data
- Earth's structure
- Location and origin time errors

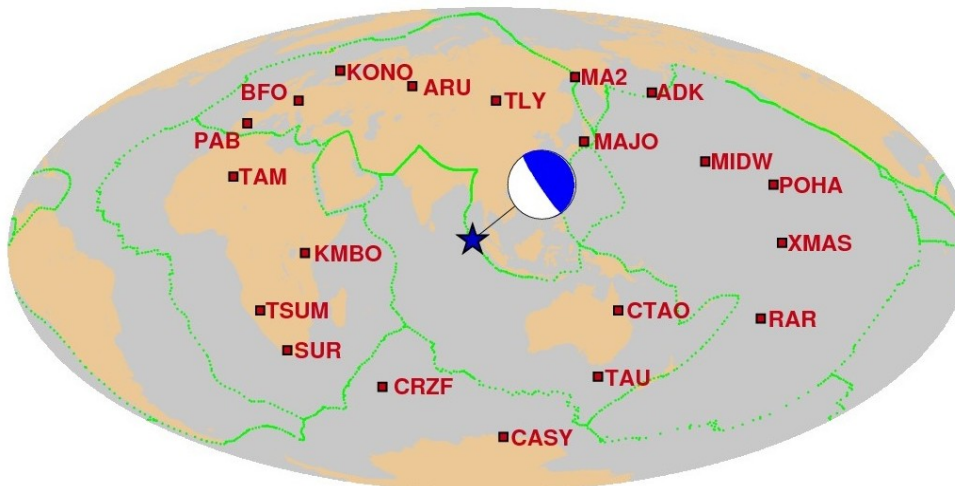
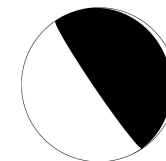
$M_w = 8.8$
 $(T_r, L) = (230s, 600km)$
Delouis et al. (2011)

Synthetic tests (Sumatra 2004 M_w 9.3 based on model of Tsai et al.(2005))

Combined effect of finiteness
and noise in synthetic data

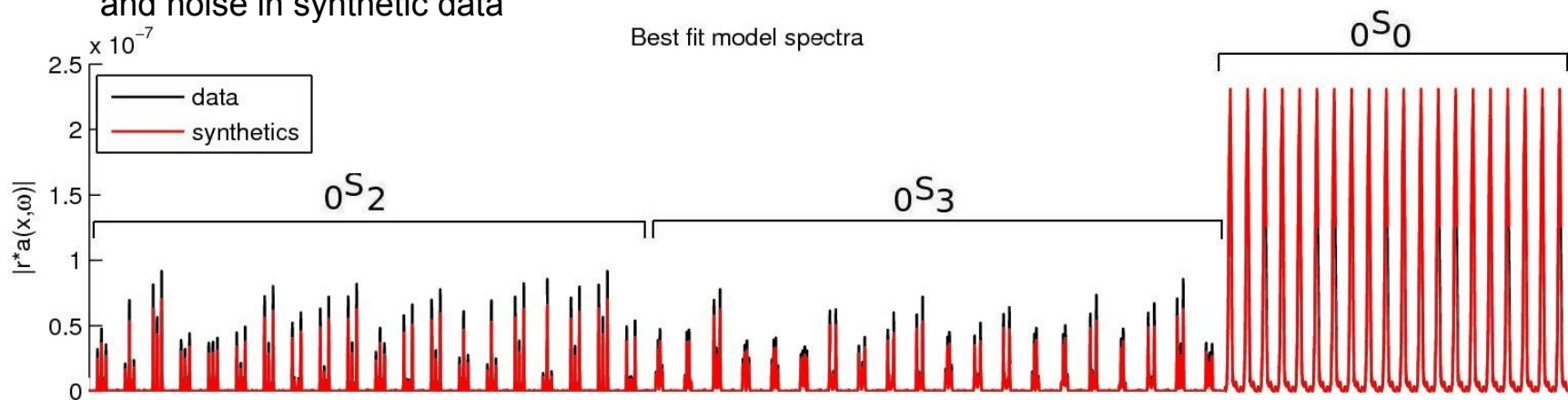


	$\varphi(^{\circ})$	$\delta(^{\circ})$	Multiplets $\lambda(^{\circ})$	M_w	T_r (s)	L (km)
Input model	343.00	6.10	107.00	9.31	545.00	1140.00

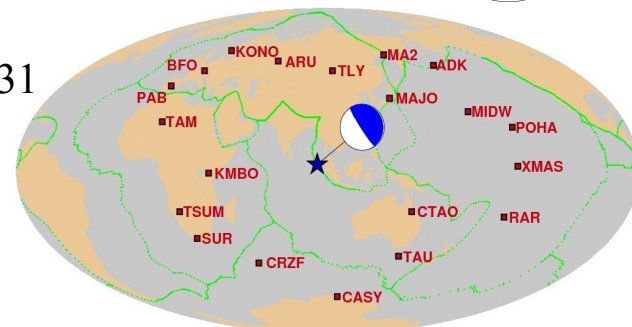
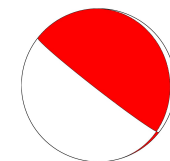
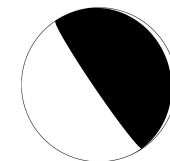


Synthetic tests (Sumatra 2004 M_w 9.3 based on model of Tsai et al.(2005))

