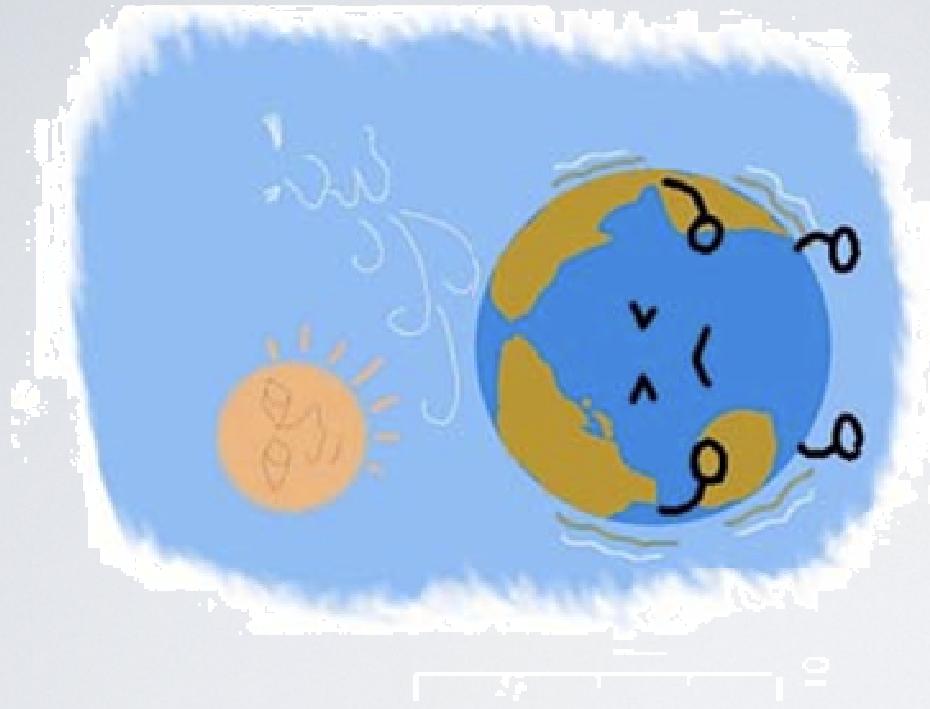


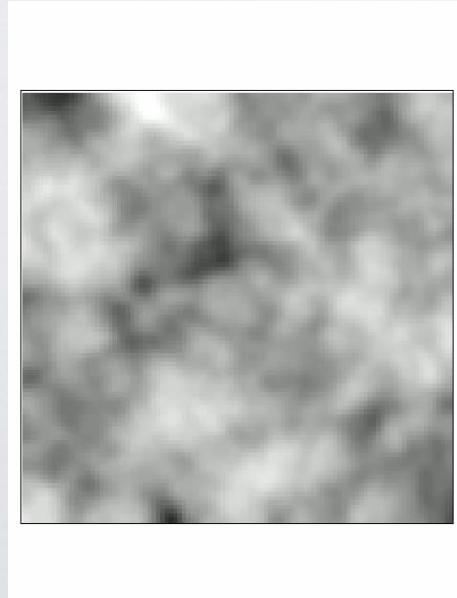
# Earth's background free oscillations



Kiwamu Nishida,  
Earthquake Research Institute,  
University of Tokyo

# Background wavefield

Persistent excitation by  
distributed sources



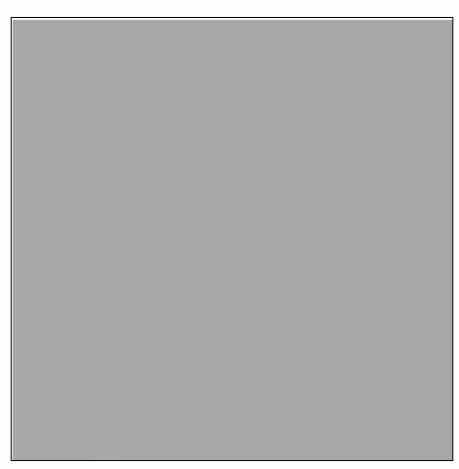
Global

Local, regional  
(Japan, California, Europe, etc)

Seismic  
hum

microseisms

Transient by an event

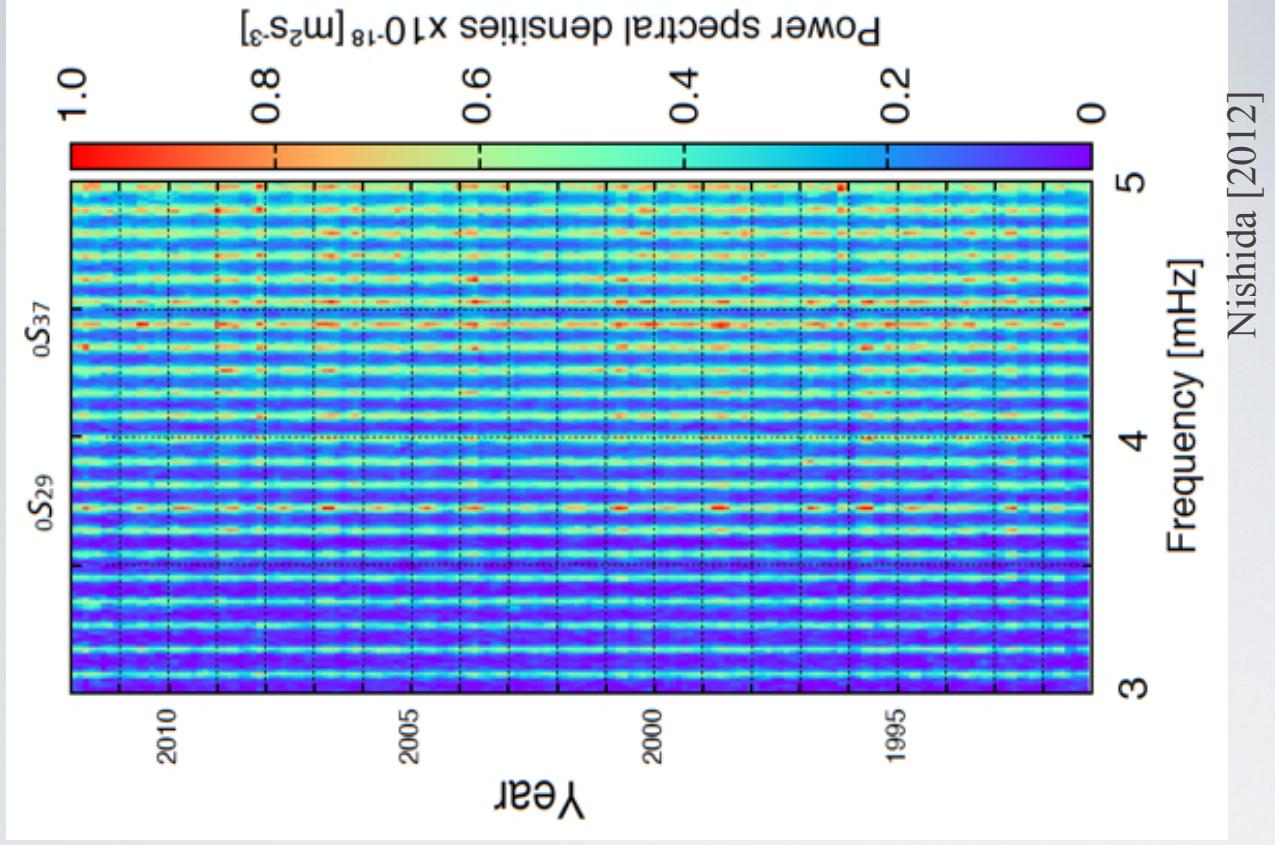


Earthquake



Global body wave propagation

# Discovery of Earth's background free oscillations (seismic hum) [1998]



- Persistent excitation of **fundamental** spheroidal modes from 2 to 20 mHz
- Annual variations of their amplitudes
- Acoustic resonance: atmospheric turbulence

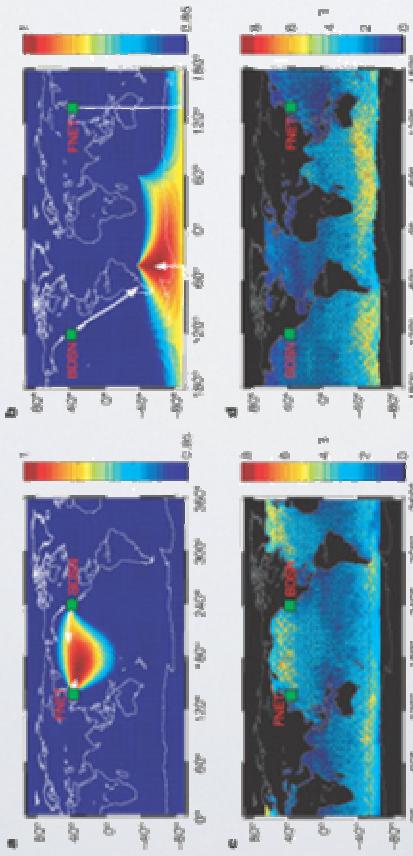
# Source distribution

- Strong excitation: Oceanic infragravity waves

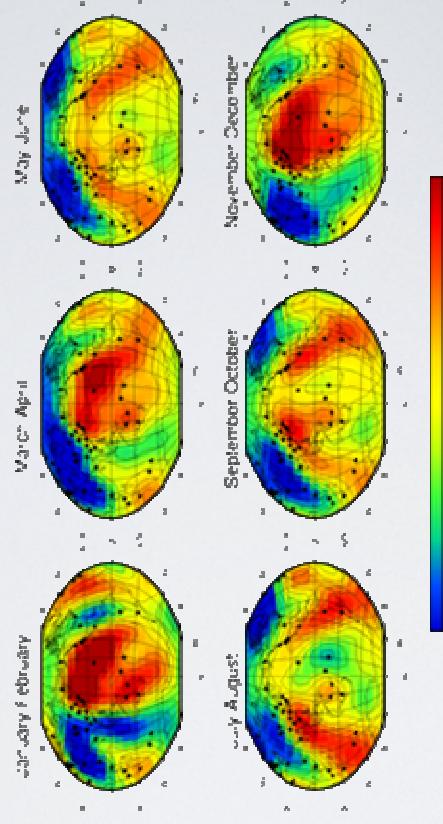
- In the north Pacific in winter

- In the southern hemisphere in summer

(1) Array observation



(2) Modeling of cross spectra

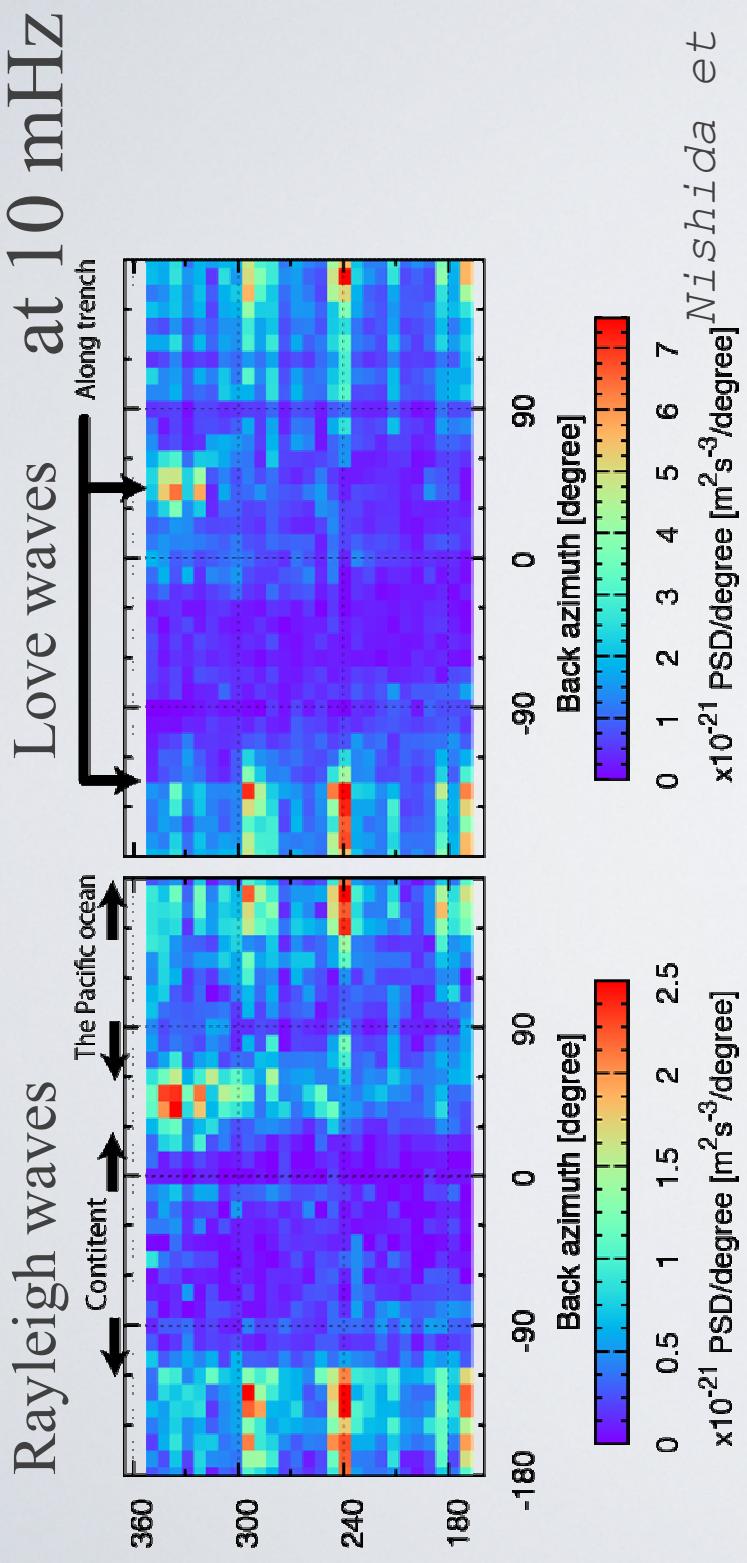


Rhie and Romonowicz [2004]

Nishida and Fukao [2007]

Pressure sources are dominant.