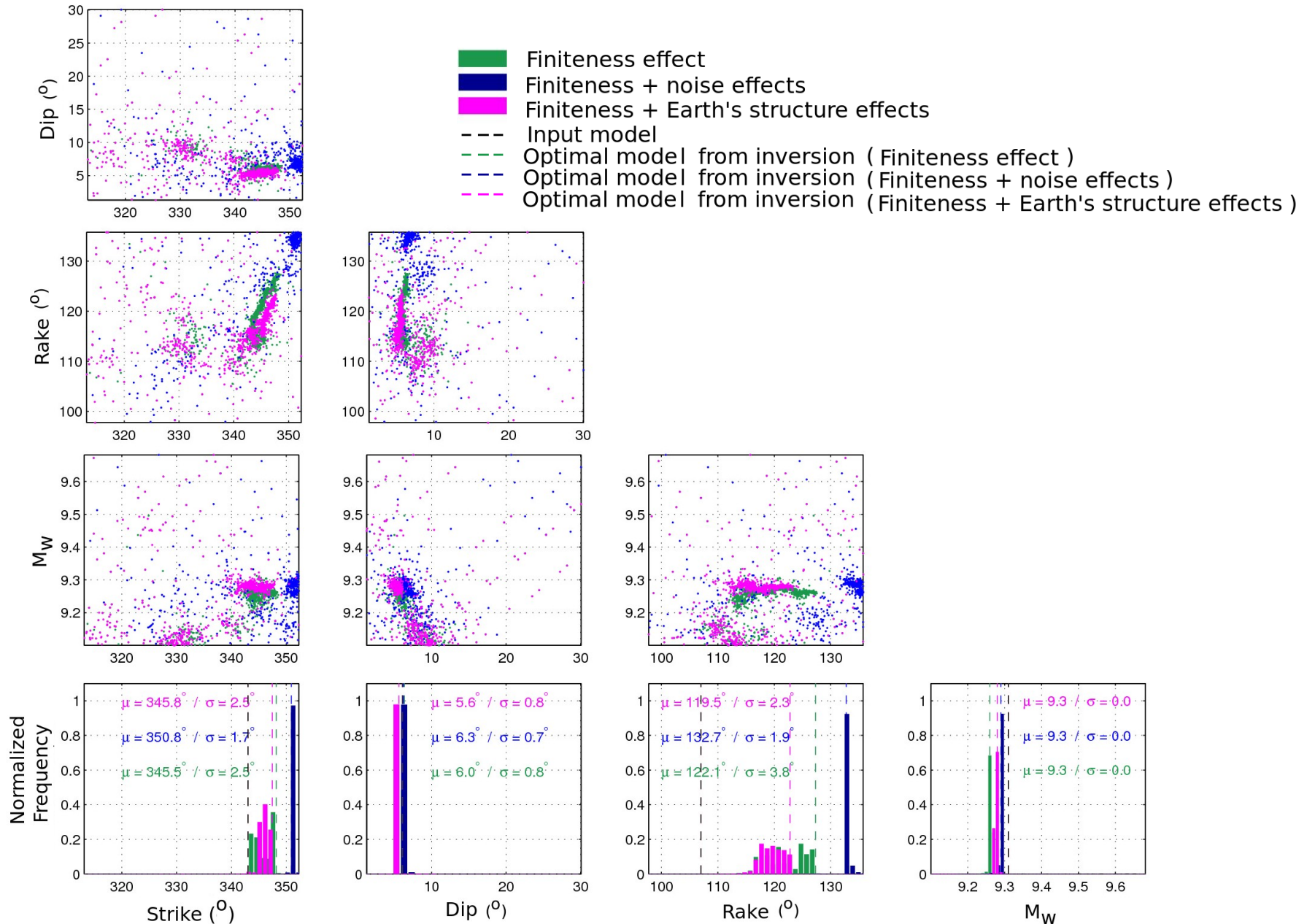
Combined effect of finiteness
and noise in synthetic data



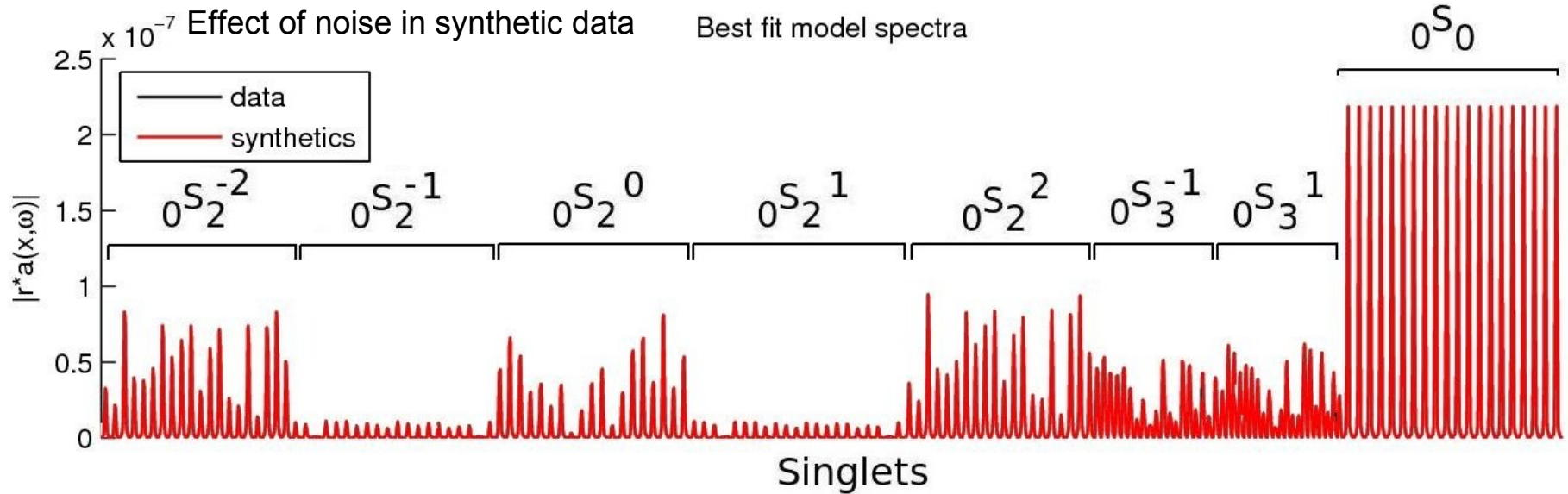
	$\varphi(^{\circ})$	$\delta(^{\circ})$	Multiplets $\lambda(^{\circ})$	M_w	T_r (s)	L (km)
Input model	343.00	6.10	107.00	9.31	545.00	1140.00
Optimal model	350.94	6.25	132.78	9.29		
Acceptable range	330.59-352.96	5.17-9.45	109.23-136.91	9.16-9.31		
Min. misfit: 0.0561						

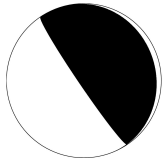
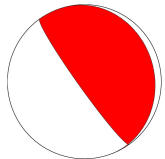


Synthetic tests (Sumatra 2004 M_w 9.3 based on model of Tsai et al.(2005))



Synthetic tests (Sumatra 2004 M_w 9.3 based on model of Tsai et al.(2005))

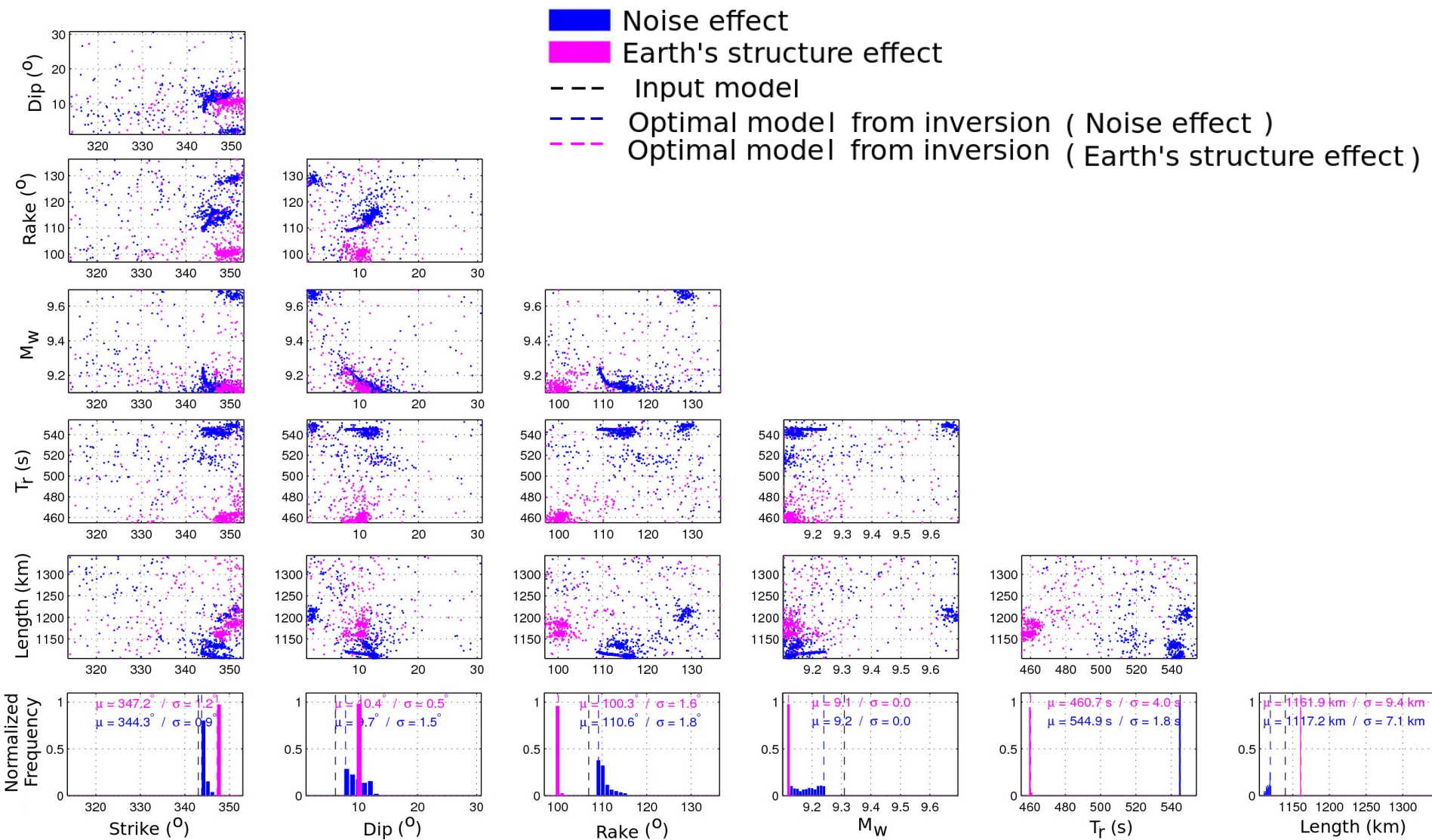


	$\varphi(^{\circ})$	$\delta(^{\circ})$	$\lambda(^{\circ})$	M_w	T_r (s)	L (km)	
Input model	343.00	6.10	107.00	9.31	545.00	1140.00	
Optimal model	343.76	7.82	109.17	9.24	544.97	1119.68	

Acceptable range 343.73-344.18 7.82-9.81 109.15-110.17 9.18-9.24 544.79-545.28 1116.28-1120.20

Min. misfit: 0.0000145

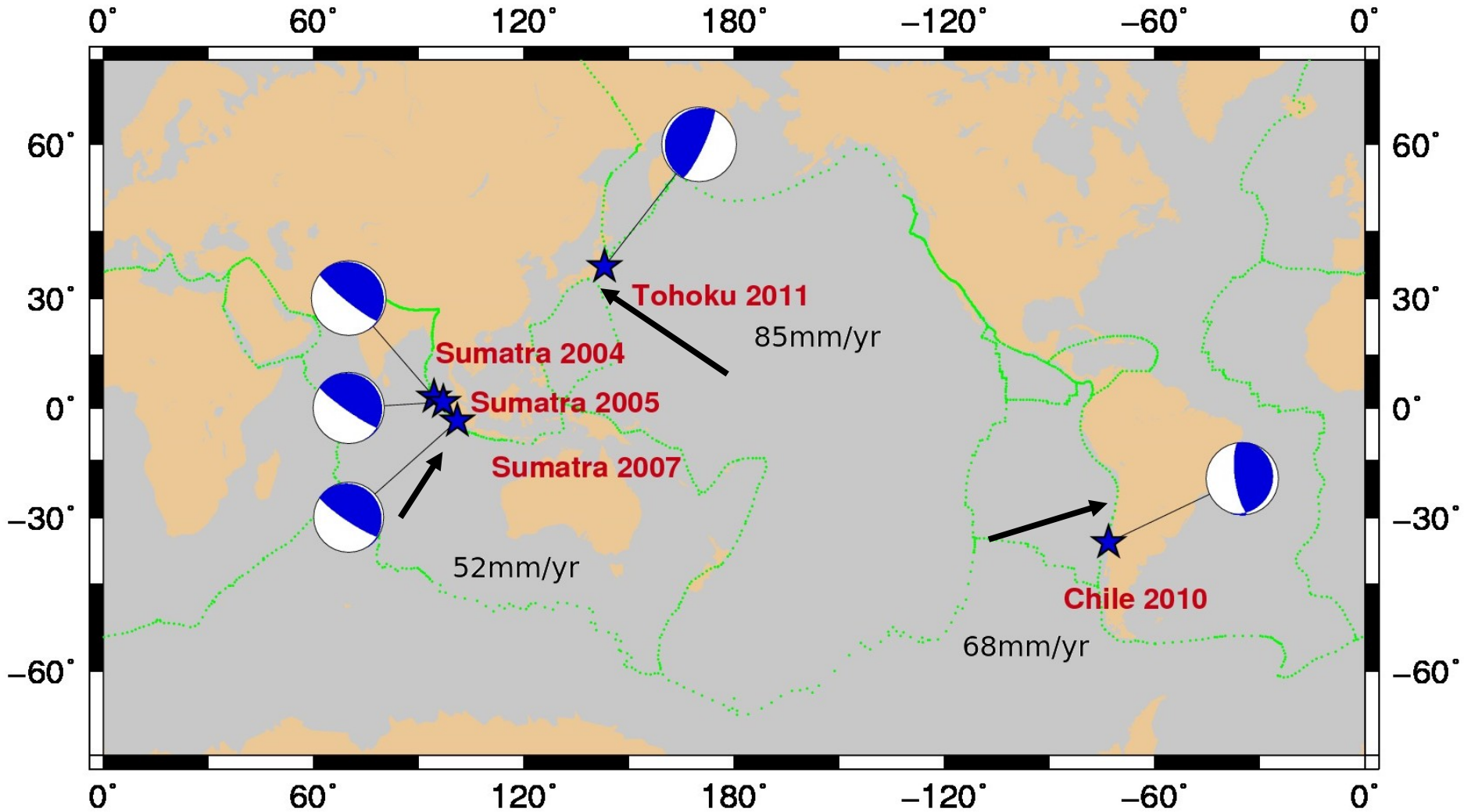
Synthetic tests (Sumatra 2004 M_w 9.3 based on model of Tsai et al.(2005))