# Discovery of horizontal hum



Love wave amplitudes  $\sim 3 \times$  Rayleigh wave amplitudes (10-100 mHz)

Similar azimuthal patterns

Background Love waves from 3 to 5 mHz Kurrle and Widmer (2008)

Random shear traction on the seafloor

# Origins of seismic hum

Acoustic resonance

<5mHz

>5mHz

$$\sqrt{g}$$

infragravity waves

|| Love and Rayleigh wave ||

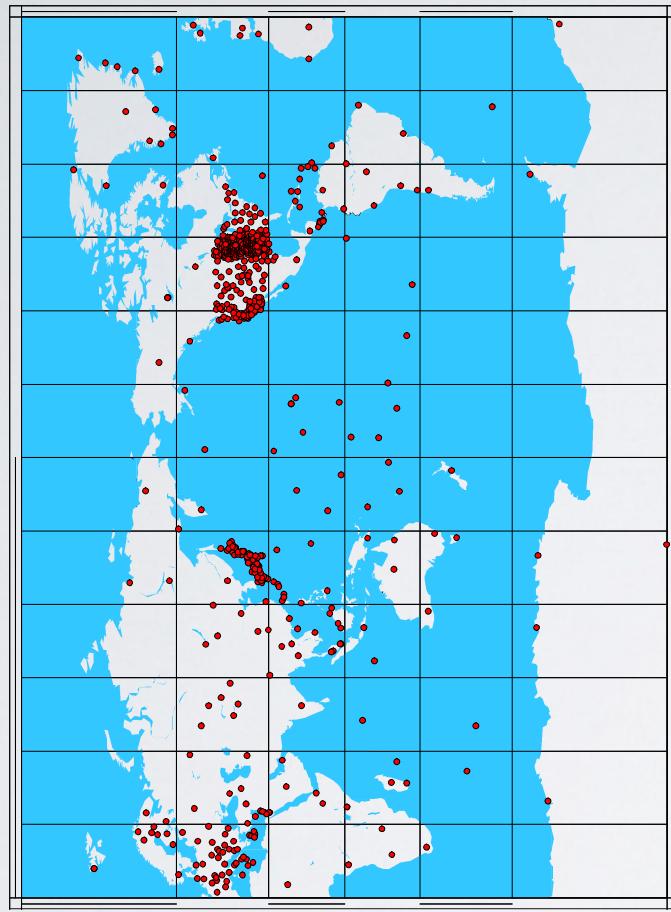
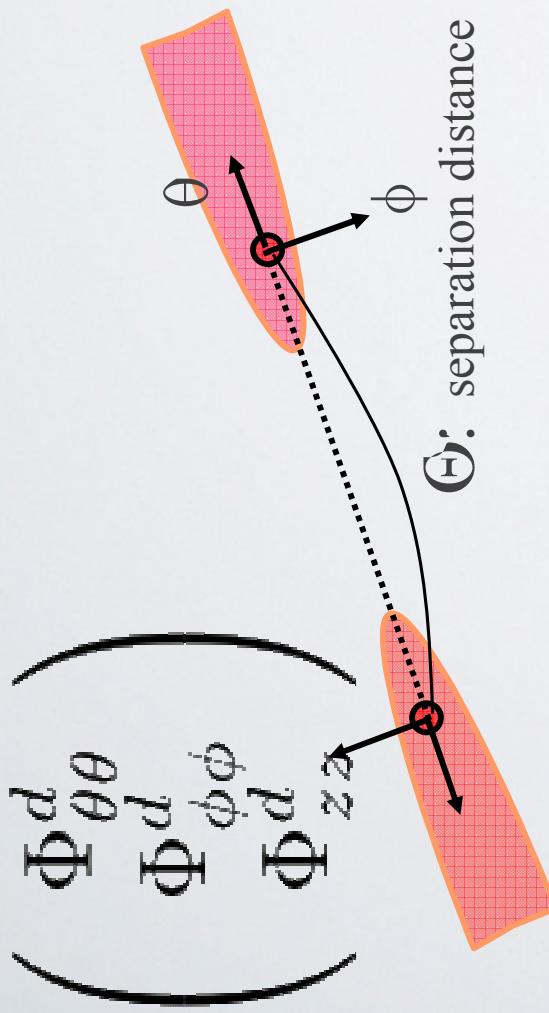
Abyssal plane: **Linear topographic coupling**

[Fukao et al., 2010; Saito, 2010]

Inference of the force system

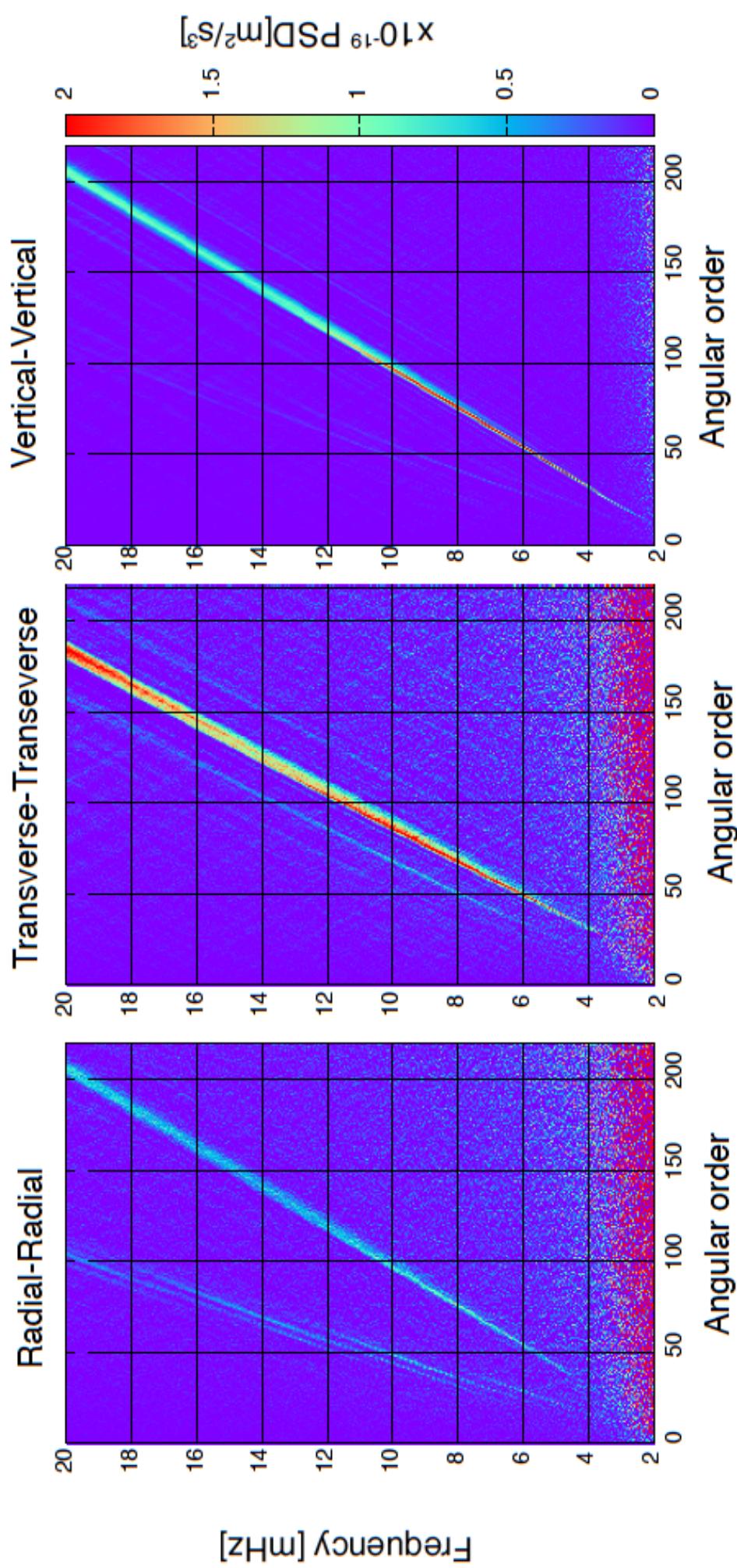
# Cross-correlation analysis: Data set

## Cross spectra



- Data: IRIS+ORFEUS+F-net STS1,2,2.5:  
658 stations 2004/1-2011/12
- Exclusion of noisy data and effects of large earthquakes
- CCFs: radial-radial, transverse-transverse, and vertical-  
vertical

# Wavenumber-frequency spectra



# Assumptions of sources

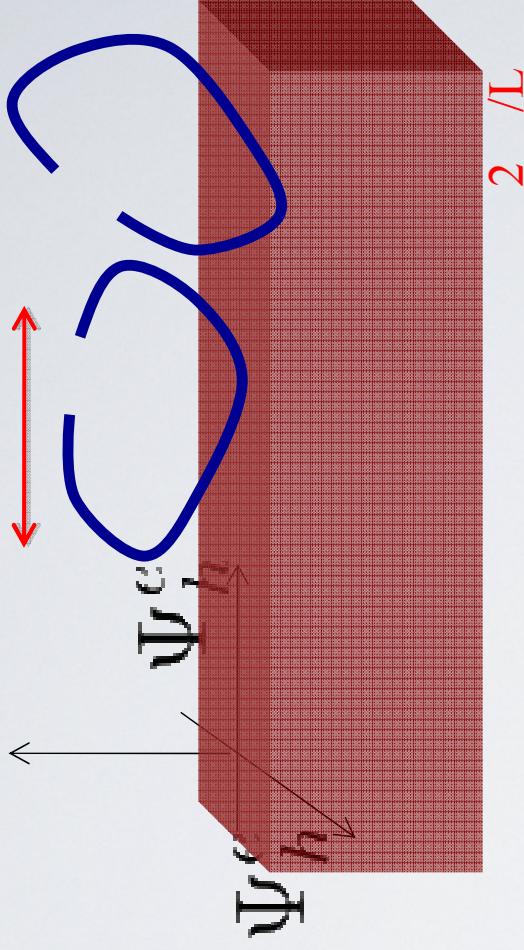
- Stochastic source parameters

• Power spectrum

• Correlation length L

- Correlation length L

$\Psi_r^{\epsilon}$

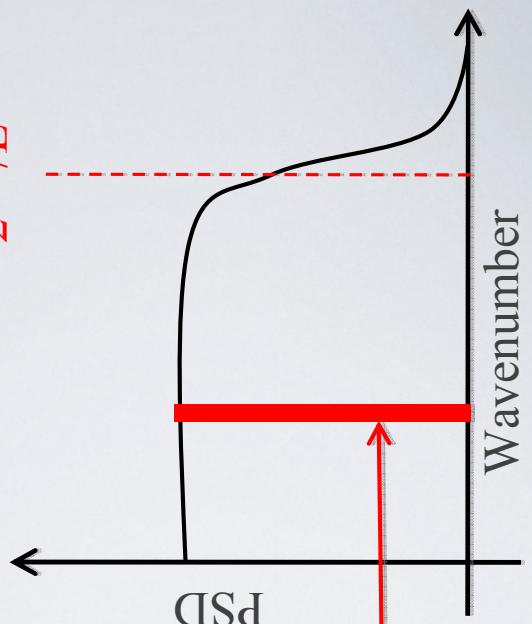


- Effective pressure and traction

$\Psi_r^{\epsilon}$  Effective pressure

$\Psi_h^{\epsilon}$  Effective traction

Power spectrum per  
unit wavenumber



# Inversion of source terms

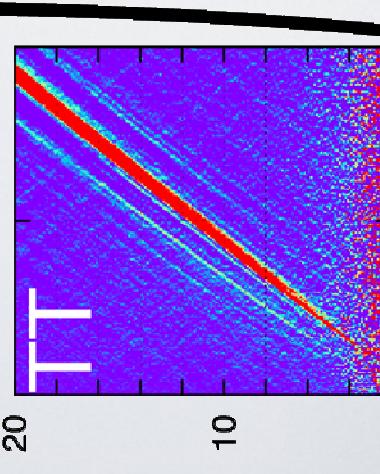
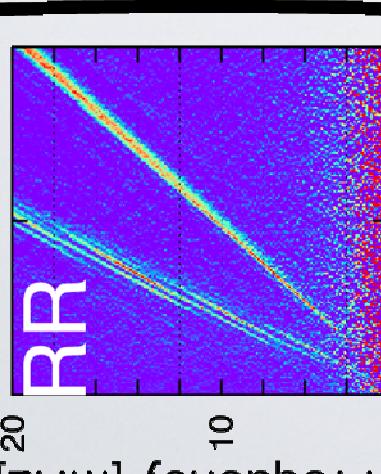
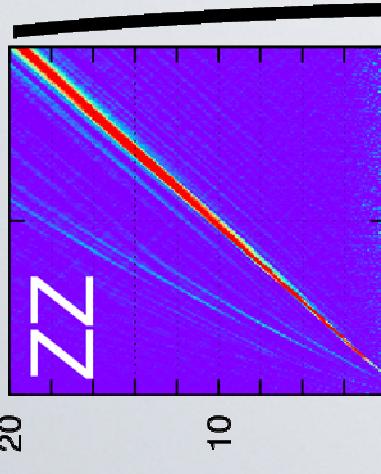
known  
Source

Spectra

(pressure)

(traction)

Kernel

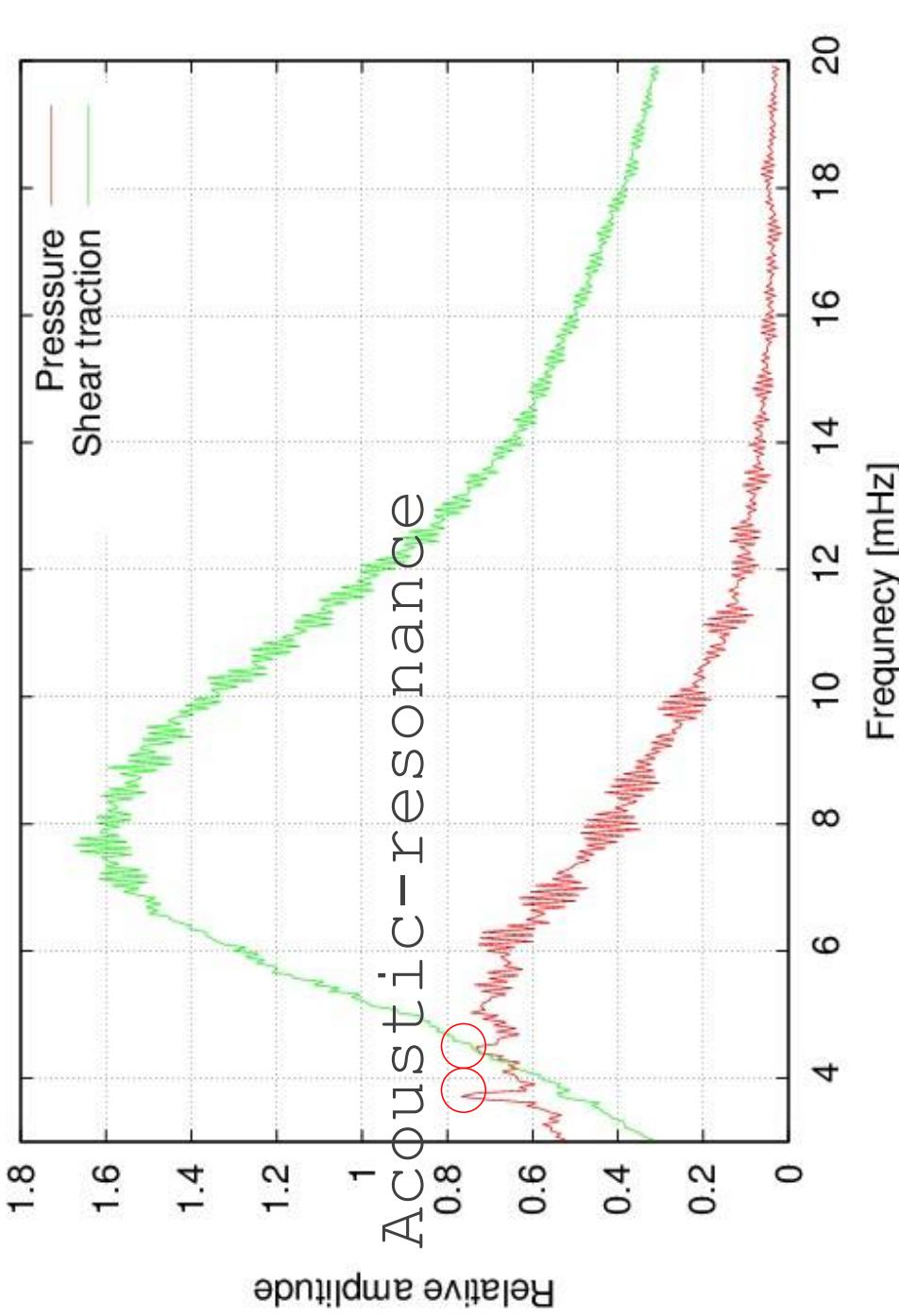


Angular order  
0 100 200 1000 2000

0 100 200 1000 2000

Frequency [MHz]

# Estimated source spectra

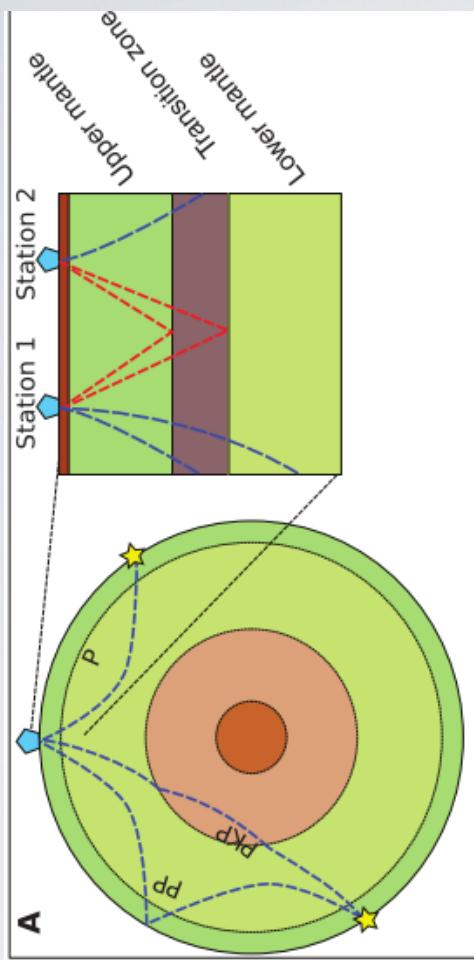


- Random shear traction: 5-20 mHz (a peak at 8 mHz)
- Pressure source: 2-5 mHz (a peak at 5 mHz)

# Body wave propagation

P410P, P660P, Poli *et al* 2012  
Core phases, Lin *et al* 2013

Lin *et al* 2013



Poli *et al* 2012

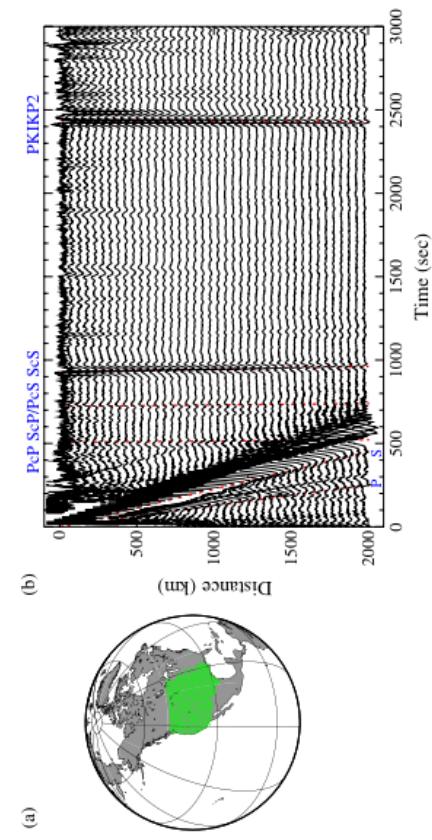
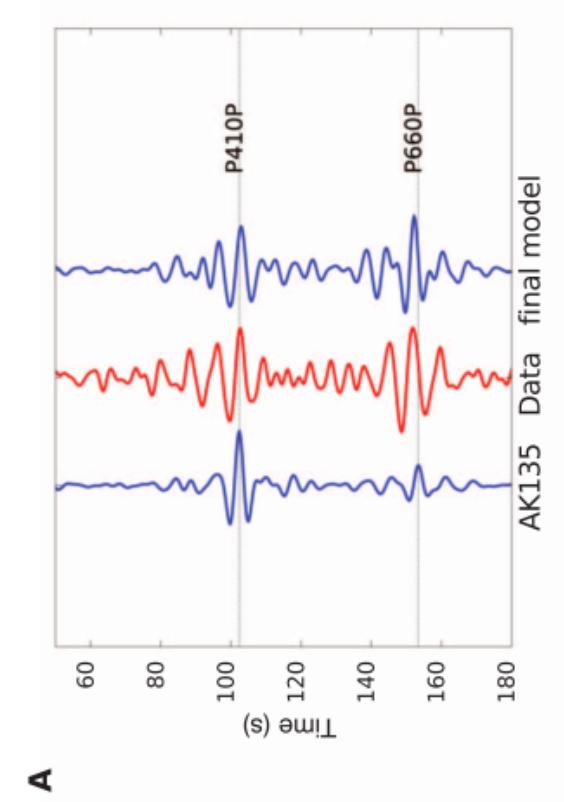
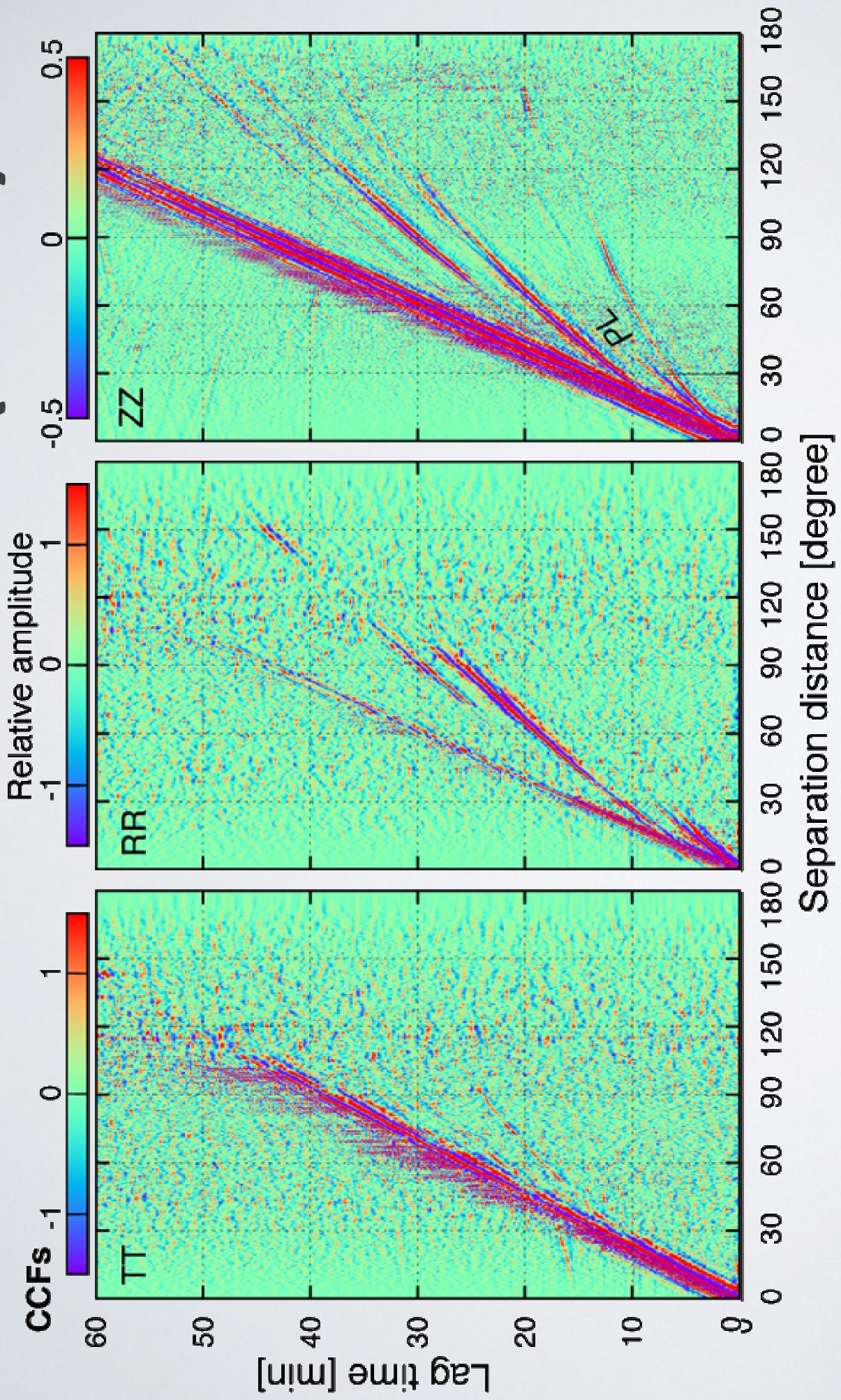


Figure 2. Stacked cross-correlations across USArray. (a) The USArray Transportable Array used in this study. Station locations are marked by green dots. (b) The observed broadband stacked cross-correlations sorted by distance. The red dashed lines mark the ray-predicted arrival times for core phases based on the iasp91 Earth model. Several observed body wave phases are indicated.

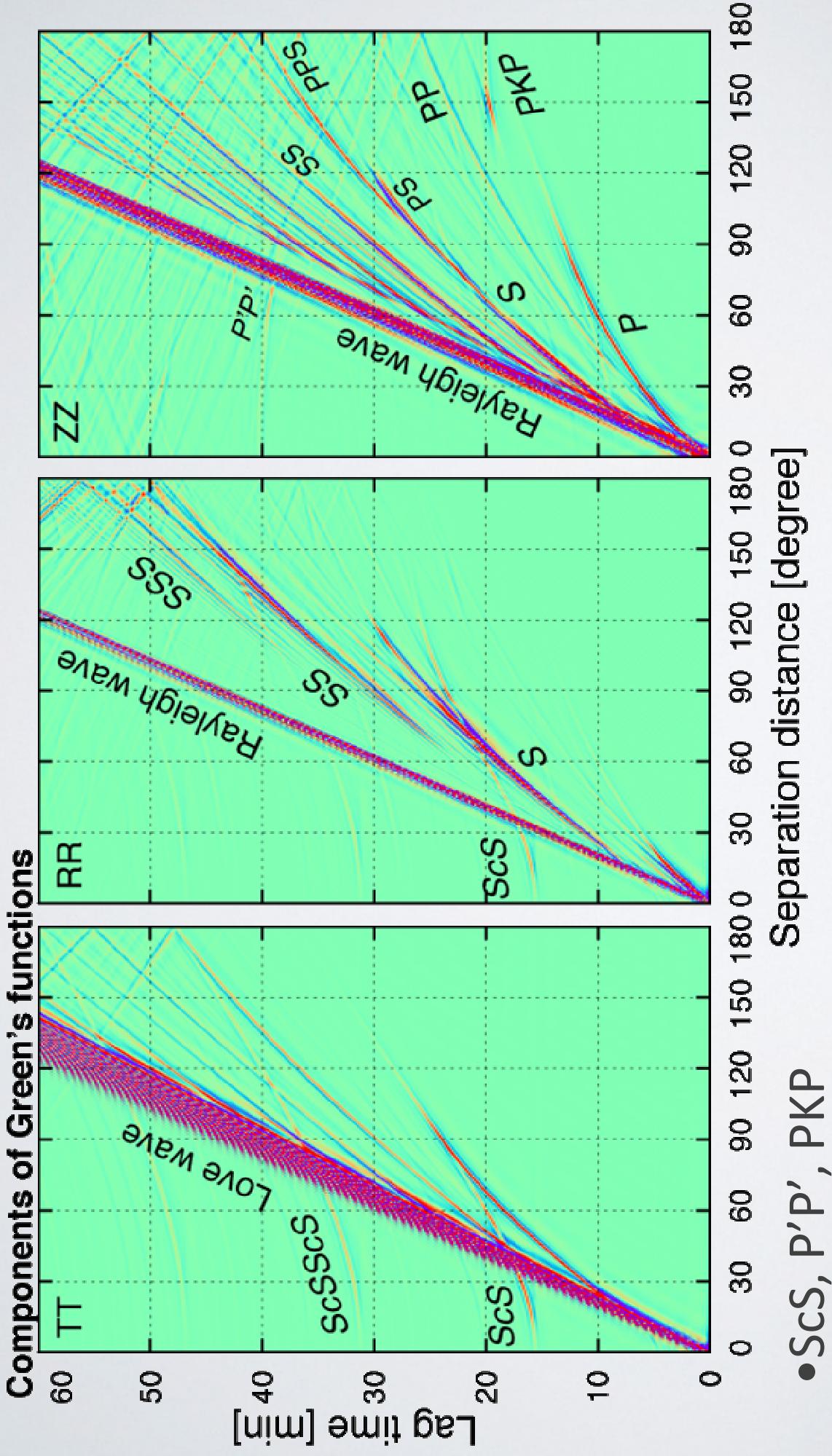


# TRAVEL TIME PLOTS (CCFS)



- Frequency range: 5-40 mHz
- Deconvolution by NLNM

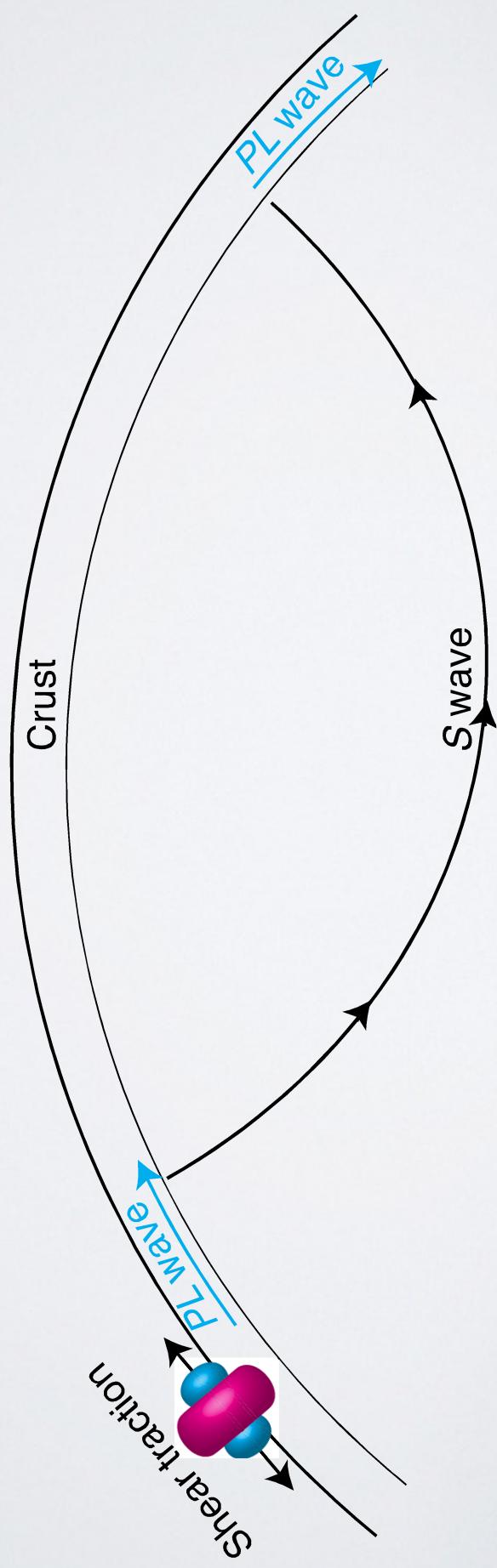
# Comparison of CCFs with Green's functions