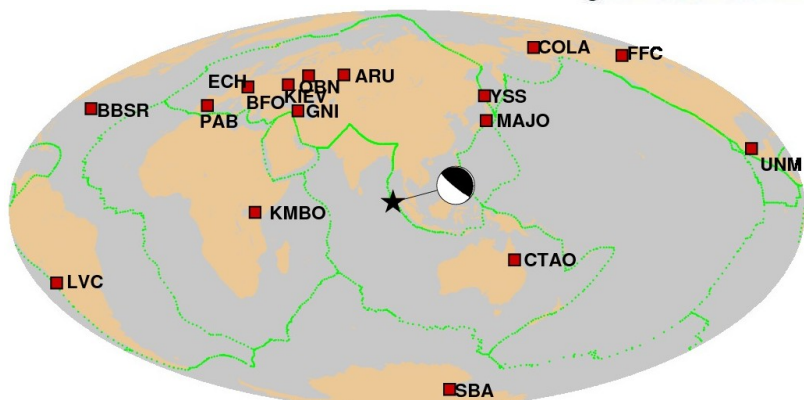
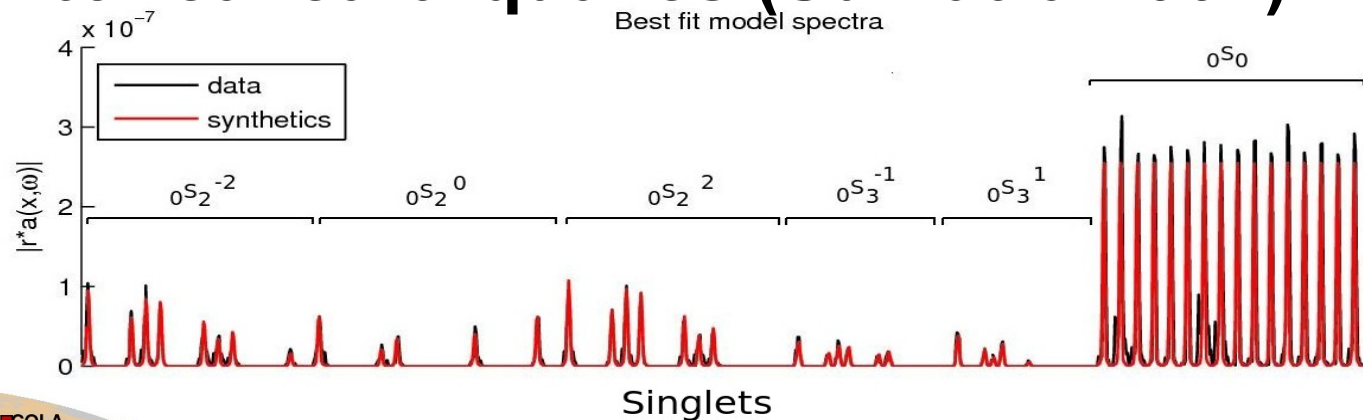
Synthetic tests

- Errors due to the neglecting of the finiteness of the source affect gradually the rake angle (up to 20°) with respect to rupture dimensions.
- Up to 8° error in fault geometry because of noise in data.
- Up to 150s error in rupture time because of Earth structure effect.
- Large location errors (1°) can yield large errors in rake angle (up to 14°).
- The rake angle is difficult to be constrained.
- Surprisingly the M_0 - δ trade-off is relatively well resolved.

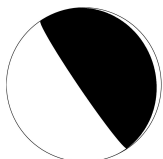
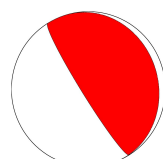
Application to real earthquakes



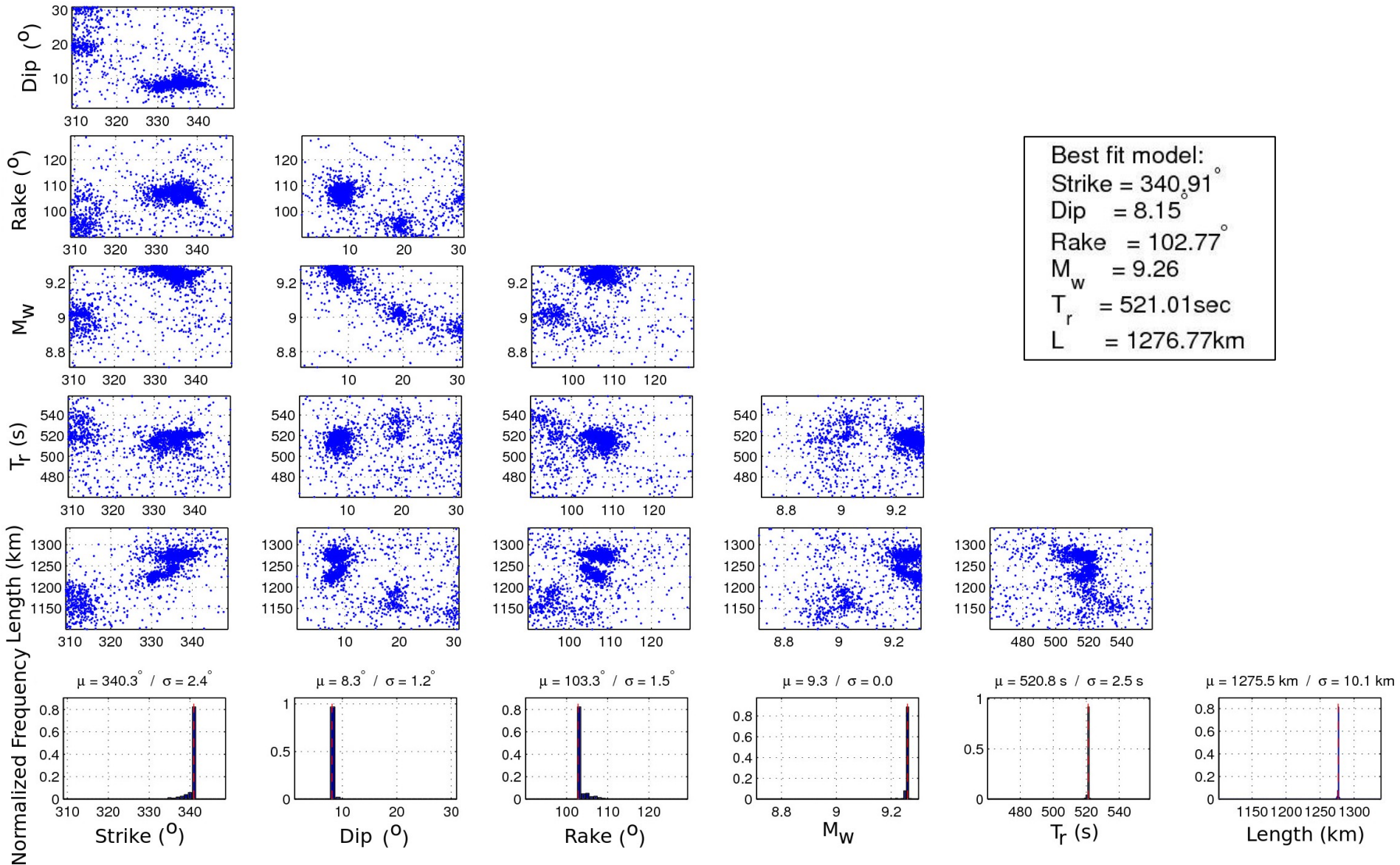
Application to real earthquakes (Sumatra 2004)