- SCS, P'P', PKP
- Lack of reflection phases in observation
- Dominance of Shear-coupled PL (SPL) wave

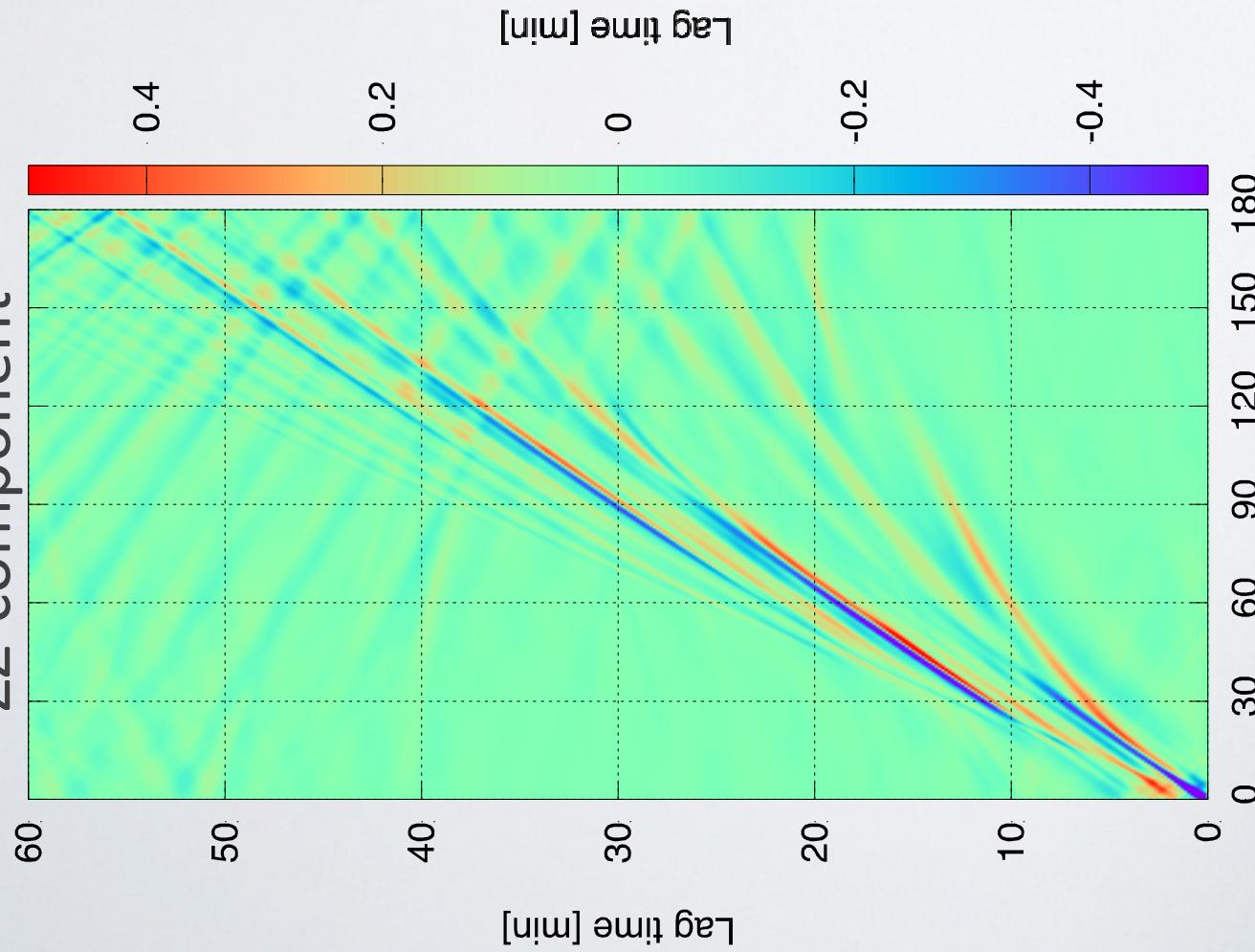
# Dominance of S<sub>L</sub> wave

The traction source radiates the strongest P<sub>L</sub> wave in the horizontal direction  
P<sub>L</sub> wave couples with S wave



# Synthetic seismograms

ZZ-component



0 10 20 30 40 50 60

Lag time [min]

Degree

0 30 60 90 120 150 180

Lag time [min]

0 10 20 30 40 50 60 90 120 150 180

-0.4

-0.2

0

0.2

0.4

# Conclusions

- Existence of background Love waves: from 3 mHz to 20 mHz
- Random surface traction is dominant above 5 mHz
- **Linear topographic coupling** on the ocean floor is the most probable excitation mechanism
- Below 5 mHz, additional pressure sources are needed
  - Atmospheric disturbances, and/or surf beat

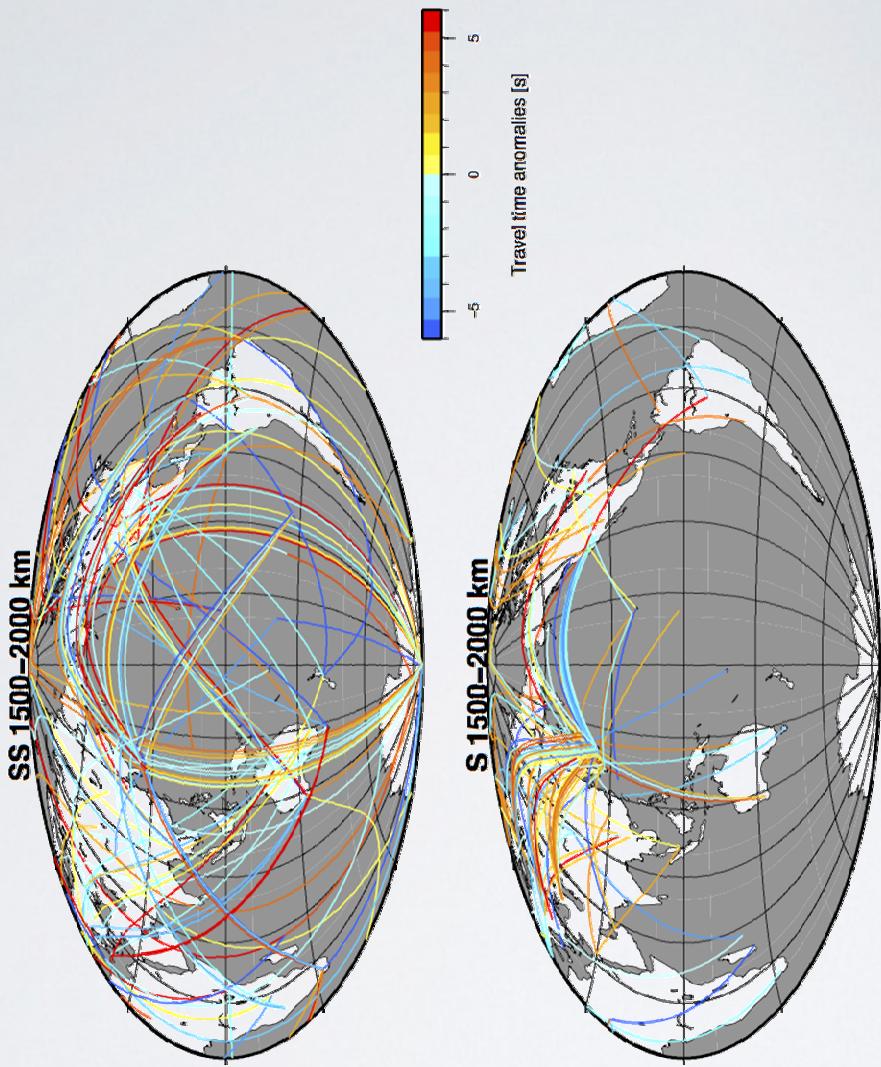
# Conclusions

- The CCFs show Global propagation of body waves
- Differences between the CCFs and the Green's functions
  - (1) The lack of reflection phases in the CCFs : surface excitation sources
  - (2) Dominance of SPL waves in the CCFs: shear-traction sources

End

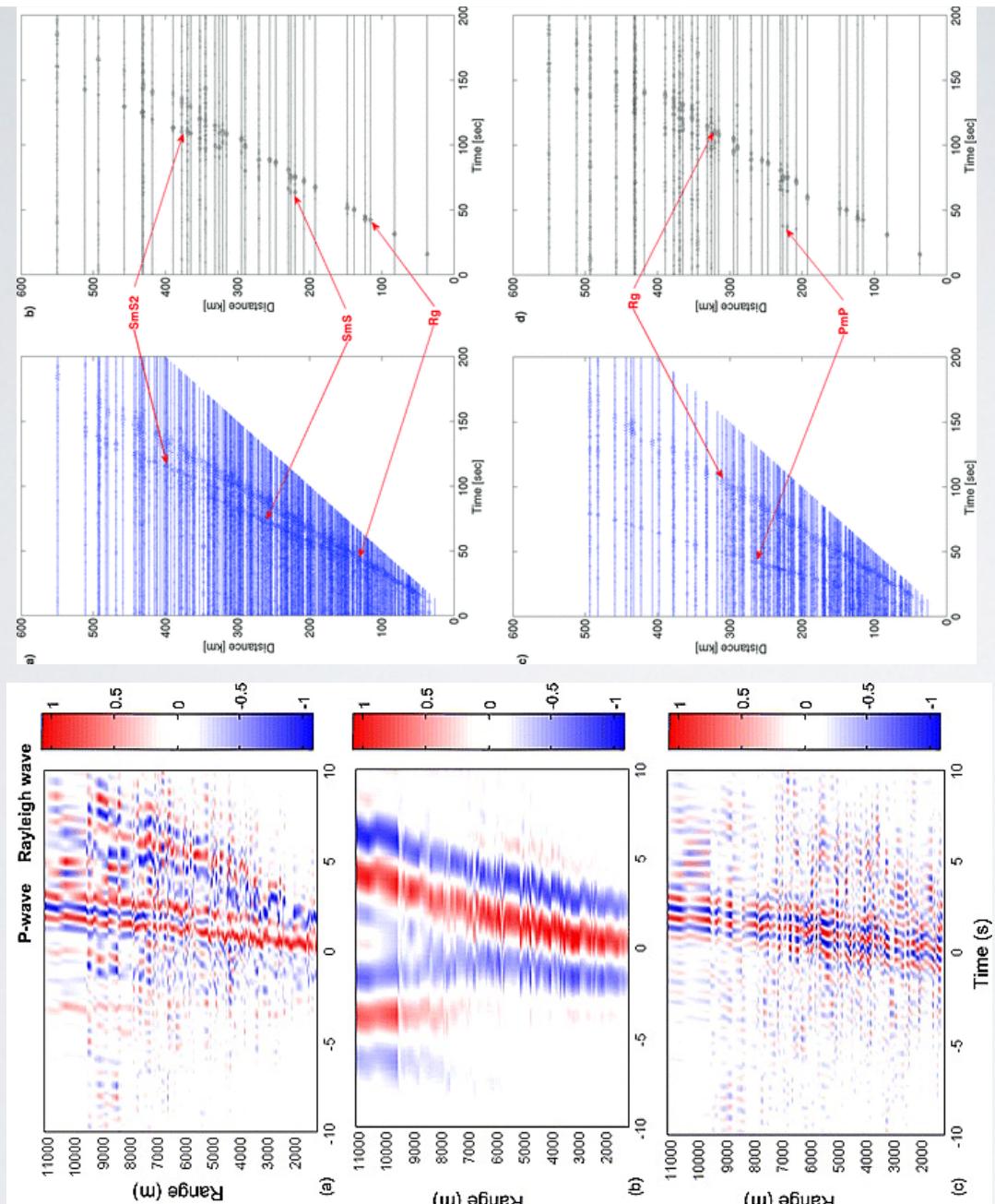
# Travel time anomalies (S and SS)

- S and SS waves: 5-30 mHz
- Phase difference between observation and synthetics
- Cross-correlation > 0.8