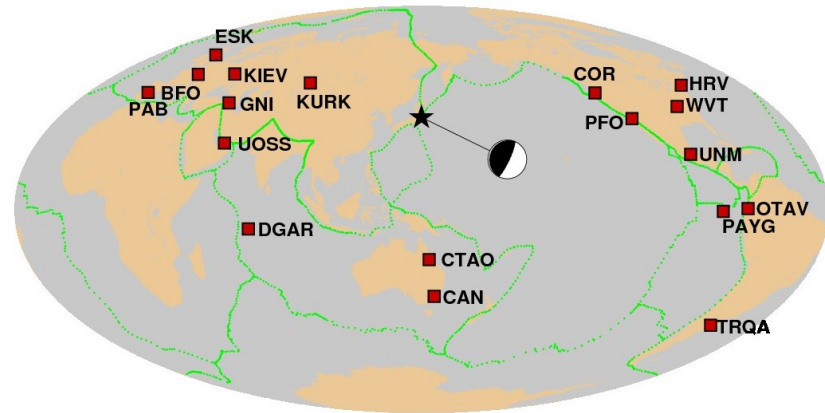
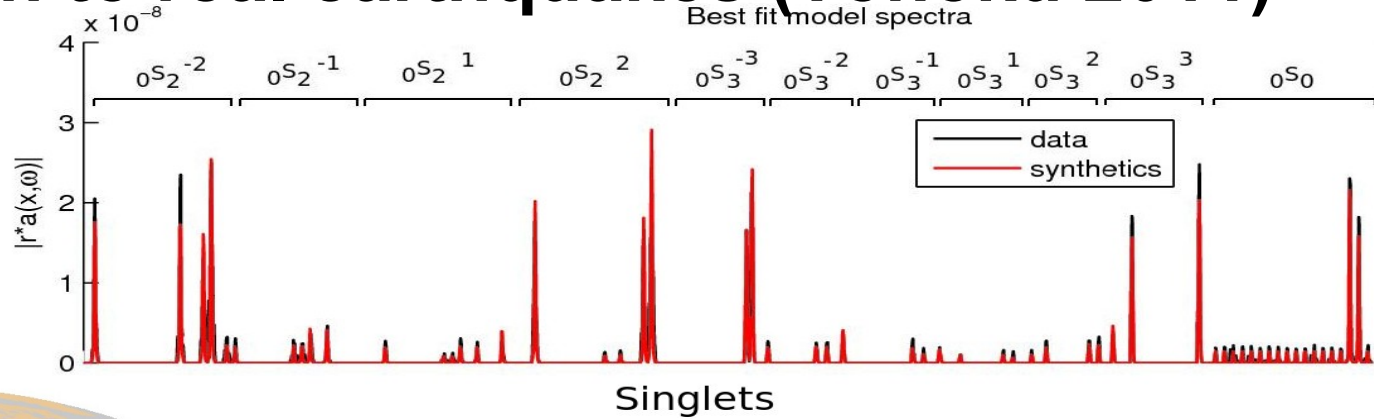
Min. misfit: 0.2463

	$\phi(^{\circ})$	$\delta(^{\circ})$	$\lambda(^{\circ})$	M_w	T_r (s)	L (km)	
Tsai et al. (2005)	343.00	6.10	107.00	9.31	545.00	1140.00	
Optimal model	340.91	8.15	102.77	9.26	521.01	1276.77	
Acceptable range	309.02-346.77	6.92-30.35	90.50-115.70	8.92-9.30	480.08-544.33	1122.63-1322.51	

Application to real earthquakes (Sumatra 2004)



Application to real earthquakes (Tohoku 2011)



$\varphi(^{\circ})$ $\delta(^{\circ})$ $\lambda(^{\circ})$ M_w T_r (s) L (km)

GCMT

203.00

10.00

88.00

9.10

T_r (s)

150.95

L (km)

461.01

Optimal model

197.32

9.11

79.33

9.00

Acceptable range

189.06-209.14

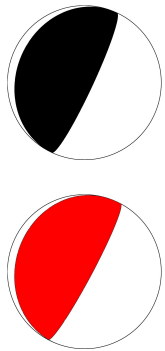
8.96-19.78

68.17-102.18

8.80-9.00

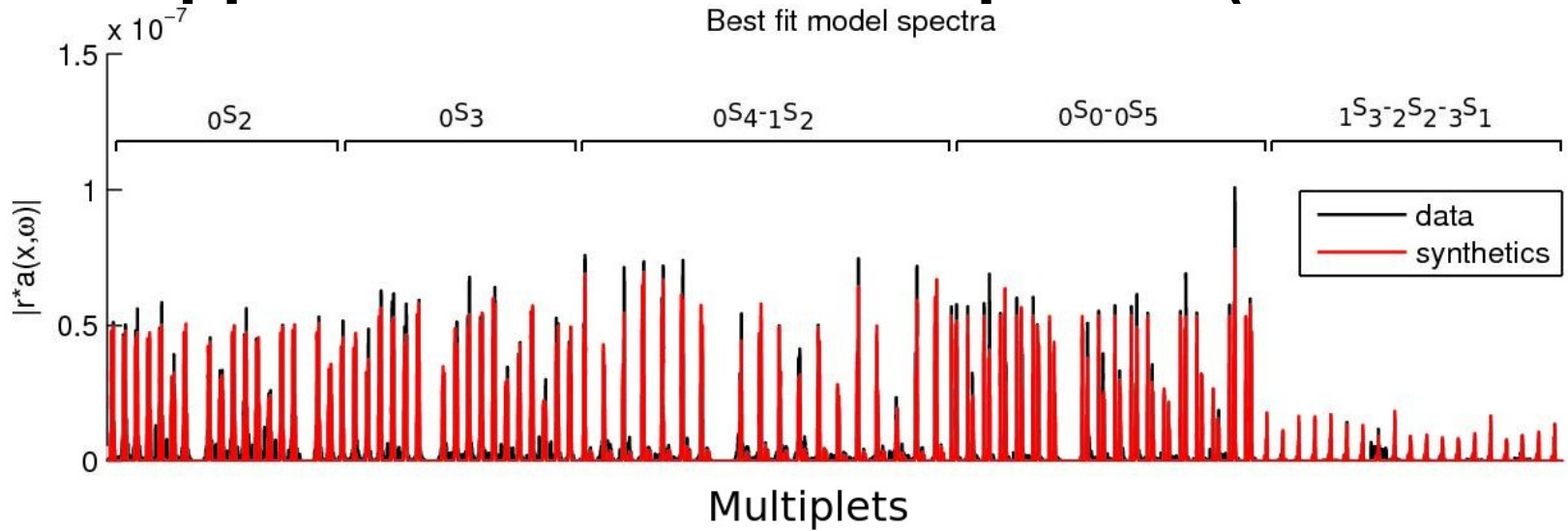
133.47-197.22

448.49-559.03

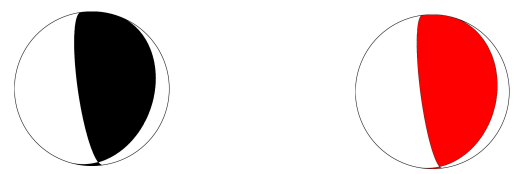
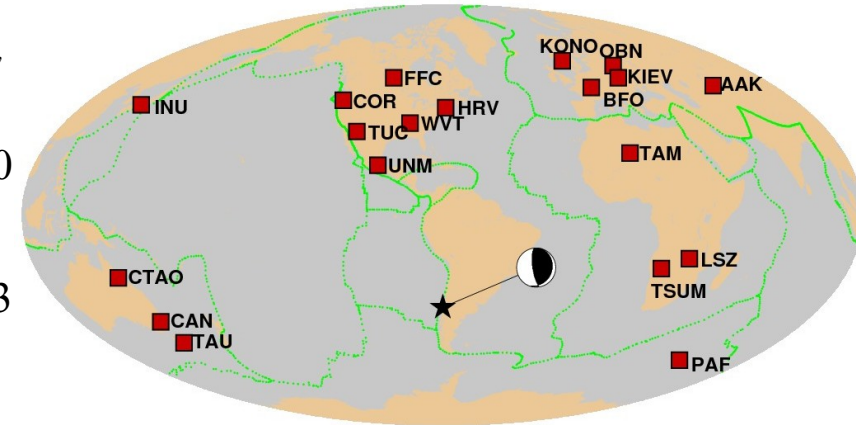


Application to real earthquakes (Chile 2010)

Best fit model spectra



	$\varphi(^{\circ})$	$\delta(^{\circ})$	$\lambda(^{\circ})$	M_w
GCMT	19.00	18.00	116.00	8.80
Optimal model	13.59	14.83	110.45	8.83
Acceptable range	8.55-20.40	11.99-21.92	109.02-119.44	8.74-8.89

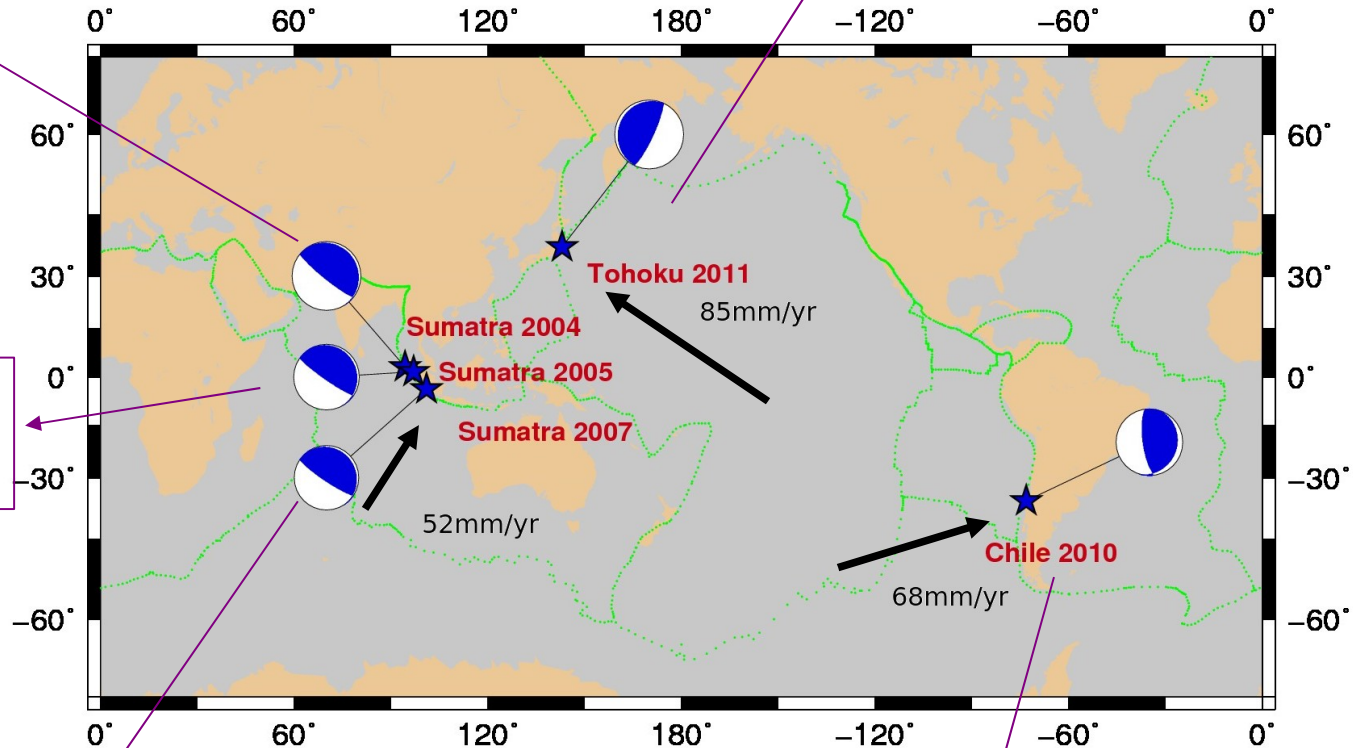


Min. misfit: 0.10344

Application to real earthquakes

$(\varphi, \delta, \lambda) = (341^\circ, 8^\circ, 103^\circ)$
 $(M_w, T_r, L) = (9.3, 521\text{s}, 1277\text{km})$

$(\varphi, \delta, \lambda) = (197^\circ, 9^\circ, 79^\circ)$
 $(M_w, T_r, L) = (9.0, 151\text{s}, 461\text{km})$



$(\varphi, \delta, \lambda) = (341^\circ, 9^\circ, 133^\circ)$
 $(M_w, T_r, L) = (8.7, -, -)$

$(\varphi, \delta, \lambda) = (330^\circ, 8^\circ, 112^\circ)$
 $(M_w, T_r, L) = (8.6, -, -)$

$(\varphi, \delta, \lambda) = (14^\circ, 15^\circ, 111^\circ)$
 $(M_w, T_r, L) = (8.8, -, -)$

Conclusions

- The neglect of finite rupture effects yields errors in rake gradually as the rupture dimensions (T_r , L) increase.
- Noise is not a significant source of errors in source parameters.
- The use of simplified 1D Earth model can lead to considerable errors in fault geometry (up to 8°) and large errors in rupture time (up to 150s) and length (up to 140km).
- Spatio-temporal location uncertainties yield considerable errors in rake angle (up to 14°) and rupture length (~ 190 km).
- We successfully determined simultaneously the fault geometry, moment magnitude and rupture characteristics of the giant 2004 Sumatra and 2011 Tohoku earthquakes.
- Normal mode data can offer an independent way to study large seismic sources and highlight bulk rupture characteristics.