# Body wave propagation revealed by ambient noise

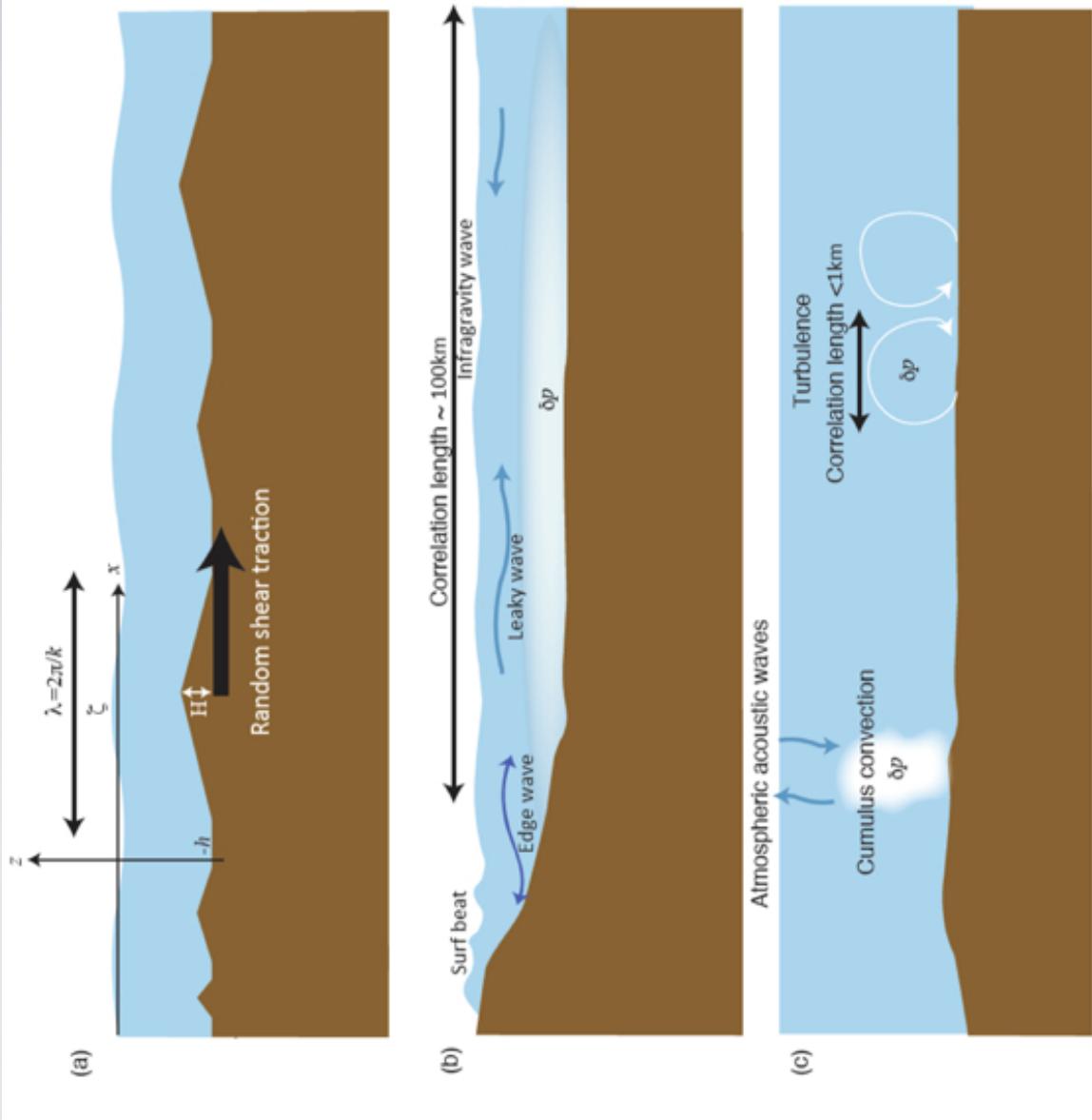
Local scale:  
e.g. Roux 2005  
Regional scale:  
e.g. Nishida *et al.*  
2008, Poli *et al.*  
2012  
High frequency ( $>0.5$   
Hz)



# Excitation mechanism of seismic hum

Abyssal plane:

- Linear topographic coupling [Fukao et al., 2010; Saito, 2010]

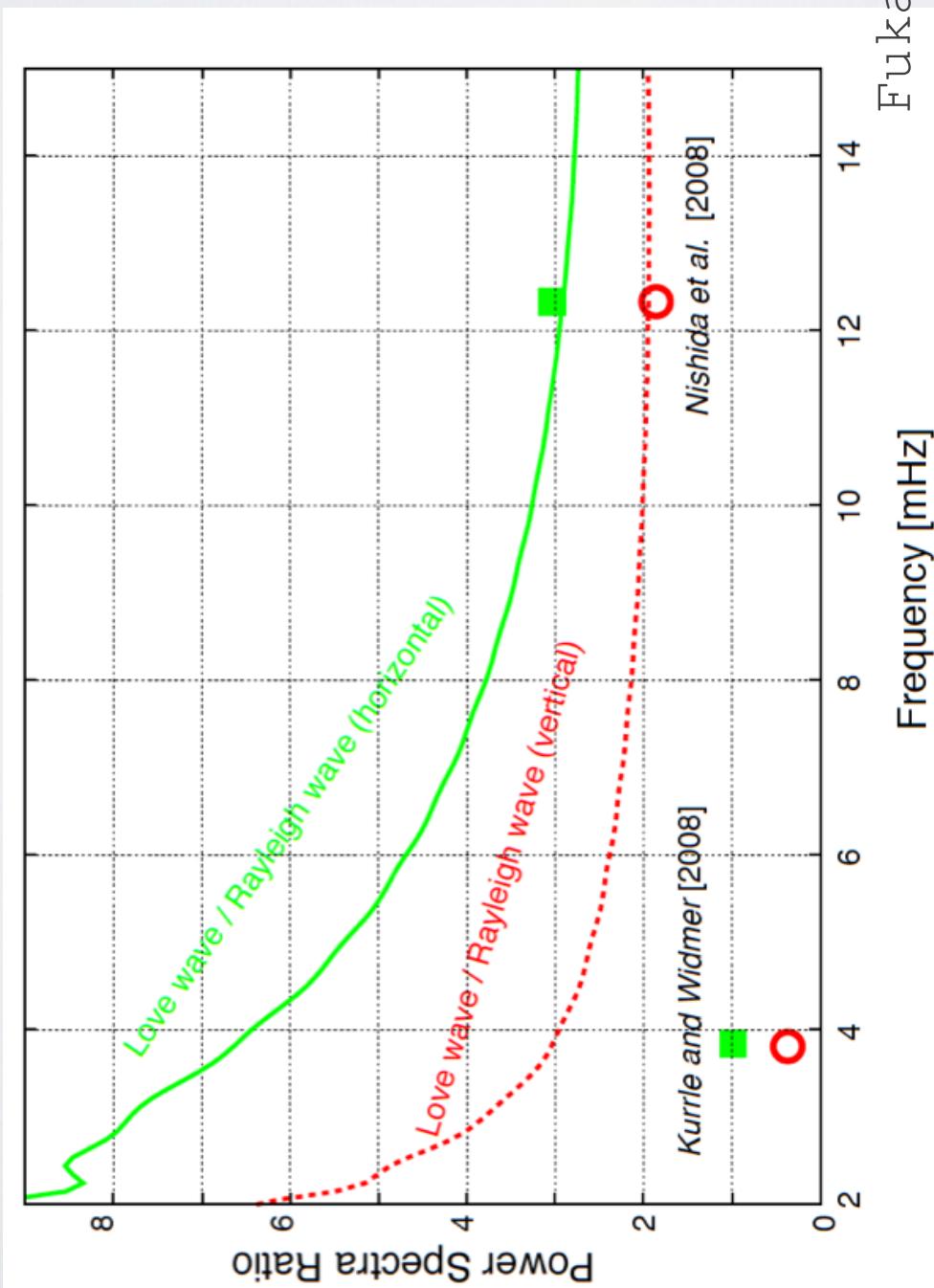


Along a continental shelf:

- Surf beat: Nonlinear interactions

# The purpose of this study

- Determination of amplitudes of toroidal modes below 10 mHz
- To elucidate the force system of the excitation sources



# Source distribution

- Source distribution

- (1) Array observation

- (2) Modeling of cross spectra

- Strong excitation

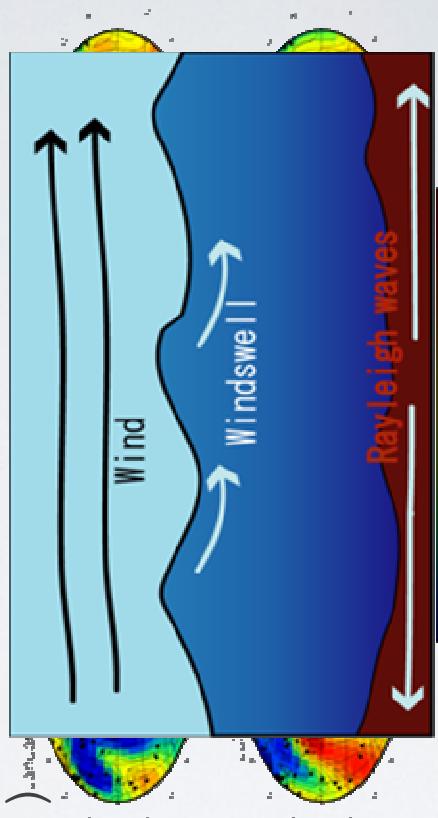
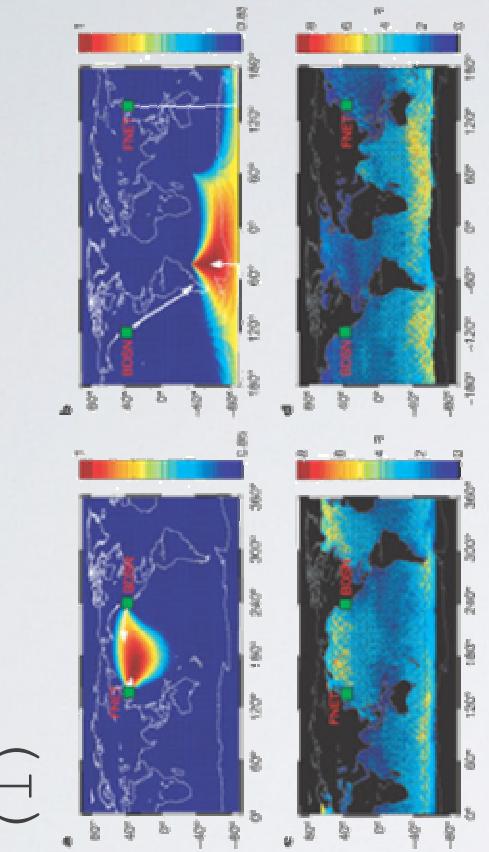
- In the north Pacific in winter

- In the southern hemisphere in summer

- Oceanic infragravity waves

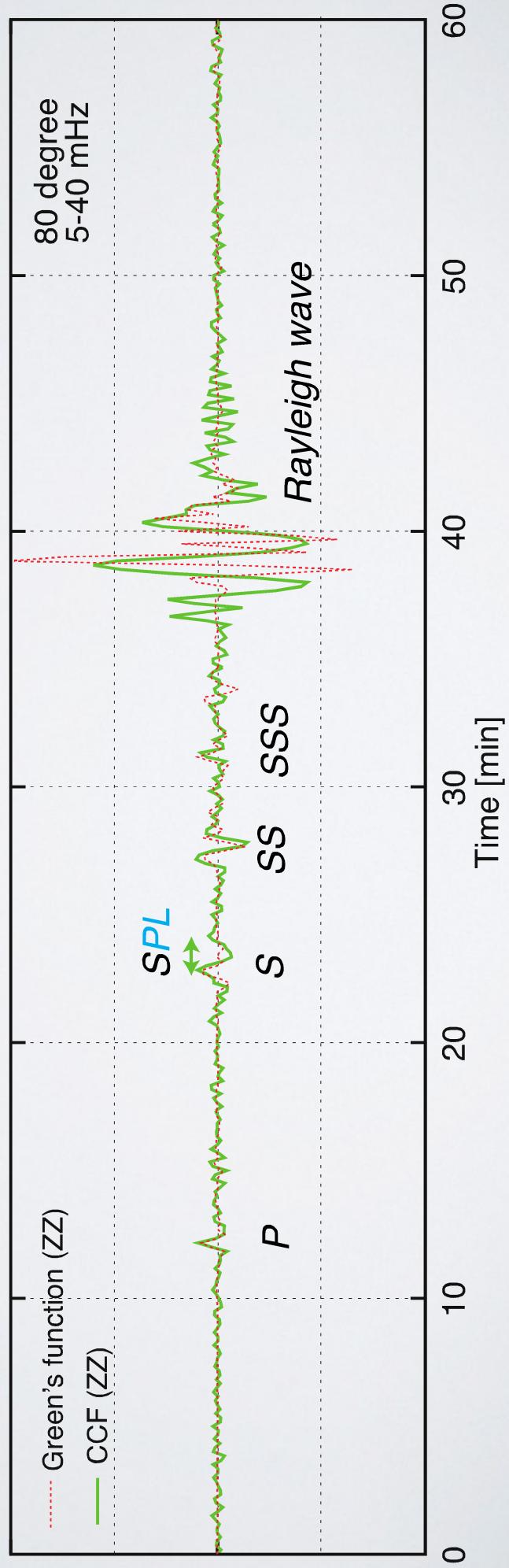
- Consistent with wave height data  
Watada and Masters [2001], R<sup>hie</sup> and Romonowicz [2004], Tanimoto [2005], Webb [2007]

Anyway pressure sources are dominant!  
Nishida and Fukao [2007]



# Dominance of SPL wave

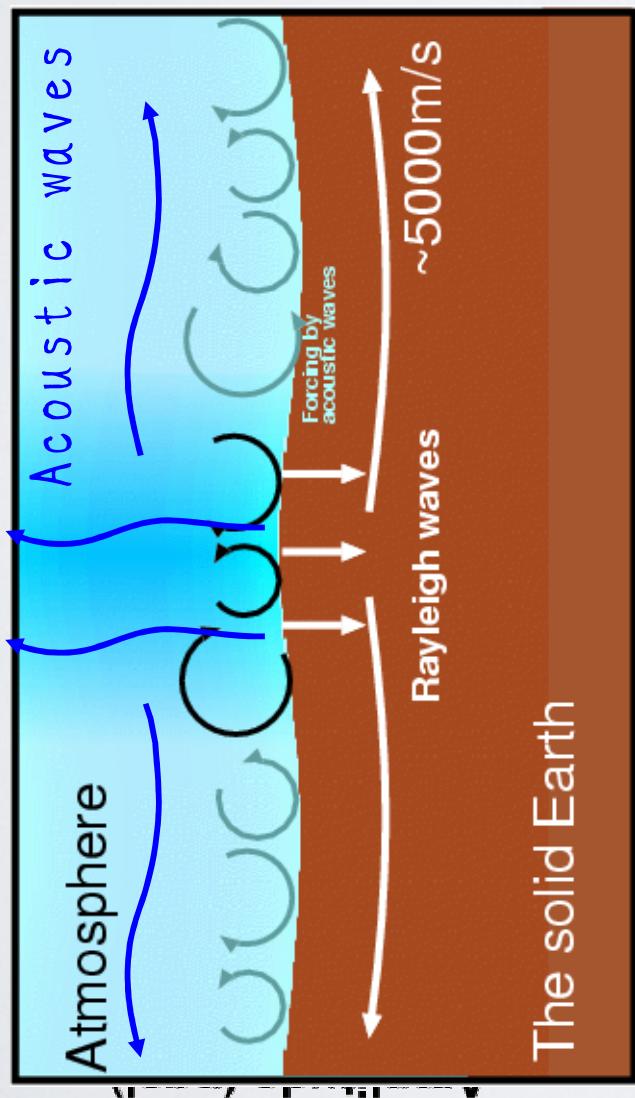
Lack of reflection phases  
Dominance of Shear-coupled PL (SPL) wave



# Conclusions

- Global propagation of body waves extracted by cross-correlation analysis of F-net, USArray, IRIS, FDSN, and ORFEUS data.
- The observed seismograms can be synthesized with an assumption of stochastic stationary excitation by random surface traction and random pressure sources.
- Travel time anomalies (S and SS) can be measured from phase difference between synthetic data and observed ones.

# Acoustic resonance

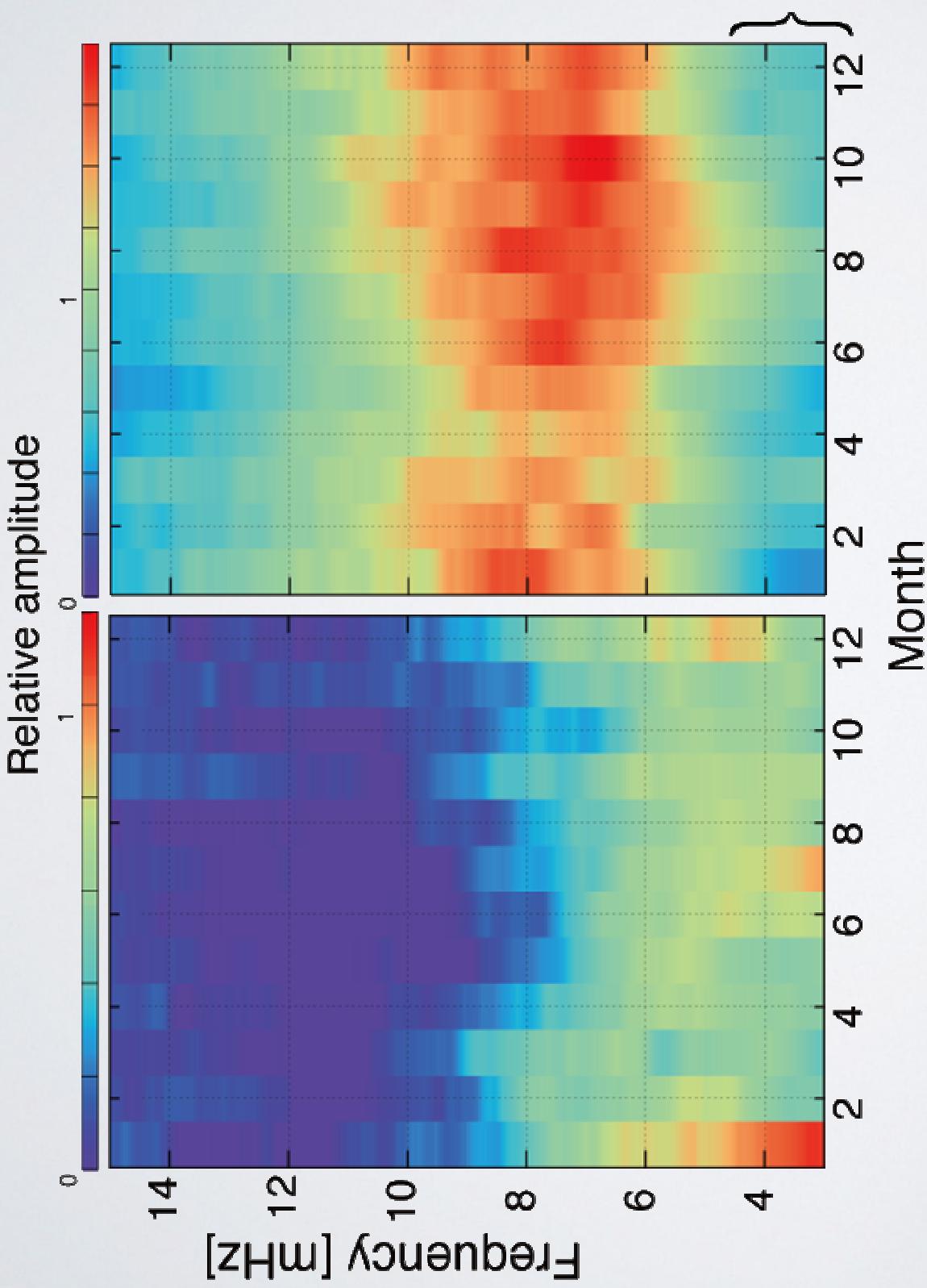


Mode number

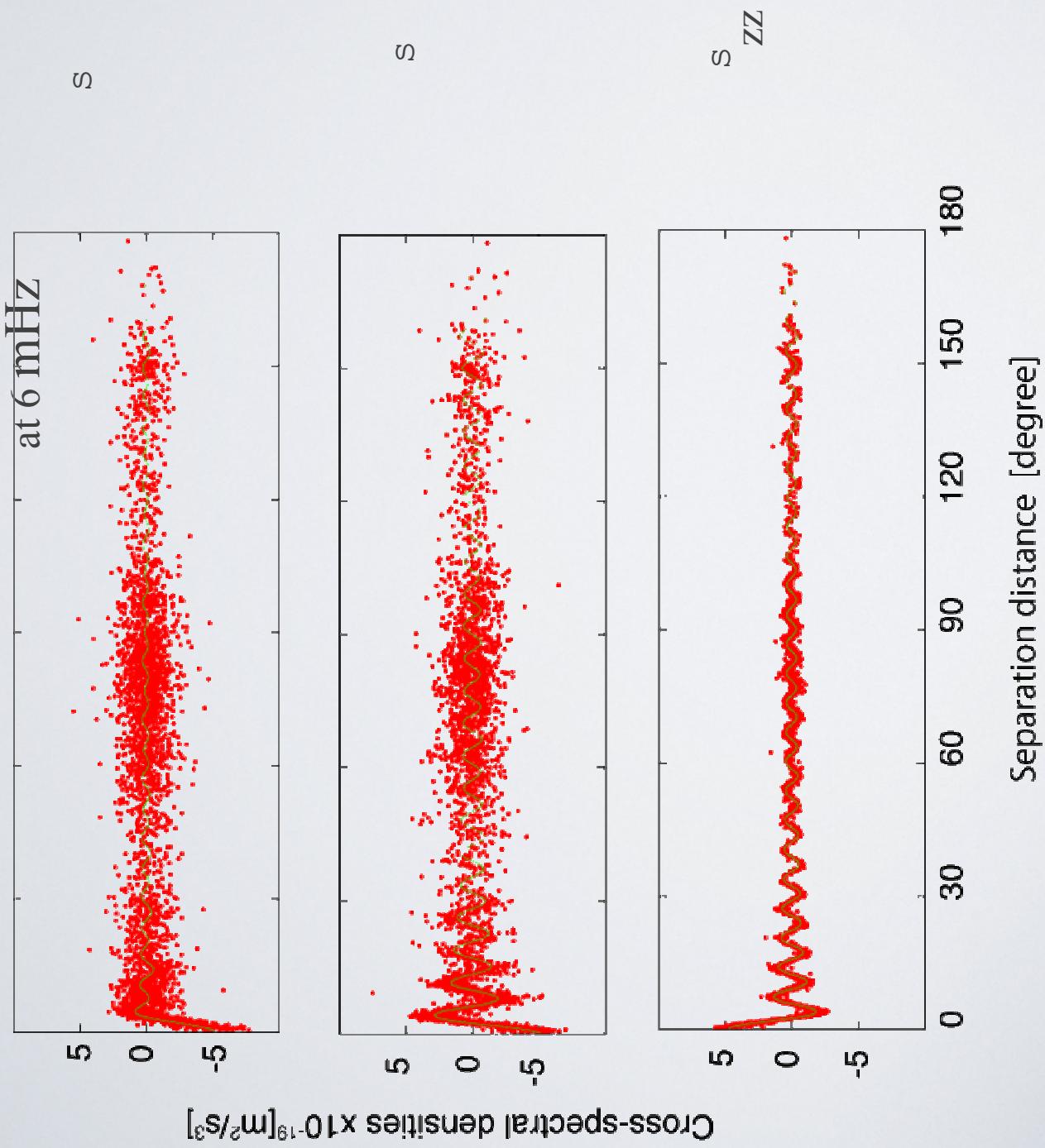
Nishida *et al.* [2000]

- Excess amplitudes:  $OS_{29}$ ,  $OS_{37}$  (220, 270 s)
- Atmospheric turbulence  $< 5 \text{ mHz}$

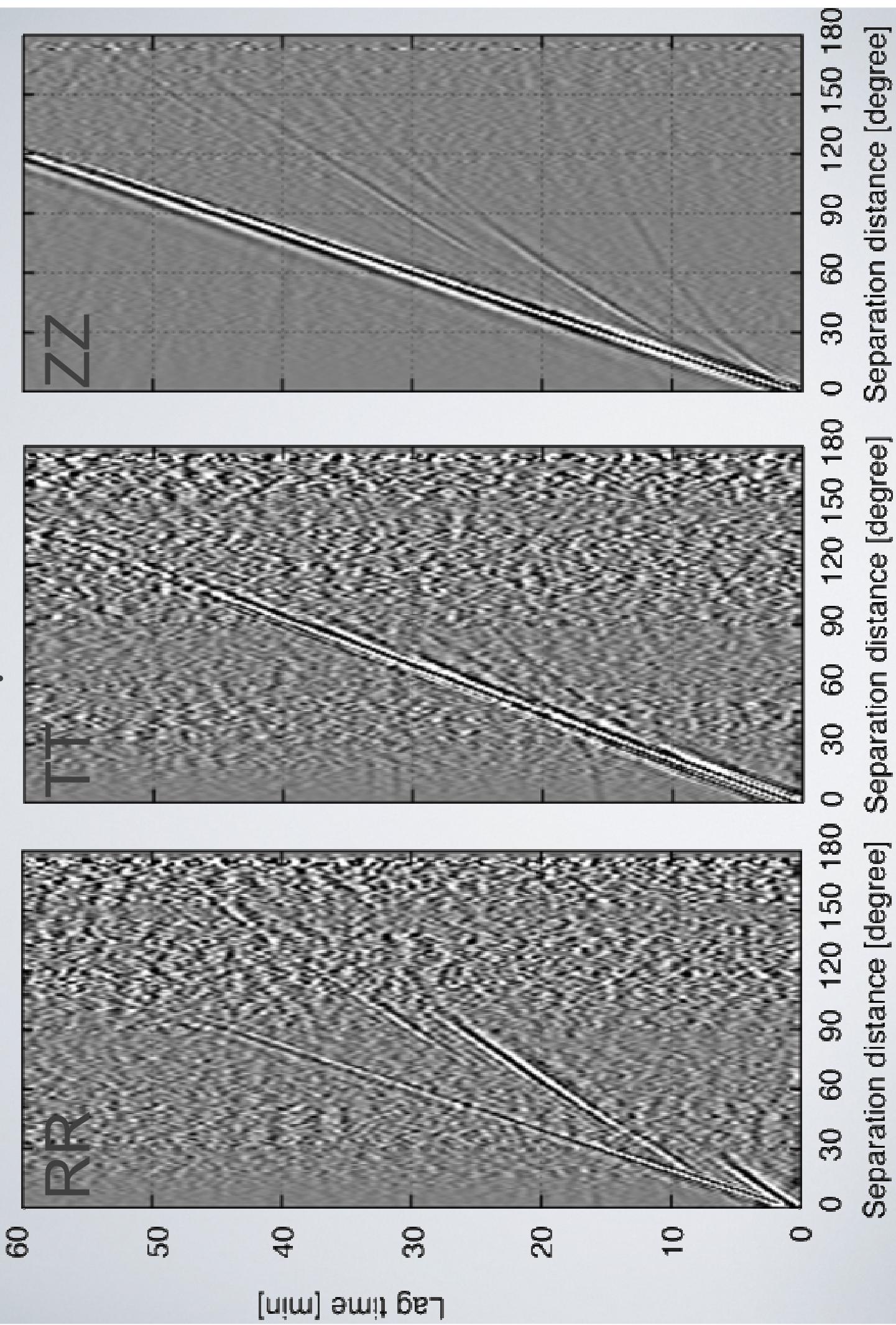
# SEASONAL VARIATIONS



# Fitting of cross spectra



# Travel time plots (CCFs)



# Synthetic cross-spectra

$$\Phi_{rr}(\Theta; \omega) = -R^2 \sum_l U_l^2 (\Psi_r^e U_l^2 + \Psi_h^e V_l^2) \frac{2l+1}{4\pi l(l+1)} |P_l(\cos\Theta)| n_l^r|^2 \quad (1)$$