Synthetic tests

$M_w = 9.31$
 $(T_r, L) = (545s, 1140km)$

$M_w = 8.1$
 $(T_r, L) = (90s, 240km)$

$M_w = 8.1$
 $(T_r, L) = (60s, 220km)$

$M_w = 8.8$
 $(T_r, L) = (230s, 600km)$

Point source inversion



SAW12D

SAW12D

SAW12D

SAW12D

$\Delta\phi^{(0)}$	-5.18	-0.36	0.33	-9.06
$\Delta\delta^{(0)}$	-0.26	2.46	-0.15	1.07
$\Delta\lambda^{(0)}$	-20.30	4.83	0.18	-9.28
ΔM_w	0.05	0.01	0.00	-0.02



misfit	0.05398	0.00065	0.00060	0.00876
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	SAW12D	PREM	PREM	SAW12D	PREM	PREM	SAW12D	PREM	PREM	SAW12D	PREM	PREM
	WN		WN	WN		WN	WN		WN	WN		WN

$\Delta\phi(^{\circ})$	-0.76	-4.20	-8.81	-0.70	2.16	1.47	2.86	-5.38	-14.33	-0.07	-1.64	-1.44
$\Delta\delta(^{\circ})$	-1.72	-4.29	-4.45	5.73	-0.89	4.26	-0.64	-0.86	-13.08	5.19	7.76	-10.88
$\Delta\lambda(^{\circ})$	-2.17	6.83	-8.02	7.98	-3.19	6.49	-6.97	0.11	6.50	1.29	-8.10	-3.10
ΔM_w	0.07	0.19	0.17	0.00	0.01	0.02	0.01	-0.00	-0.13	-0.09	-0.15	0.12
$\Delta T_r(s)$	0.03	84.59	84.69	-1.91	90.00	90.00	-1.44	60.00	60.00	-0.31	153.91	154.22
$\Delta L(km)$	20.32	-21.13	16.90	121.76	30.71	149.96	93.22	141.88	45.41	131.40	137.25	26.66









misfit	0.00002	0.01775	0.01777	0.00343	0.02256	0.02438	0.00071	0.01582	0.01990	0.00010	0.02093	0.02098
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	SAW12D	PREM	PREM	SAW12D	PREM	PREM	SAW12D	PREM	PREM	SAW12D	PREM	PREM
	WN		WN	WN		WN	WN		WN	WN		WN

$\Delta\phi(^{\circ})$	-7.94	-4.46	-8.11	-0.54	0.23	0.03	2.60	-3.30	0.62	-1.38	-7.35	-1.28
$\Delta\delta(^{\circ})$	-0.15	0.49	-4.86	1.79	3.25	5.19	9.58	1.13	12.67	4.71	2.02	-1.17
$\Delta\lambda(^{\circ})$	-25.78	-15.82	-23.06	3.89	5.56	7.54	7.83	-1.57	8.11	-3.05	-11.15	-5.00
ΔM_w	0.02	0.03	0.19	0.00	0.02	0.01	0.01	0.01	0.02	-0.07	-0.04	0.02



misfit	0.05416	0.05591	0.05609	0.02183	0.05126	0.07130	0.00669	0.02814	0.03401	0.00974	0.02604	0.02702
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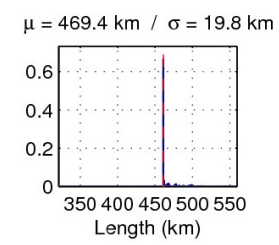
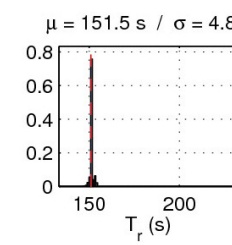
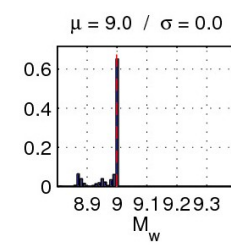
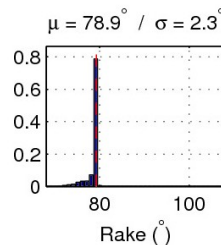
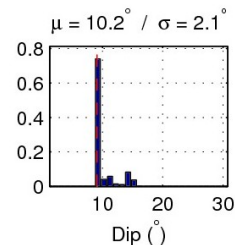
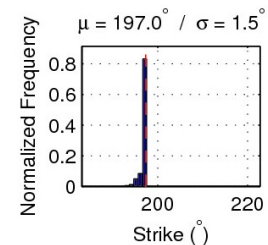
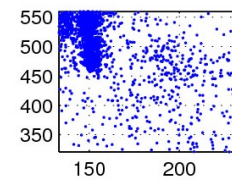
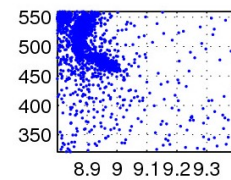
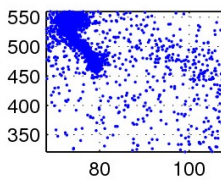
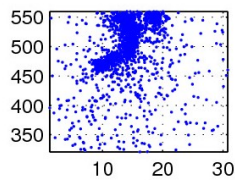
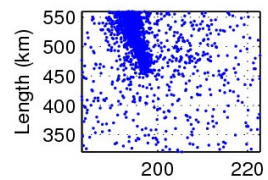
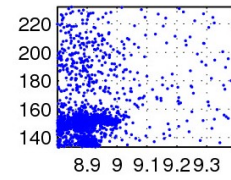
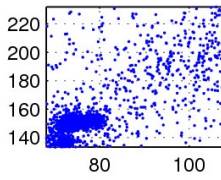
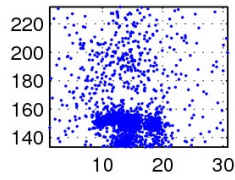
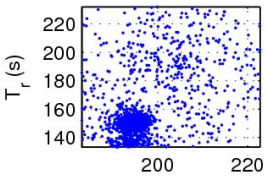
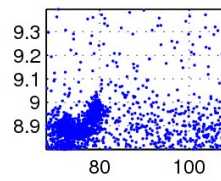
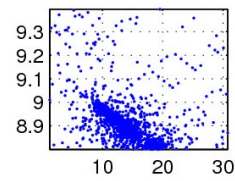
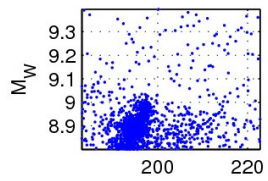
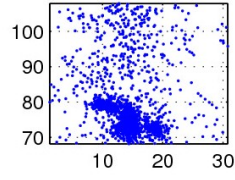
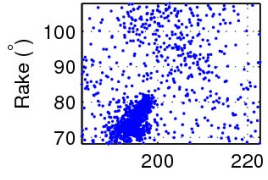
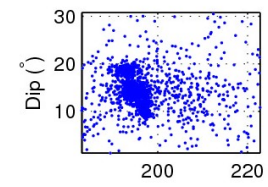
Error in origin time	+10 s	+0 s	+0 s	+0 s	+0 s	+10 s
Error in latitude	+0 ⁰ W	+0 ⁰ W	+1 ⁰ W	+0 ⁰ W	+1 ⁰ E	+0.60 ⁰ W
Error in longitude	+0 ⁰ S	+1 ⁰ S	+0 ⁰ S	+1 ⁰ N	+0 ⁰ S	+0.23 ⁰ N
	SAW12D	SAW12D	SAW12D	SAW12D	SAW12D	PREM WN
$\Delta\phi(^{\circ})$	-1.83	-5.52	3.45	5.80	-0.88	9.46
$\Delta\delta(^{\circ})$	0.05	4.34	1.4	-6.30	-3.18	-2.71
$\Delta\lambda(^{\circ})$	-2.47	-14.00	7.74	-10.58	-2.02	-4.54
ΔM_w	-0.01	-0.39	-0.07	0.21	0.12	0.12
$\Delta T_r(s)$	-7.96	0.12	0.23	0.62	-0.18	70.91
$\Delta L(km)$	-190.01	-196.32	6.20	-21.90	29.21	-192.97
						
misfit	0.00884	0.00016	0.00349	0.00030	0.00011	0.02209

		$\phi(^{\circ})$	$\Delta\phi(^{\circ})$	$\delta(^{\circ})$	$\Delta\delta(^{\circ})$	$\lambda(^{\circ})$	$\Delta\lambda(^{\circ})$	M_w	ΔM_w
GCMT		329.0	–	8.0	–	110.0	–	9.0	–
This study	GCMT location, ($h=28.6\text{km}$)	343.7	336.5–348.8	19.3	12.8–21.8	121.2	109.2–129.4	9.0	9.0–9.1
This study	GCMT location, ($h=10\text{km}$)	342.5	332.8–345.6	17.0	16.6–28.5	119.3	101.7–120.3	9.0	8.9–9.0
This study	Tsai et al. (2005) Centroid location	340.1	335.0–341.1	10.3	10.1–13.8	113.4	107.0–116.0	9.2	9.1–9.2

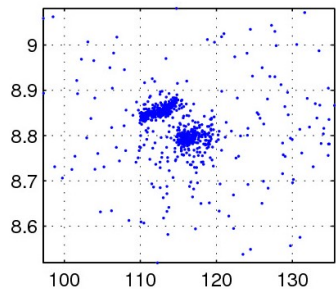
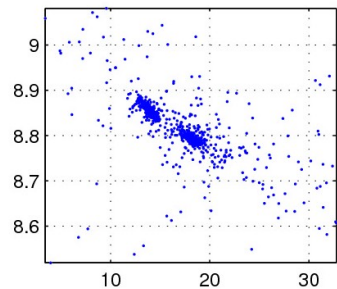
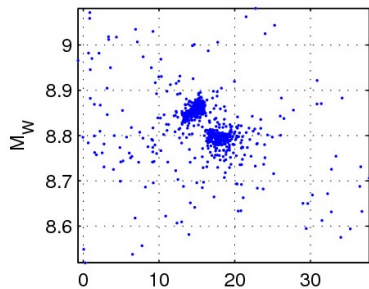
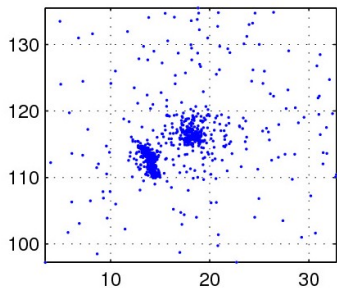
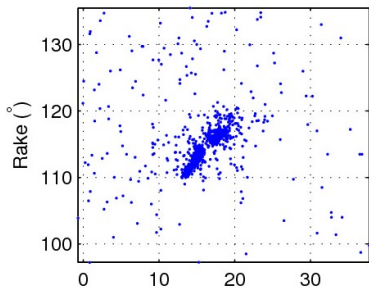
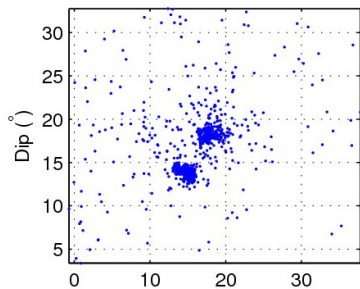
Application to real earthquakes

		$\phi(^{\circ})$	$\Delta\phi(^{\circ})$	$\delta(^{\circ})$	$\Delta\delta(^{\circ})$	$\lambda(^{\circ})$	$\Delta\lambda(^{\circ})$	M_w	ΔM_w	$T_r(s)$	$\Delta T_r(s)$	$L(km)$	$\Delta L(km)$
1	GCMT	329.0	–	8.0	–	110.0	–	9.0	–	–	–	–	–
	This study	343.7	336.5–348.8	19.3	12.8–21.8	121.2	109.2–129.4	9.0	9.0–9.1	–	–	–	–
	This study	340.9	309.0–346.8	8.2	6.9–30.4	102.8	90.5–115.7	9.3	8.9–9.3	521.0	480.1–544.3	1276.8	1122.6–1322.5
2	GCMT	203.0	–	10.0	–	88.0	–	9.1	–	–	–	–	–
	This study	202.1	195.5–202.7	9.6	7.1–11.1	98.2	91.5–98.7	9.1	9.0–9.1	–	–	–	–
	This study	197.3	189.1–209.1	9.1	9.0–19.8	79.3	68.2–102.2	9.0	8.8–9.0	151.0	133.5–197.2	461.0	448.5–559.0
3	GCMT	19.0	–	18.0	–	116.0	–	8.8	–	–	–	–	–
	This study	13.6	8.6–20.0	14.8	12.0–21.9	110.5	109.0–119.4	8.8	8.7–8.9	–	–	–	–
4	GCMT	333.0	–	8.0	–	118.0	–	8.6	–	–	–	–	–
	This study	341.0	334.7–341.8	9.4	6.2–13.8	132.8	122.8–133.2	8.7	8.5–8.7	–	–	–	–
5	GCMT	328.0	–	9.0	–	114.0	–	8.5	–	–	–	–	–
	This study	329.6	321.1–333.8	8.1	7.7–19.3	111.7	97.6–116.7	8.6	8.3–8.6	–	–	–	–

1. Sumatra 2004
2. Tohoku 2011
3. Chile 2010
4. Sumatra 2005
5. Sumatra 2007



Best fit model:
 Strike = 197.32°
 Dip = 9.11°
 Rake = 79.33°
 $M_w = 9.00$
 $T_r = 150.95\text{sec}$
 $L = 461.01\text{km}$



Best fit model:
 Strike = 13.59°
 Dip = 14.83°
 Rake = 110.45°
 $M_w = 8.83$