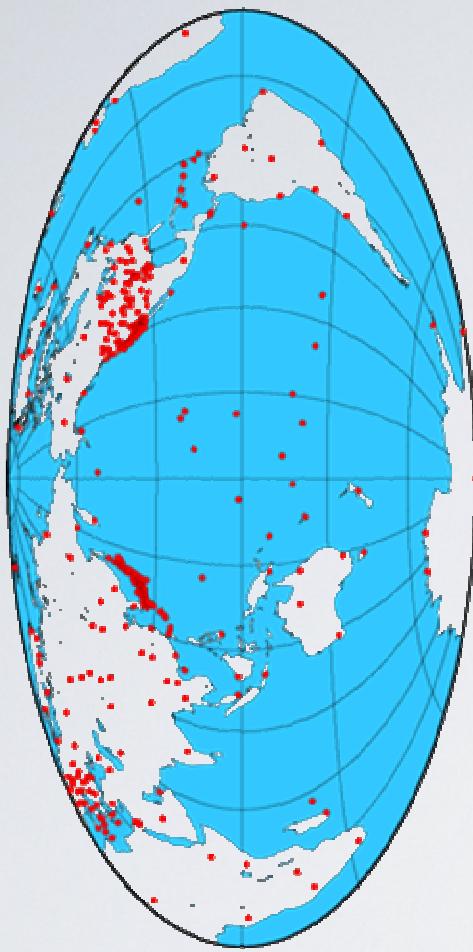
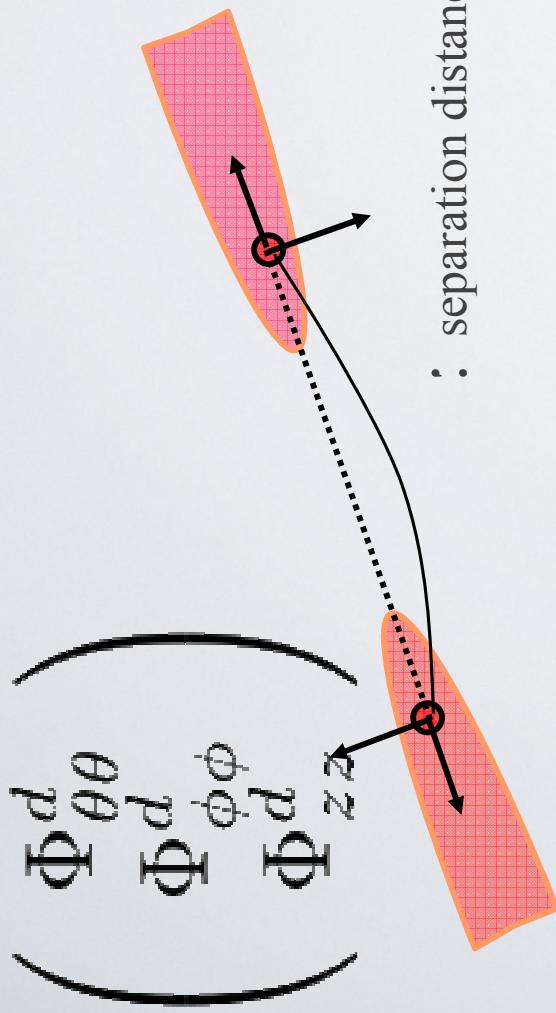
$$\Phi_{\theta\theta}(\Theta; \omega) = -R^2 \sum_l V_l^2 (\Psi_r^e U_l^2 + \Psi_h^e V_l^2) \frac{2l+1}{4\pi l(l+1)} \frac{d^2 P_l(\cos\Theta)}{d\Theta^2} |n_l^r|^2 \quad (2)$$

$$\begin{aligned} \Phi_{\phi\phi}(\Theta; \omega) &= -R^2 \sum_l W_l^4 \Psi_h^e \frac{2l+1}{4\pi l(l+1)\sin\Theta} \frac{dP_l(\cos\Theta)}{d\Theta} |n_l^r|^2 \\ &\quad - R^2 \sum_l W_l^4 \Psi_h^e \frac{2l+1}{4\pi l(l+1)\sin\Theta} \frac{d^2 P_l(\cos\Theta)}{d\Theta^2} |n_l^r|^2 \end{aligned} \quad (3)$$

$$\begin{pmatrix} \Phi_{\theta\theta}^s(\Theta, \Phi) \\ \Phi_{\phi\phi}^s(\Theta, \Phi) \\ \Phi_{zz}^s(\Theta, \Phi) \end{pmatrix} = \begin{pmatrix} K_{\theta r}(\Theta, \Phi) & K_{\theta h}(\Theta, \Phi) \\ K_{\phi r}(\Theta, \Phi) & K_{\phi h}(\Theta, \Phi) \\ K_{zr}(\Theta, \Phi) & K_{zh}(\Theta, \Phi) \end{pmatrix} \begin{pmatrix} \Psi_r \\ \Psi_h \end{pmatrix}$$

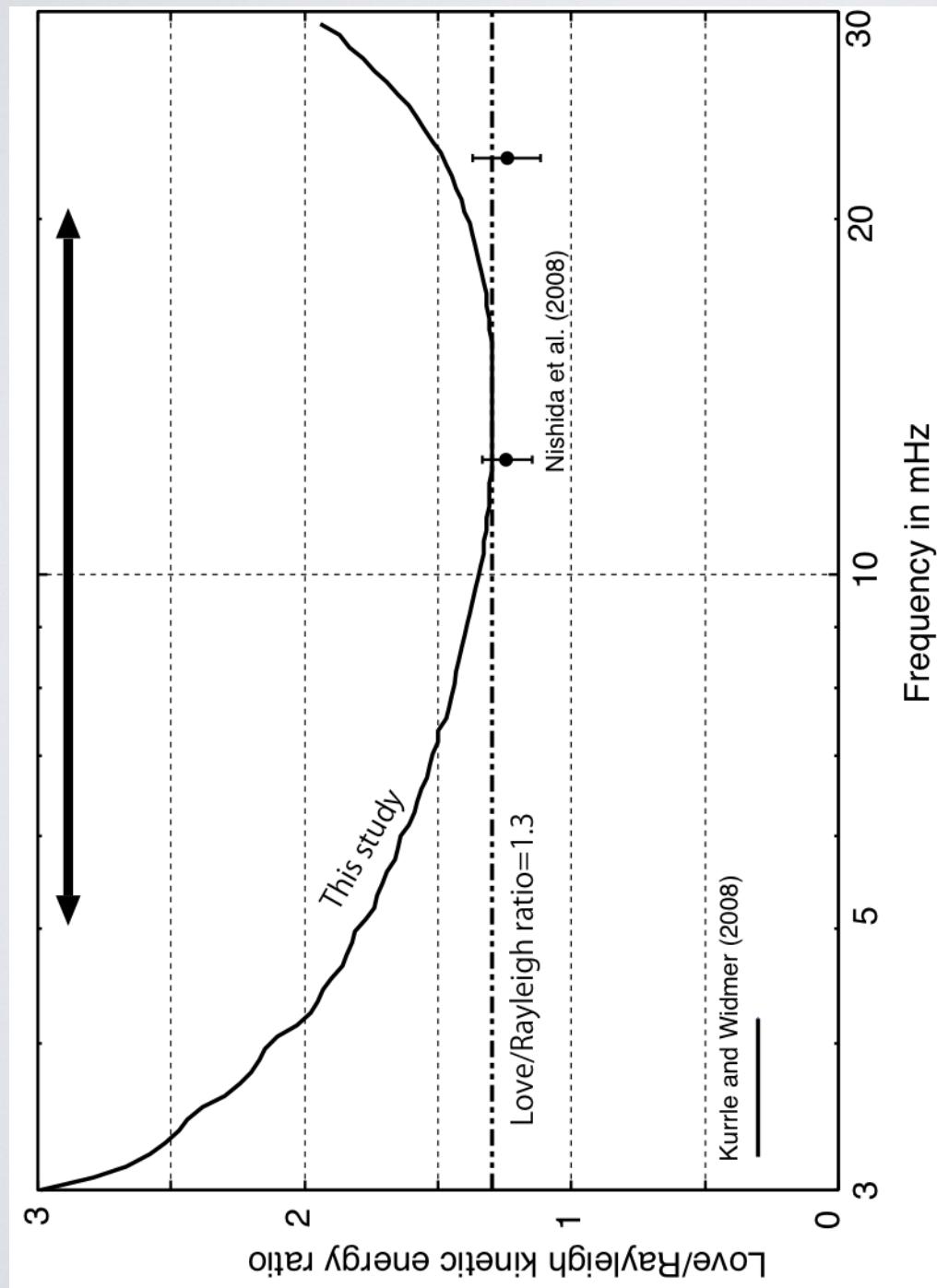
# Cross-correlation analysis

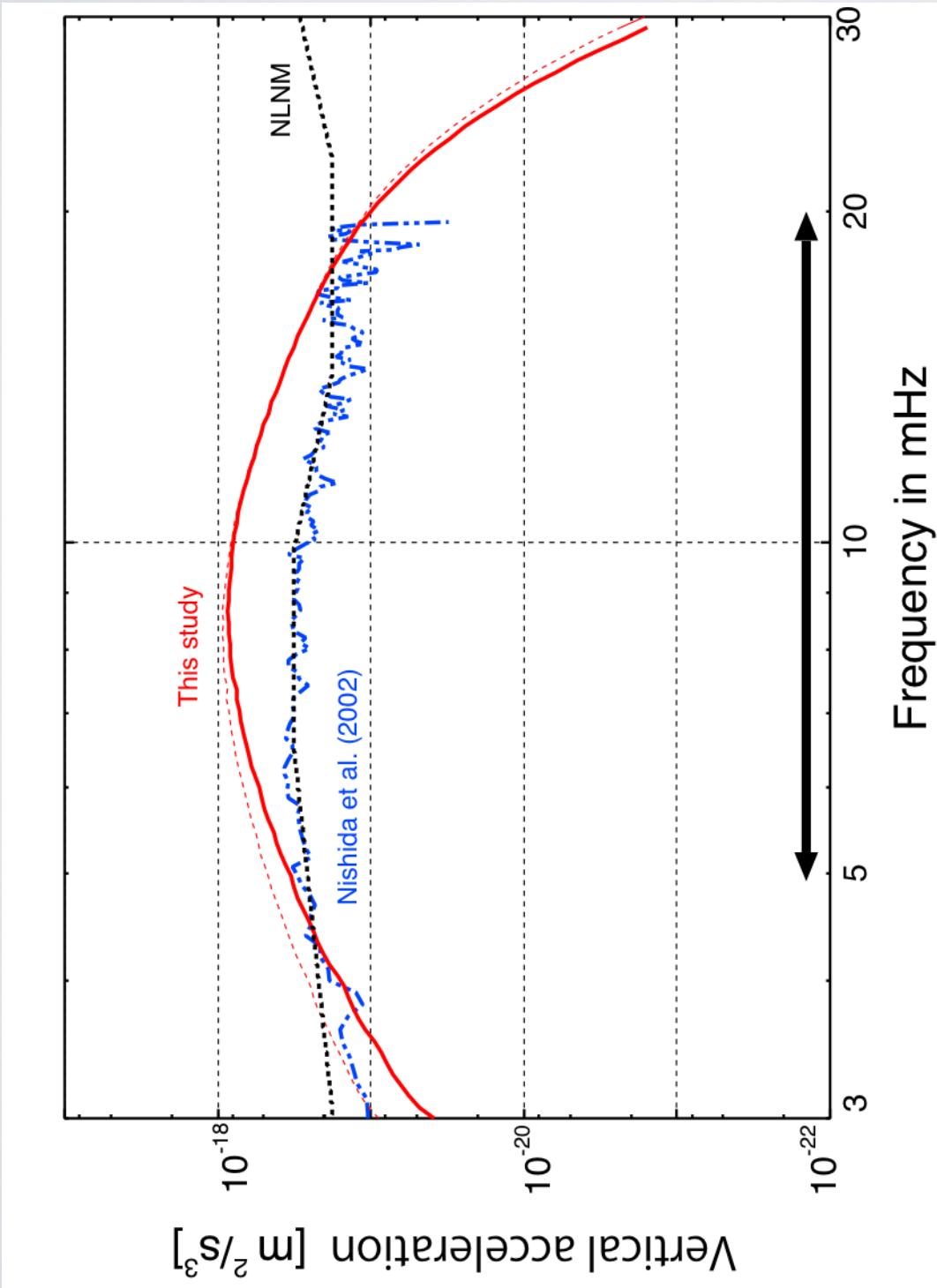
## Cross spectra



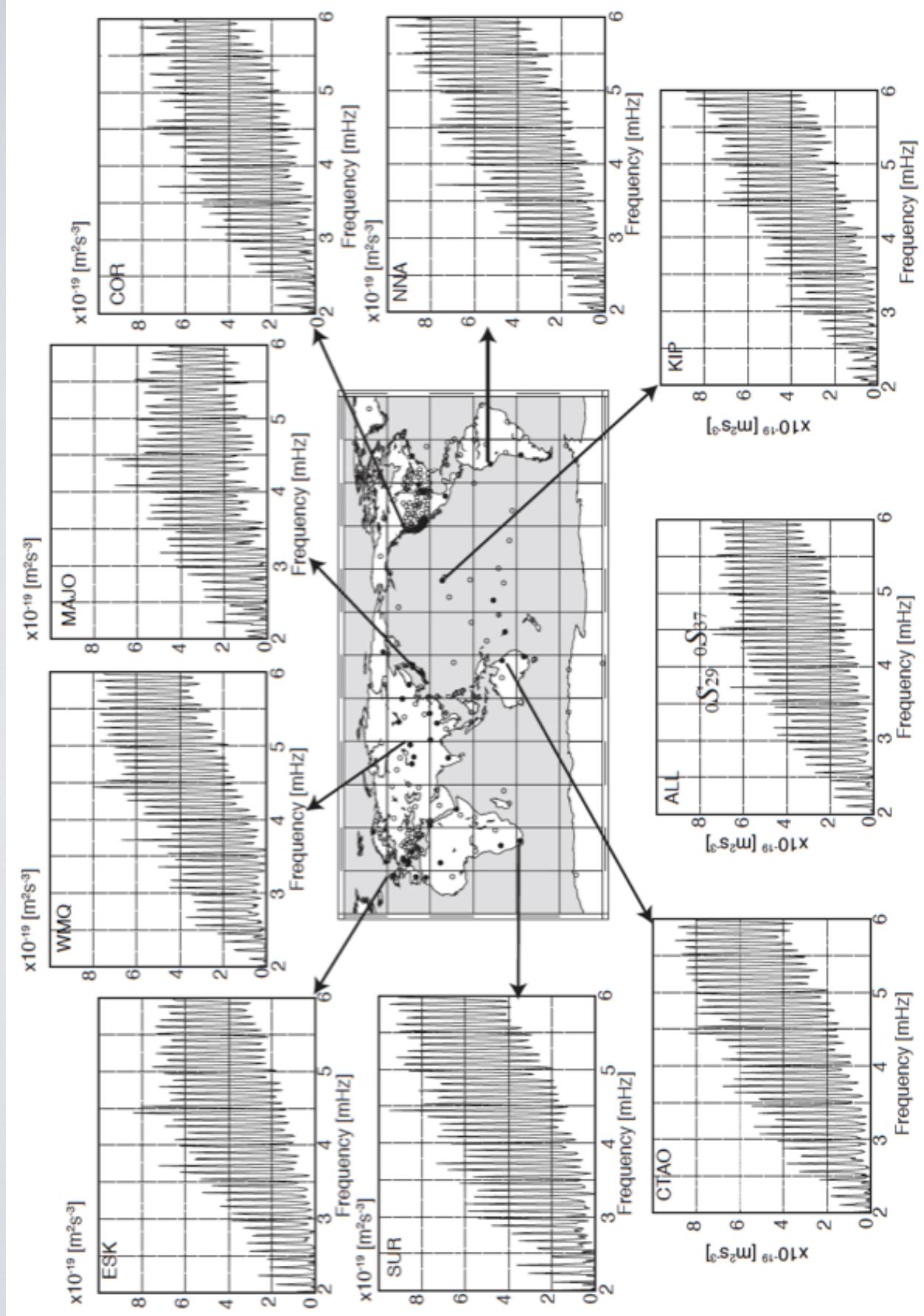
- Data: IRIS+ORFEUS+F-net STS1,2,2.5: 349 stations  
2004/1-2011/12

- Cross spectra: radial-radial, transverse-transverse, and vertical-vertical

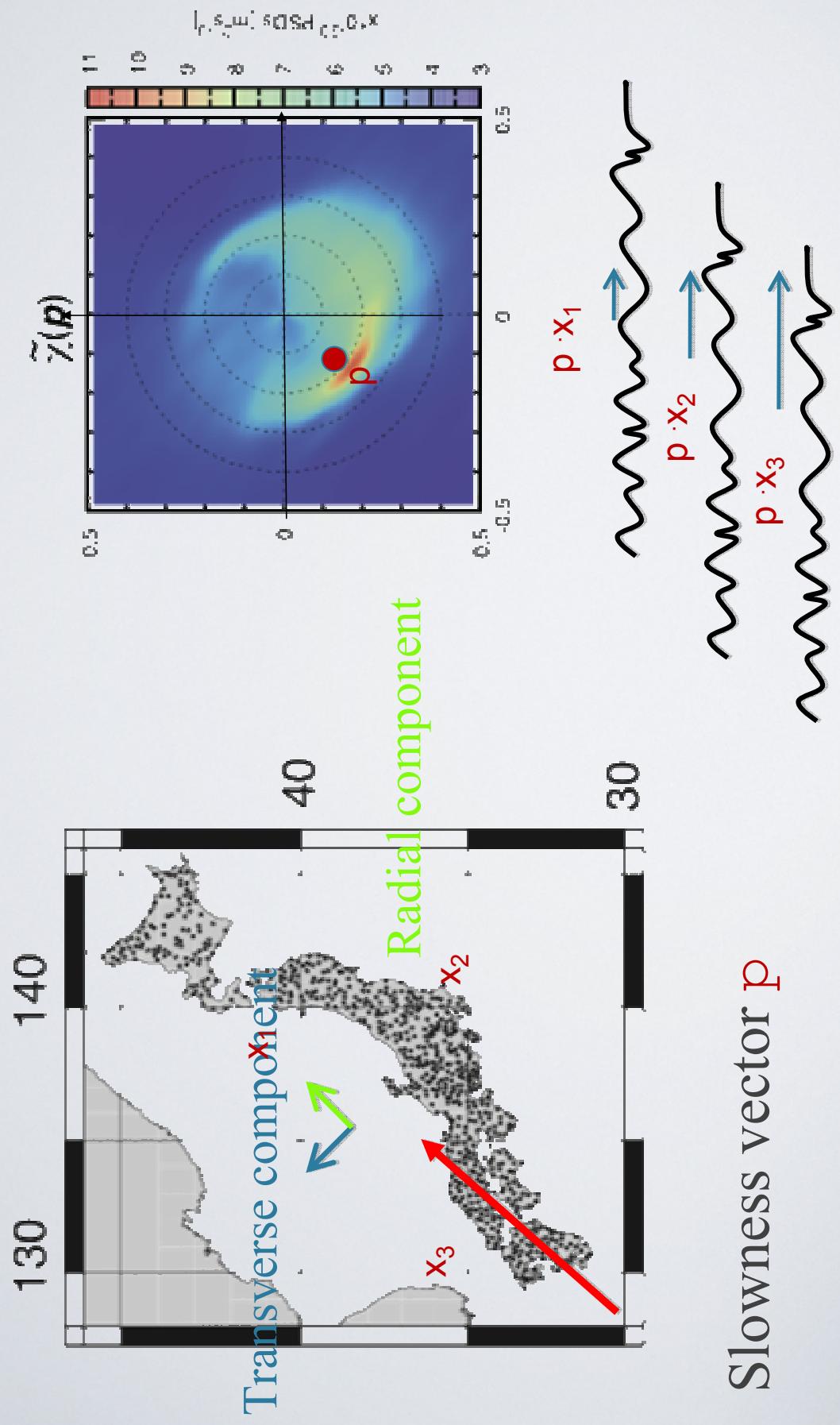




# Discovery of Earth's background free oscillations

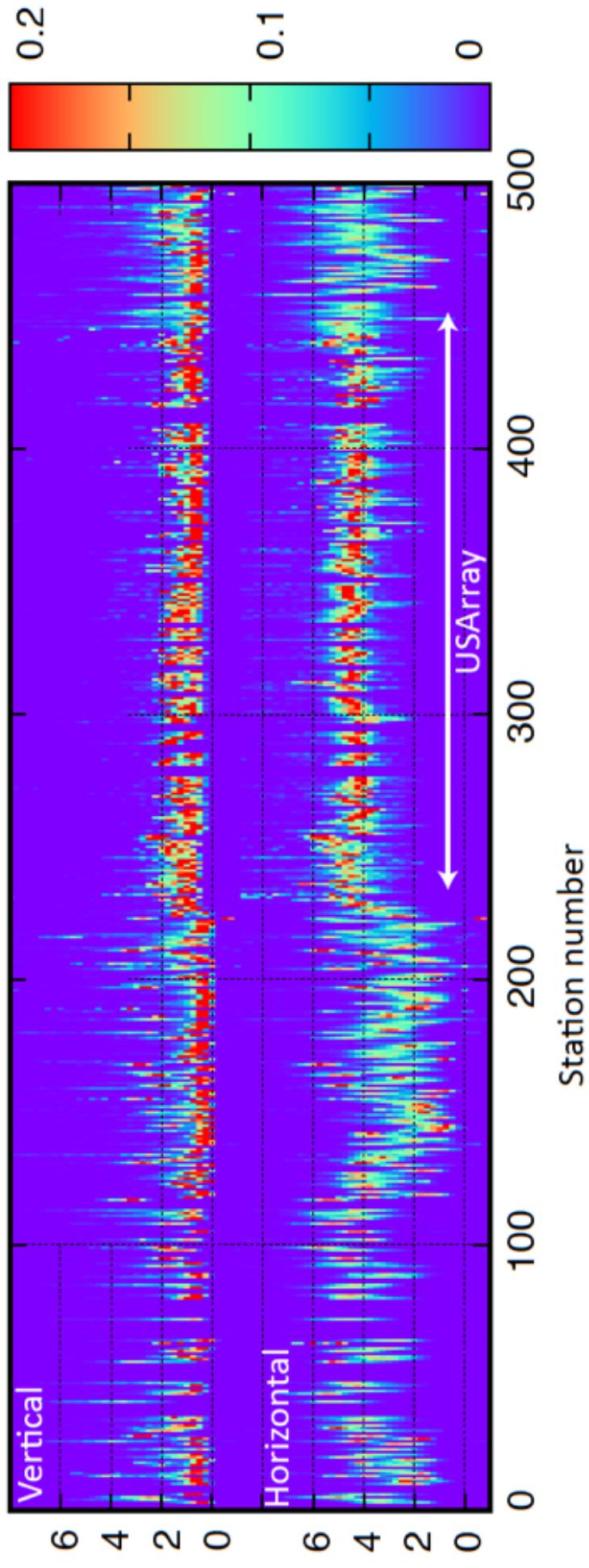


# Slant stack analysis

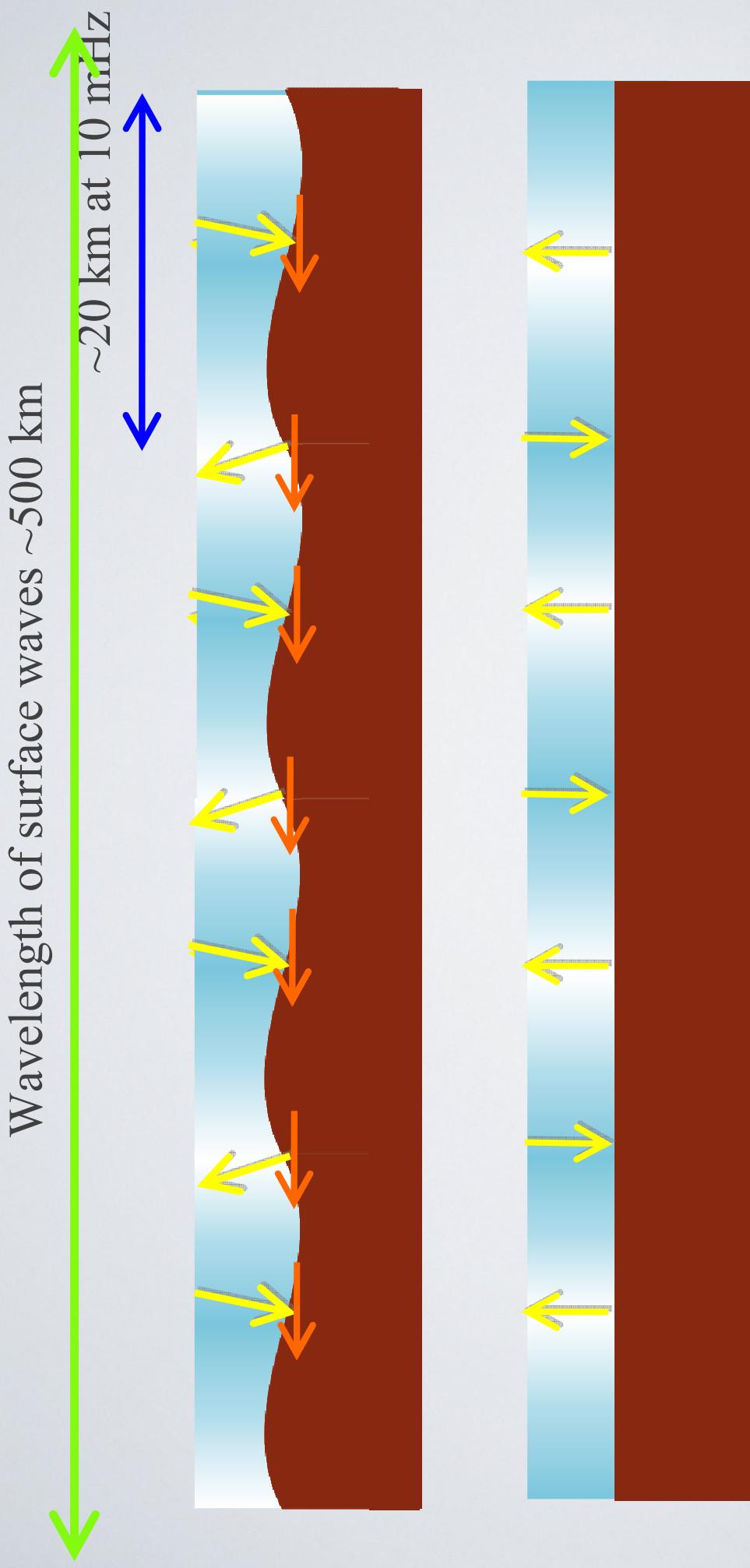


# Noise level

$\log_{10}(\text{PSD}/\text{NLNM})$



# Resonance of infragravity wave with seafloor topography



This mechanism can explain observed amplitudes

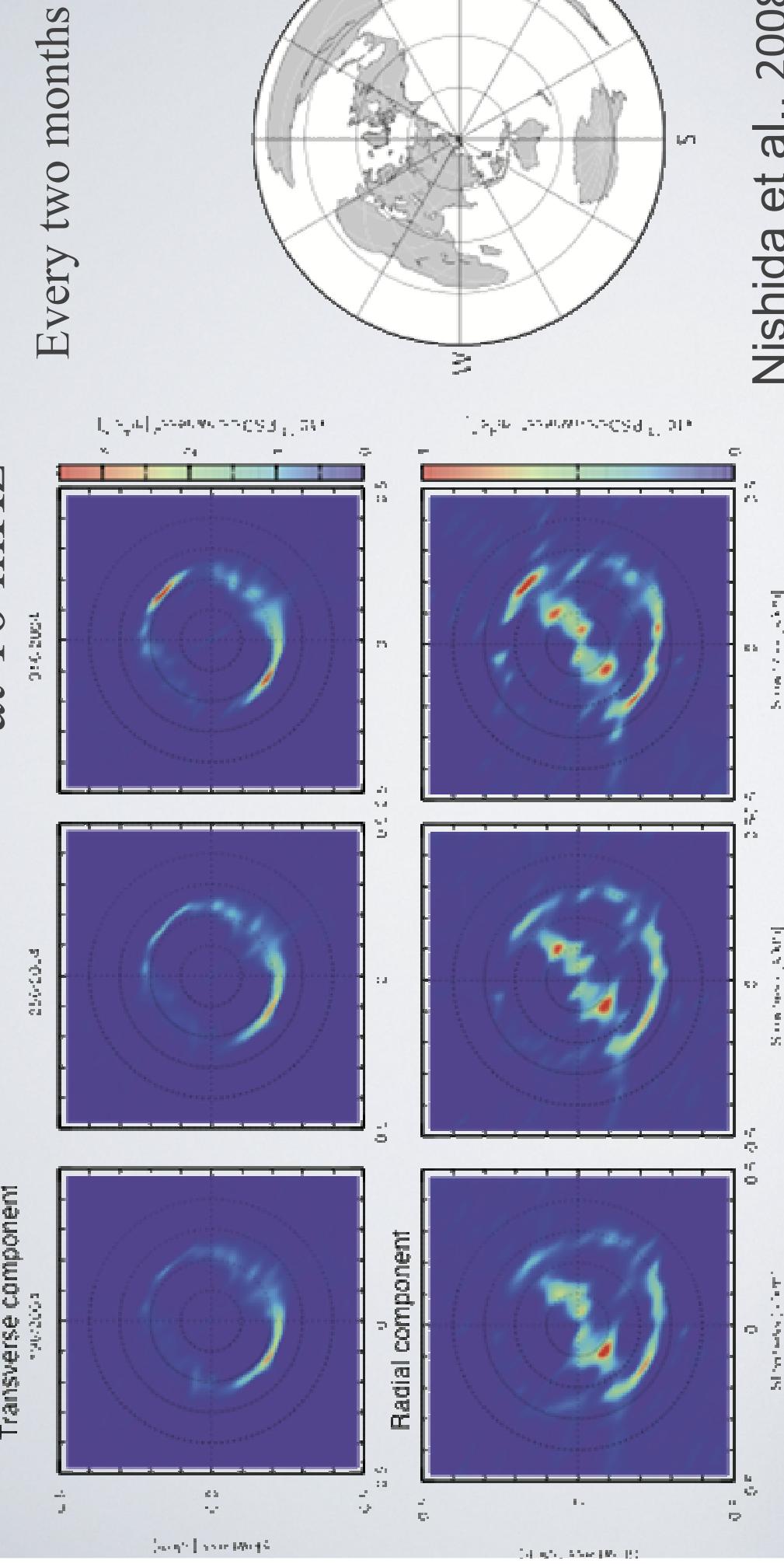
Fukao et al.,

# Slant stack analysis: Data set

- Hi-net horizontal accelerometers
- **679** stations, 2004/6-2004/12
- Data selections
- Exclusion of data contaminated by large earthquakes (Harvard CMT catalogue)
- Exclusion of noisy data and local transients

# Plots against slowness vector

at 10 mHz



# Why background Love waves?

- Pressure sources cannot excite Love waves for a spherical symmetric Earth
- Features of background Love waves is a key for understanding their excitation mechanism
- Data analysis:
  - Slant stack analysis [Nishida et al., 2008]
  - Auto-correlation analysis [Kurrale and Widmer, 2008]

# Power spectra

